

# Quantum to classical crossover of Floquet engineering in correlated quantum systems

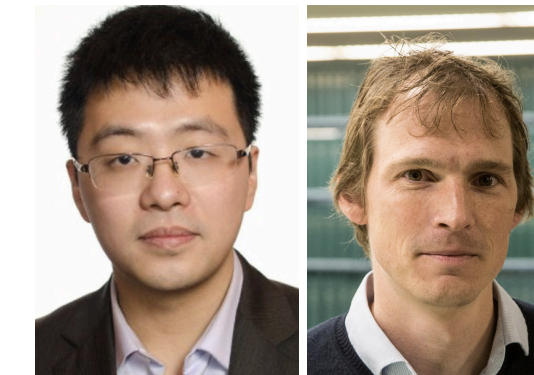
Michael A. Sentef

[lab.sentef.org](http://lab.sentef.org)

APS March meeting 2021  
March 17, 2021

**Cavity control of Hubbard model**

M.A. Sentef, J. Li, F. Künzel, M. Eckstein,  
PRResearch 2, 033033 (2020)



**Light-matter coupling and quantum  
geometry in moiré materials**

G. E. Topp, C. Eckhardt, D. M. Kennes,  
M.A. Sentef, P. Törmä,  
arXiv:2103.04967



Gabriel Topp, X46.00002, Friday 8:12

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DFG Emmy Noether programme (SE 2558/2)

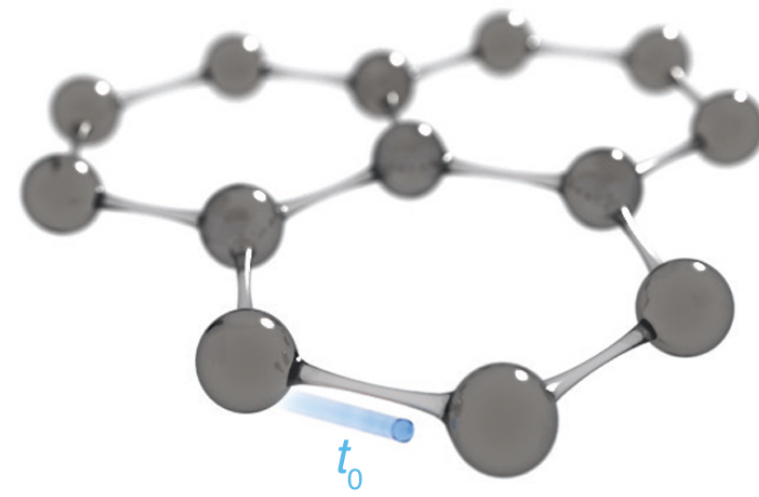


# Floquet engineering of quantum materials

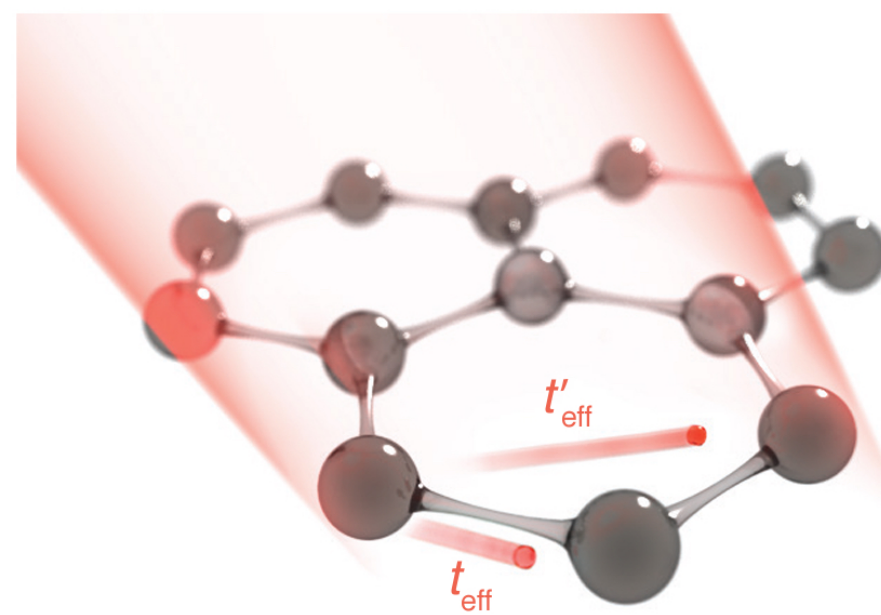
Oka & Kitamura, Ann. Rev. Condens. Matter Phys. 2019

Rudner & Lindner, Nat. Rev. Phys. 2020

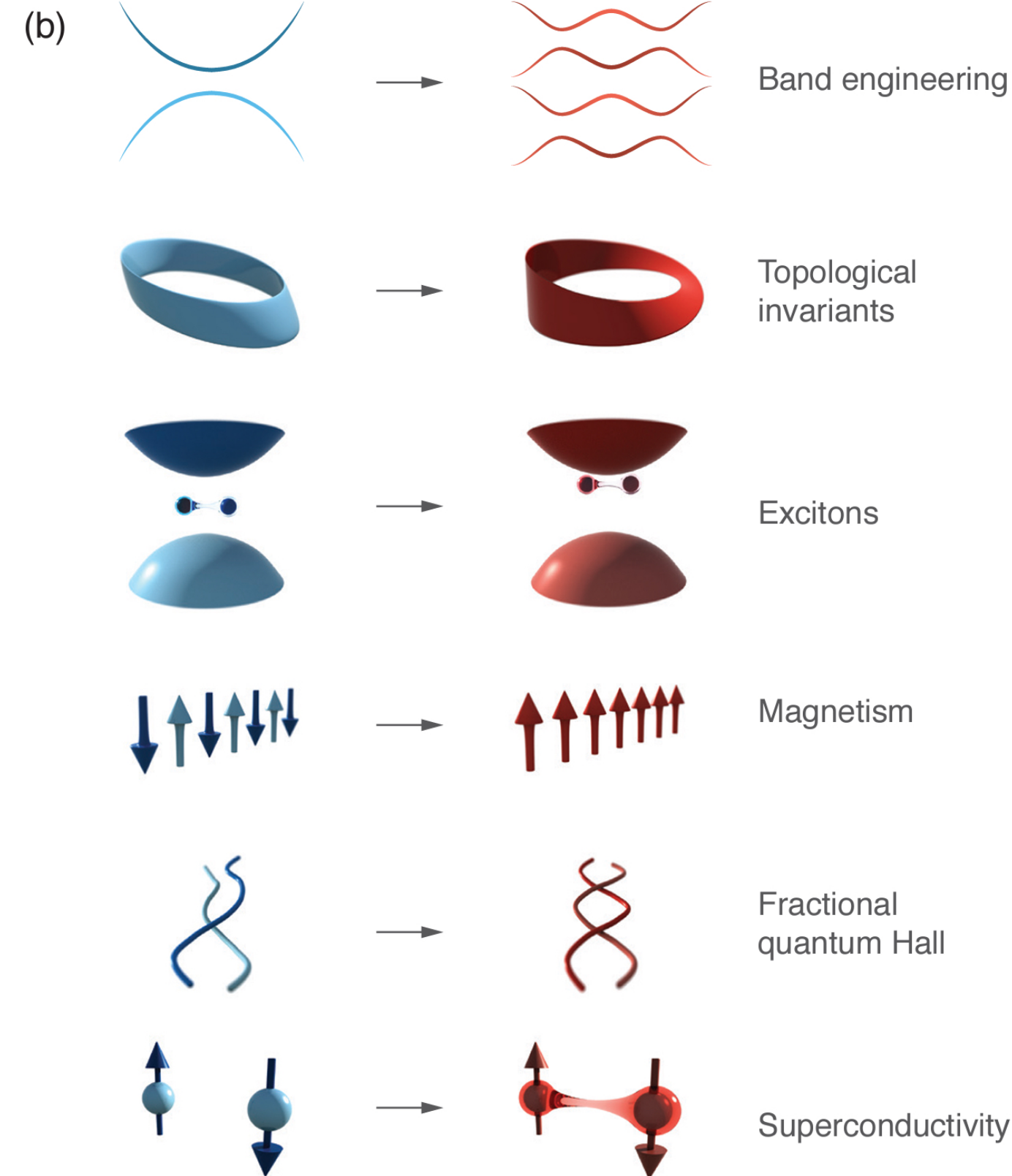
(a) Equilibrium



Optically dressed

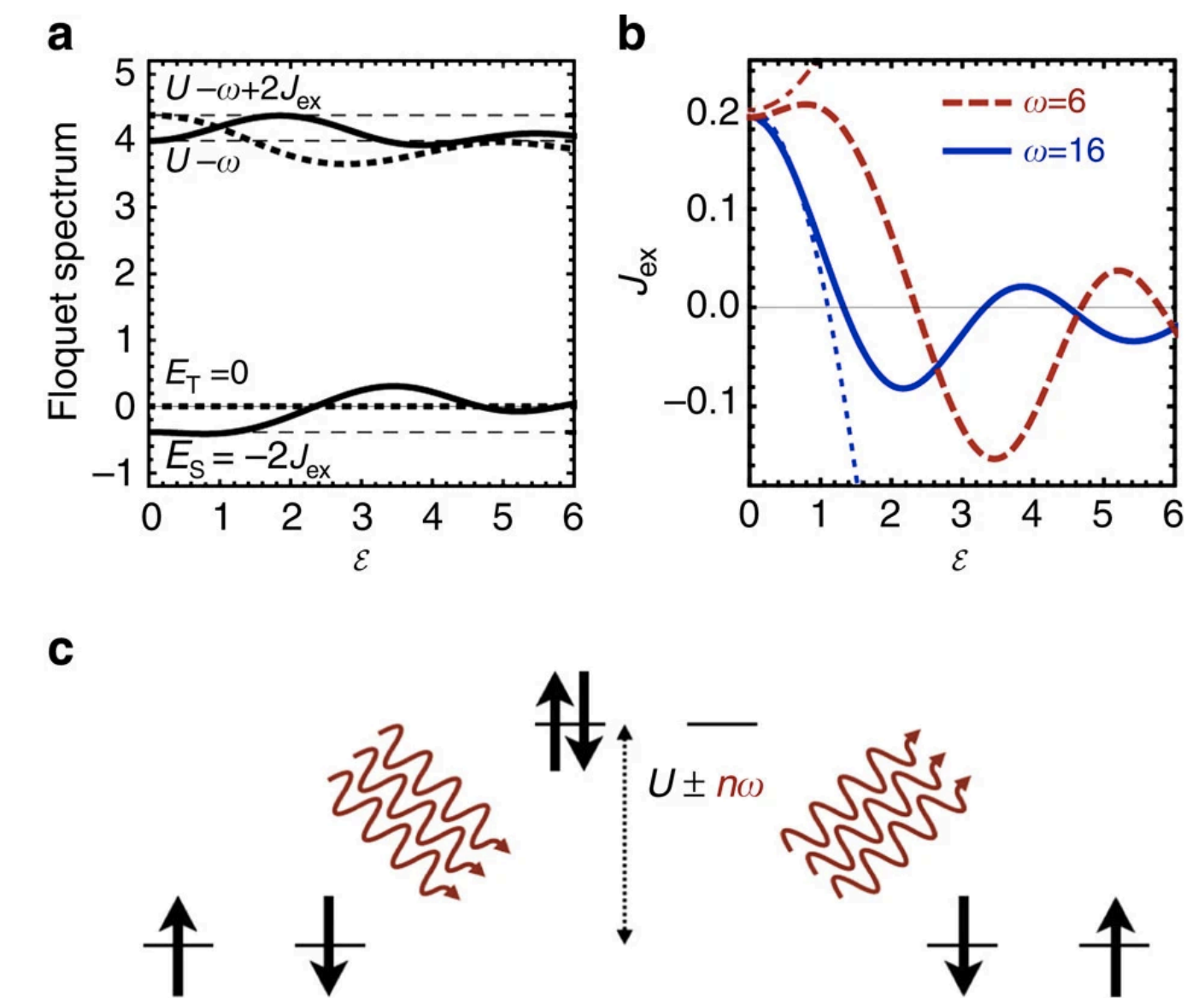


A. de la Torre, D. Kennes, M. Claassen, S. Gerber, J. Mclver, MAS, review in prep.



## Floquet engineering of spin exchange

Mentink, Balzer, and Eckstein, Nat. Commun. 6, 6708 (2015)



Photon dressing of intermediate states modifies kinetic exchange

But: need for strong lasers, problems with heating, short-lived effect

Question: can we control spin exchange with cavities?  
Answer: yes, if we replace strong fields by strong light-matter coupling



# QED quantum materials: strong light-matter coupling

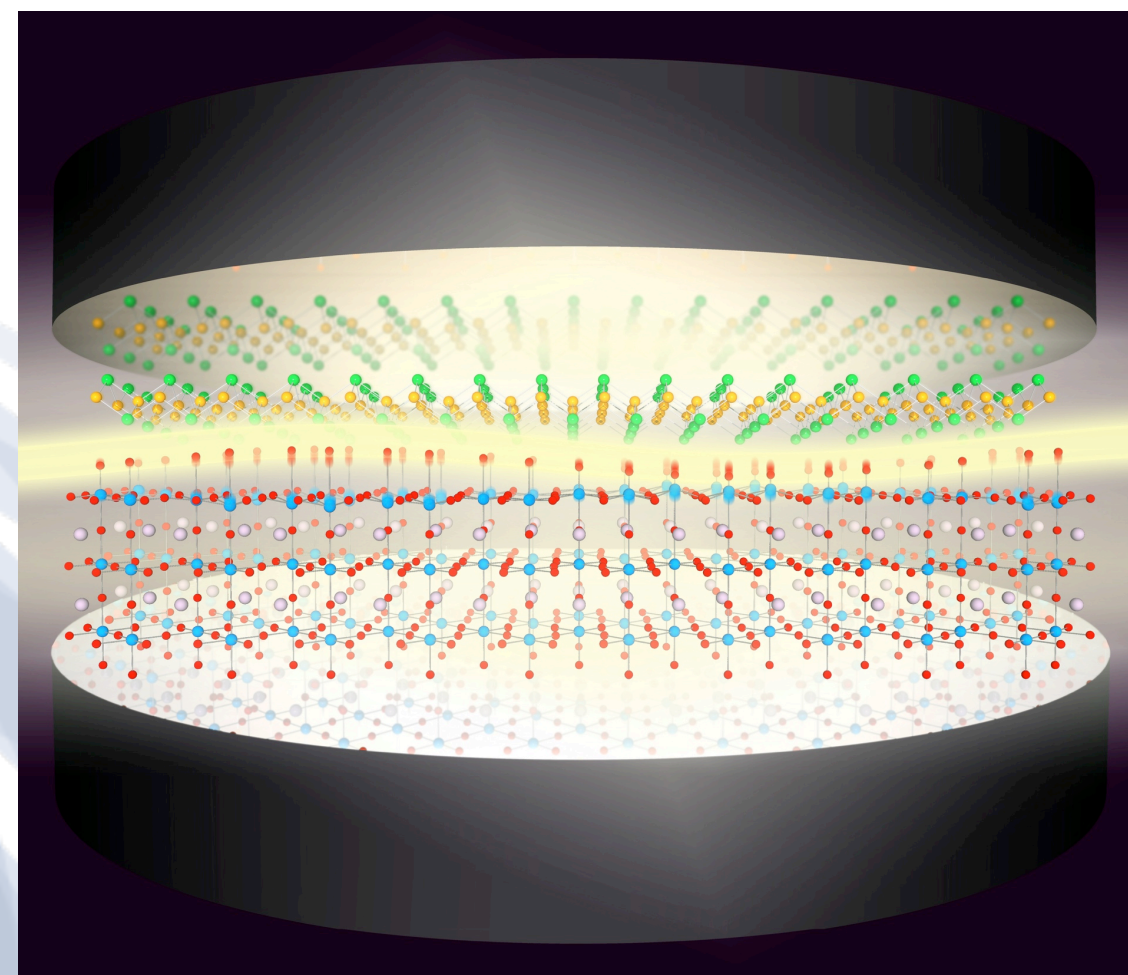
## Polaritonic chemistry

T. Ebbesen, Acc. Chem. Res. 49, 2403 (2016)  
 J. Feist et al., ACS Photonics 5, 205 (2017)  
 M. Ruggenthaler et al., Nat. Rev. Chem. 2, 0118 (2018)  
 R. F. Ribeiro et al., Chem. Sci. 9, 6325 (2018)  
 J. Flick et al., Nanophotonics 7, 1479 (2018)  
 A. F. Kockum et al., Nat. Rev. Phys. 1, 19 (2019)

## Quantum materials: towards cavity-controlled electron-boson coupling, superconductivity

Cavity quantum-electrodynamical polaritonically enhanced electron-phonon coupling and its influence on superconductivity

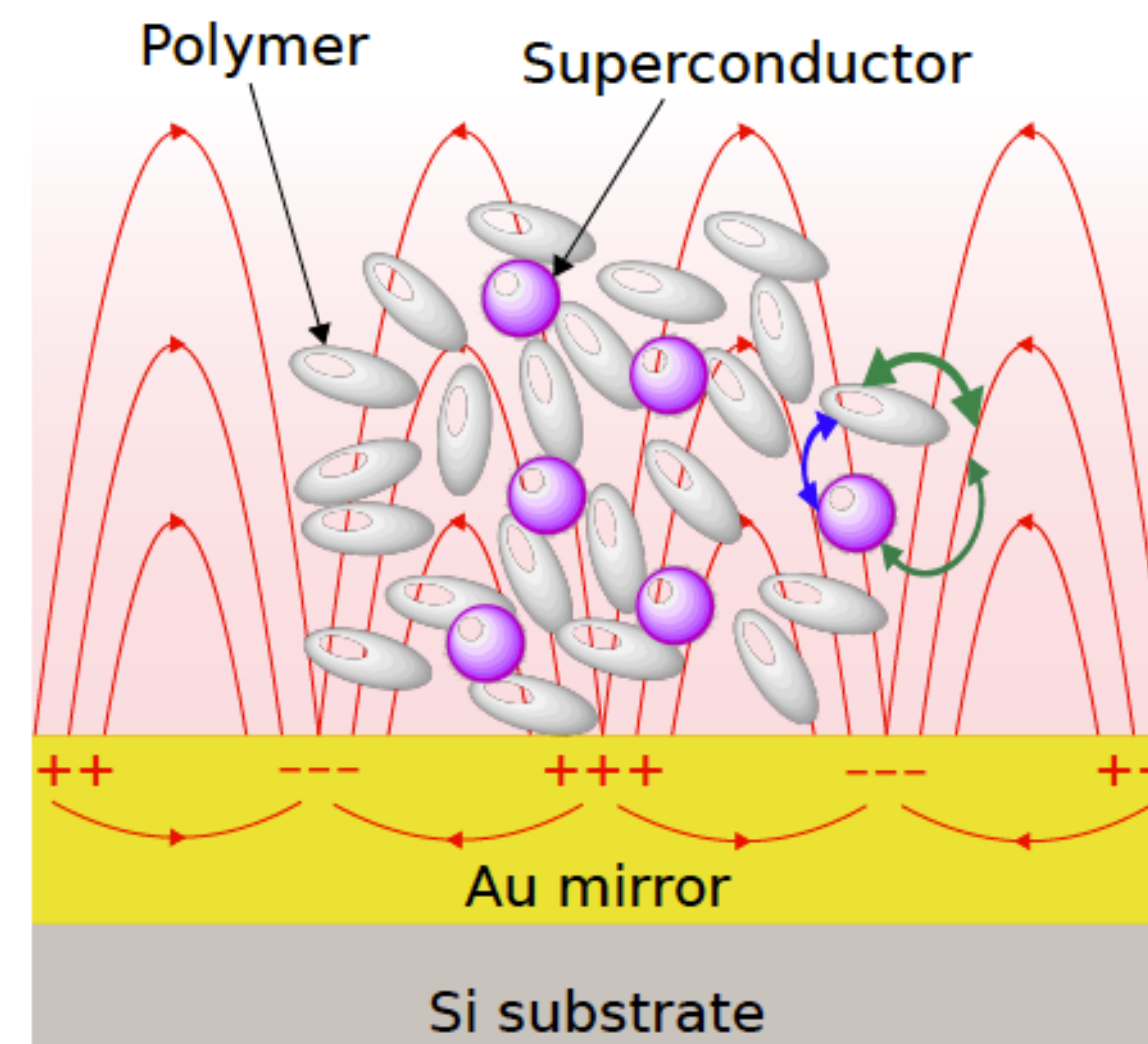
M.A. Sentef, M. Ruggenthaler, A. Rubio,  
 Science Advances 4, eaau6969 (2018)



### Exploring Superconductivity under Strong Coupling with the Vacuum Electromagnetic Field

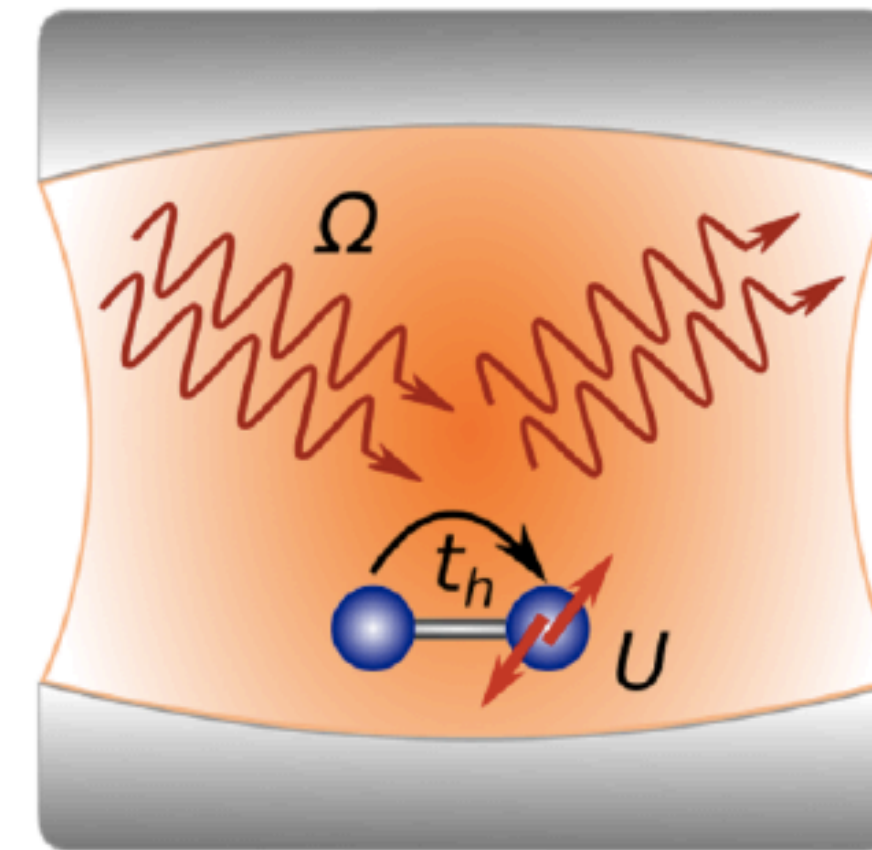
A. Thomas<sup>1</sup>, E. Devaux<sup>1</sup>, K. Nagarajan<sup>1</sup>, T. Chervy<sup>1</sup>, M. Seidel<sup>1</sup>, D. Hagenmüller<sup>1</sup>, S. Schütz<sup>1</sup>,  
 J. Schachenmayer<sup>1</sup>, C. Genet<sup>1</sup>, G. Pupillo<sup>1\*</sup> & T. W. Ebbesen<sup>1\*</sup>

arXiv:1911.01459

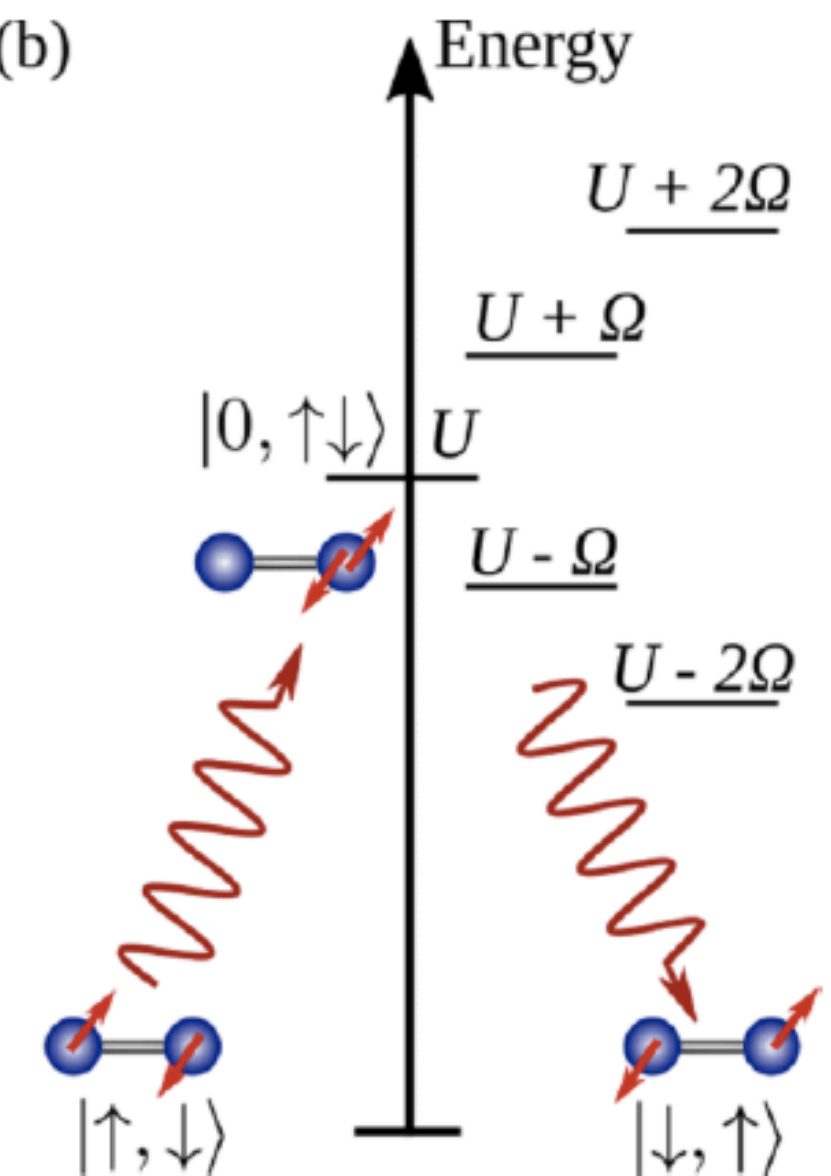


## Our work: cavity control of spin exchange Crossover from quantum to classical Floquet engineering

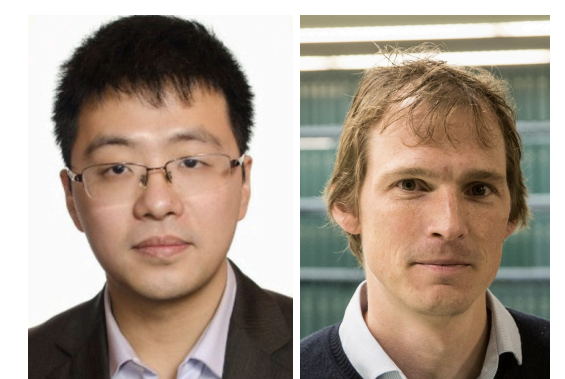
(a)



(b)



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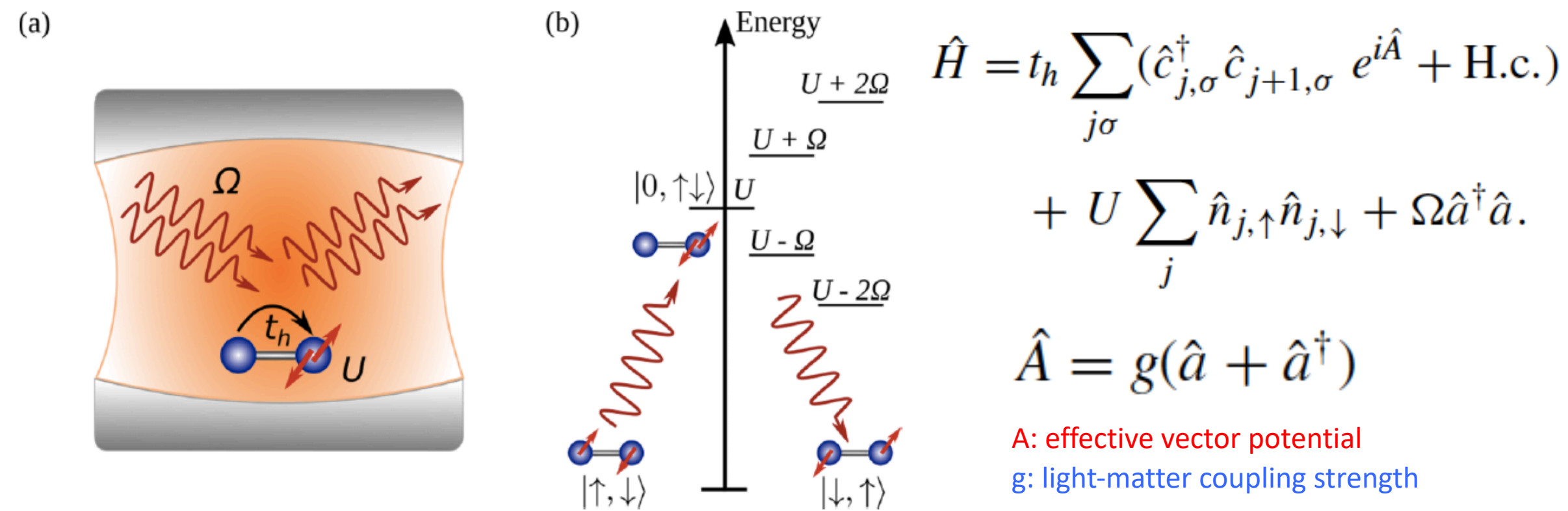
Cavity materials: Laussy, Kavokin, Shelykh 2010, Cotlet et al 2016, Kavokin & Lagoudakis 2016, Schlawin, Cavalleri, Jaksch 2019, Hagenmüller et al 2019, Curtis et al 2019, Wang, Ronca, MAS 2019, Kiffner et al 2019, Mazza & Georges 2019, Andolina et al 2019, Gao et al 2020, Chakraborty & Piazza arXiv 2020, Li & Eckstein 2020, Hübener et al 2020, Ashida et al 2020, Latini et al arXiv 2021, ...

Michael Sentef — Max Planck Institute for the Structure and Dynamics of Matter



# QED quantum materials: quantum to classical crossover

## Hubbard model in cavity

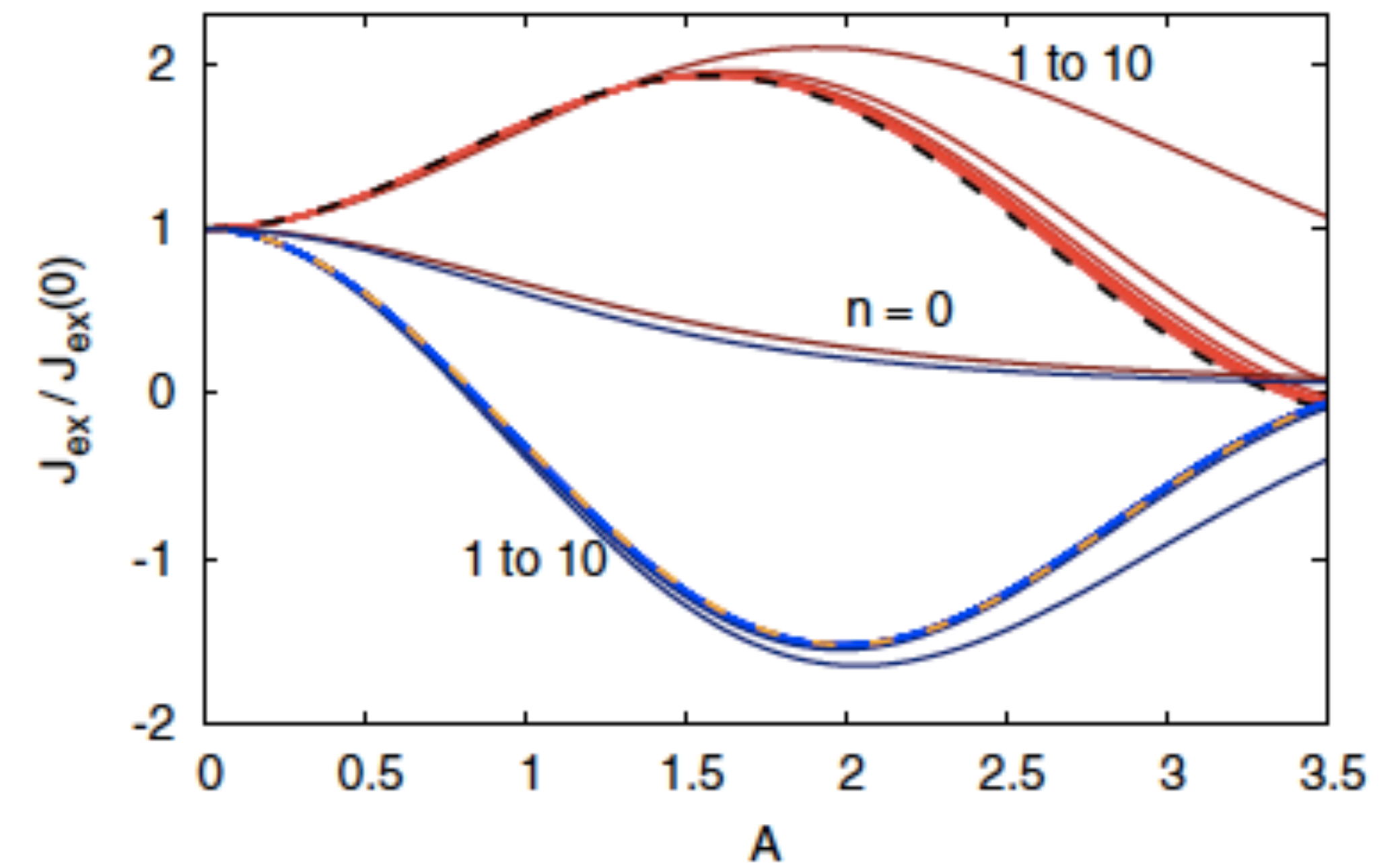


Quantum system  $\rightarrow$  Floquet system for  $n \rightarrow \infty$ ,  $g\sqrt{n}$  fixed.  
(large photon number, weak light-matter coupling strength  $g$ )

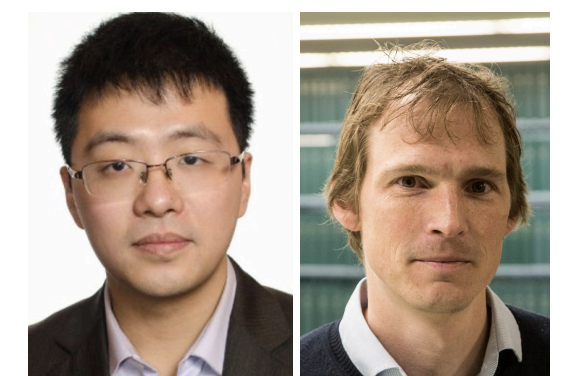
Photon number states are good enough to see Floquet-engineering effects at sufficiently large coupling strength  $g$  – **coherent states not required!**

Question: can we control spin exchange with cavities?  
Answer: yes, if we replace strong fields by strong light-matter coupling

## Cavity Schrieffer-Wolff transformation (confirmed by numerics)

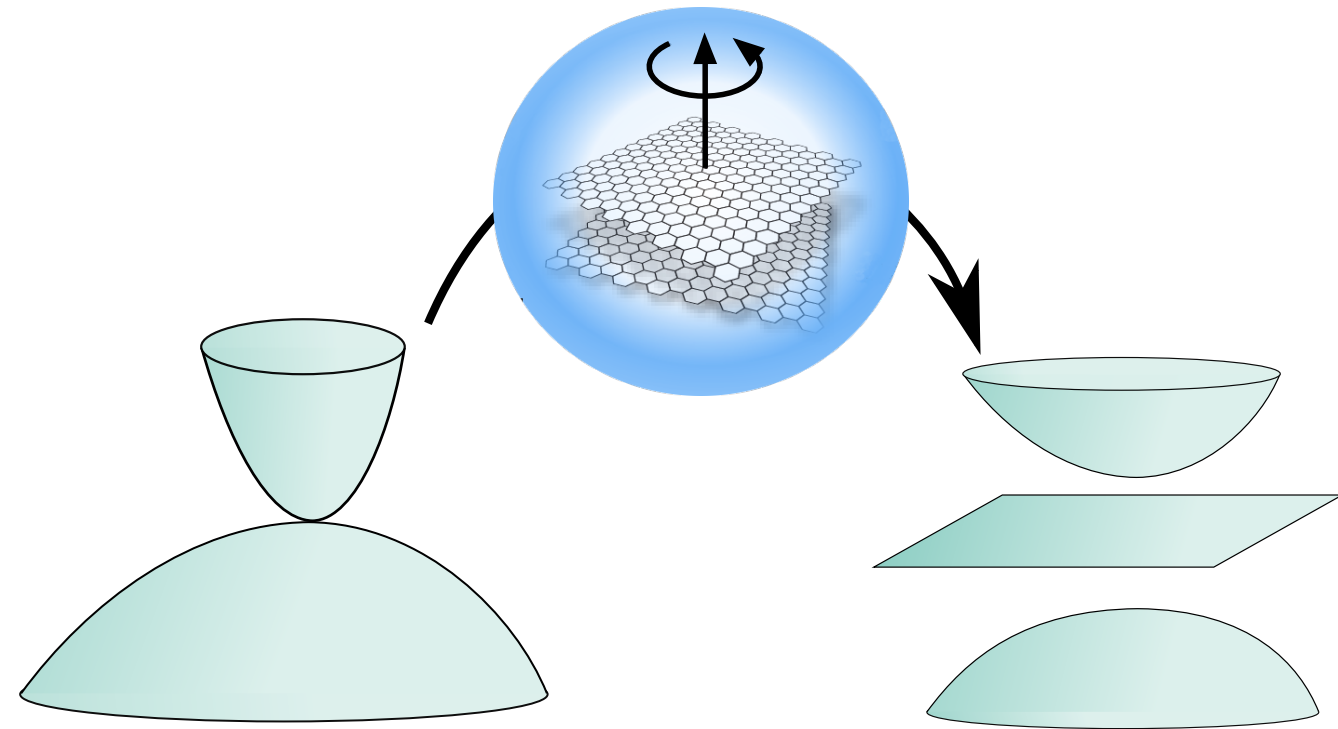


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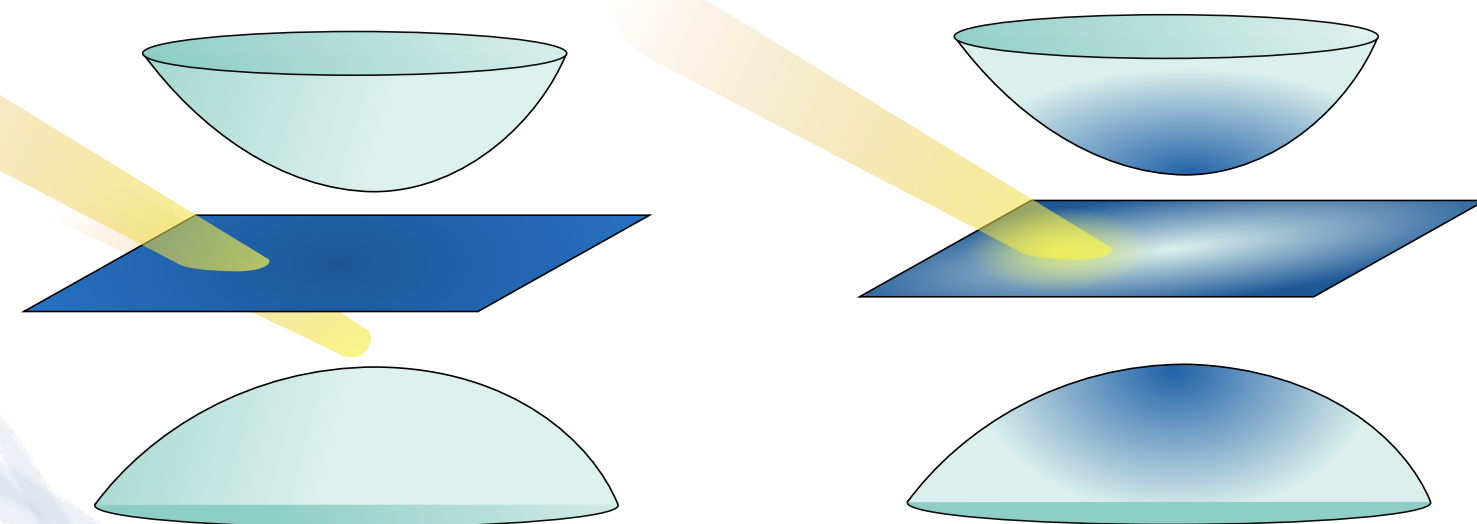


# QED quantum materials: how to reach strong coupling?



trivial quantum geometry

non-trivial quantum geometry



	Linear ( $A_\mu$ )	Quadratic ( $A_\mu A_\nu$ )
Intra-band ( $n$ )	$\partial_\mu \varepsilon_n$	$\partial_\mu \partial_\nu \varepsilon_n - \sum_{n' \neq n} (\varepsilon_n - \varepsilon_{n'}) (\langle \partial_\mu n   n' \rangle \langle n'   \partial_\nu n \rangle + \text{h.c.})$ <b>curvature without band curvature</b>
Inter-band ( $n, m$ )	$(\varepsilon_n - \varepsilon_m) \langle m   \partial_\mu n \rangle$	$\left[ \frac{1}{2} (\partial_\mu \varepsilon_n - \partial_\mu \varepsilon_m) \langle m   \partial_\nu n \rangle + \frac{1}{2} \varepsilon_m \langle \partial_\mu \partial_\nu m   n \rangle \right. \\ \left. + \frac{1}{2} \varepsilon_n \langle m   \partial_\mu \partial_\nu n \rangle + \sum_{n'} \varepsilon_{n'} (\langle \partial_\mu m   n' \rangle \langle n'   \partial_\nu n \rangle) \right] + (\mu \leftrightarrow \nu)$

Non-trivial quantum geometry enables light-matter coupling in flat bands

Can we reach strong light-matter coupling by quenching electronic kinetic energy?

**Light-matter coupling and quantum geometry in moiré materials**

G. E. Topp, C. Eckhardt, D. M. Kennes, M. A. Sentef, P. Törmä, arXiv:2103.04967

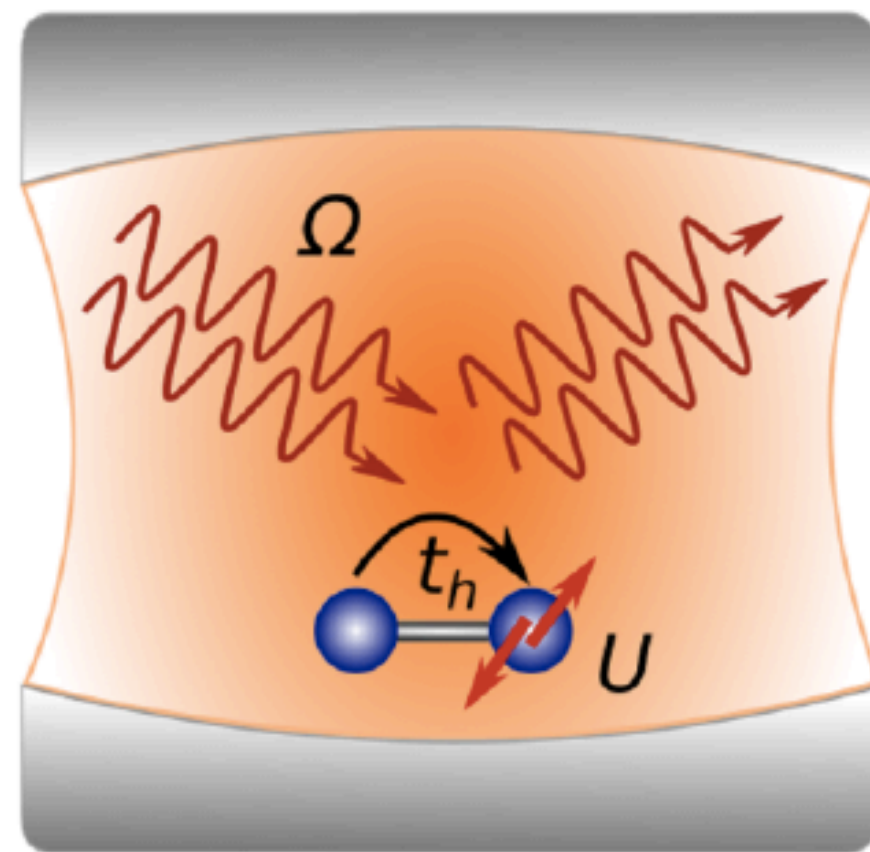
Also cf. Iskin PRA 2019; Ahn, Guo, Nagaosa, Viswanath arXiv 2021



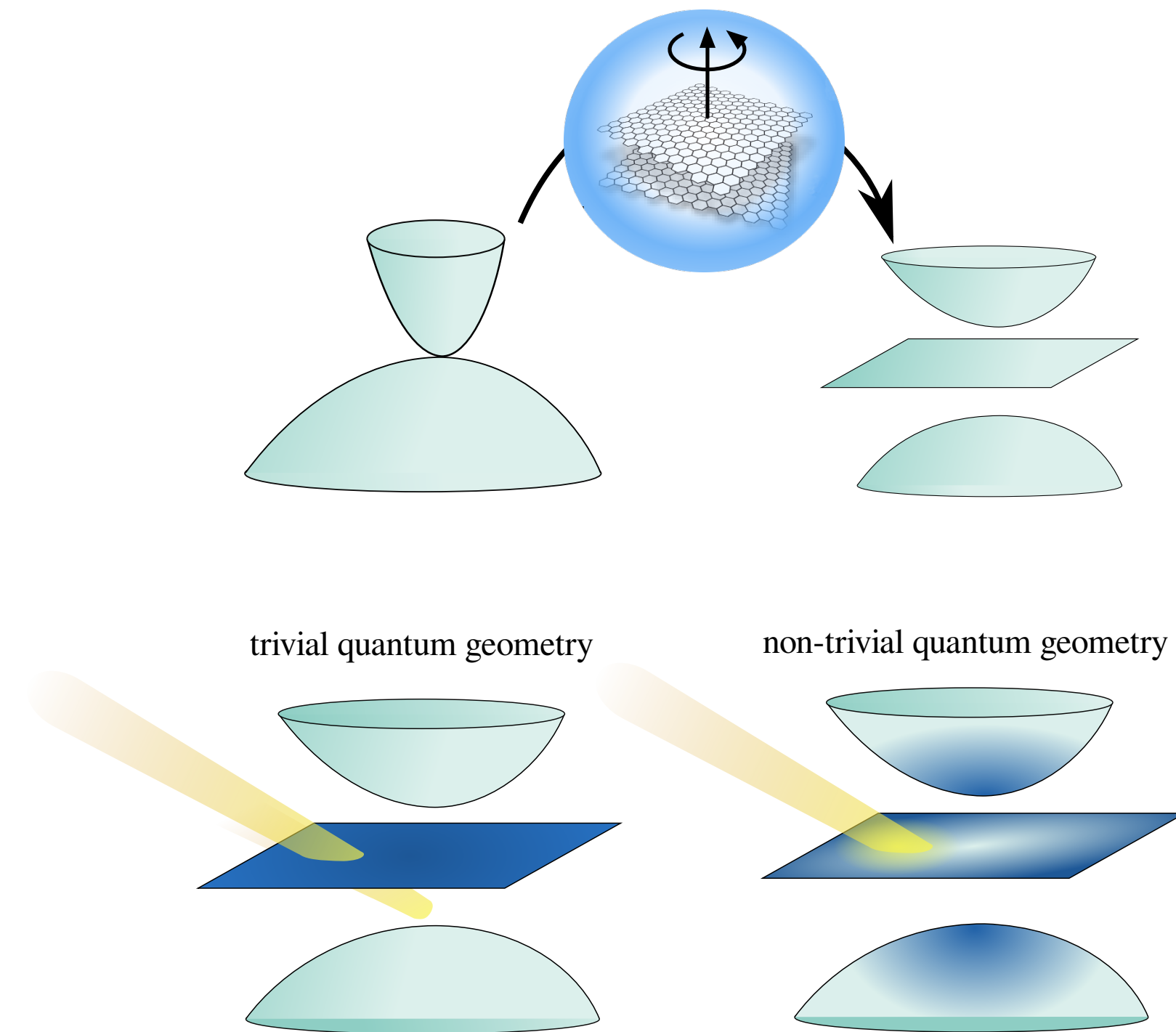
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# Summary



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