

# Nonequilibrium Materials Engineering beyond Floquet

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Max-Planck Institute for the Structure and Dynamics of Matter, Hamburg  
Boston University, November 2, 2018

# Team

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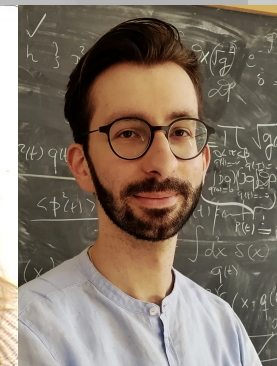
MAS

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Mona  
Kalthoff  
(Dortmund  
-> MPSD)



Matteo  
Puviani  
(Modena)

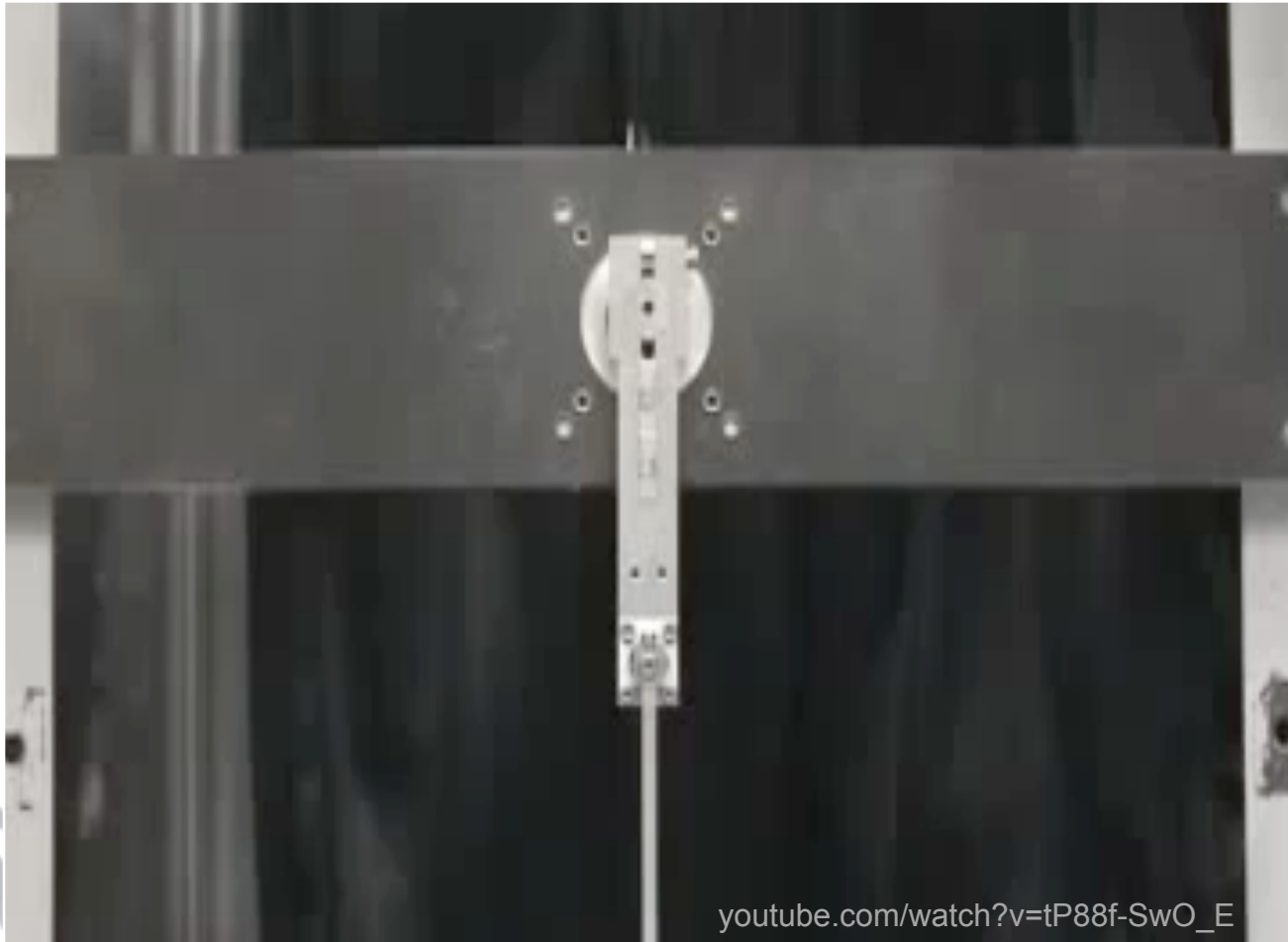
Theoretical description of pump-probe spectroscopy in solids  
*lab.sentef.org*

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Emmy Noether Programme (SE 2558/2-1)

Max Planck Institute for the Structure and Dynamics of Matter

# Driven is different

## Kapitza pendulum

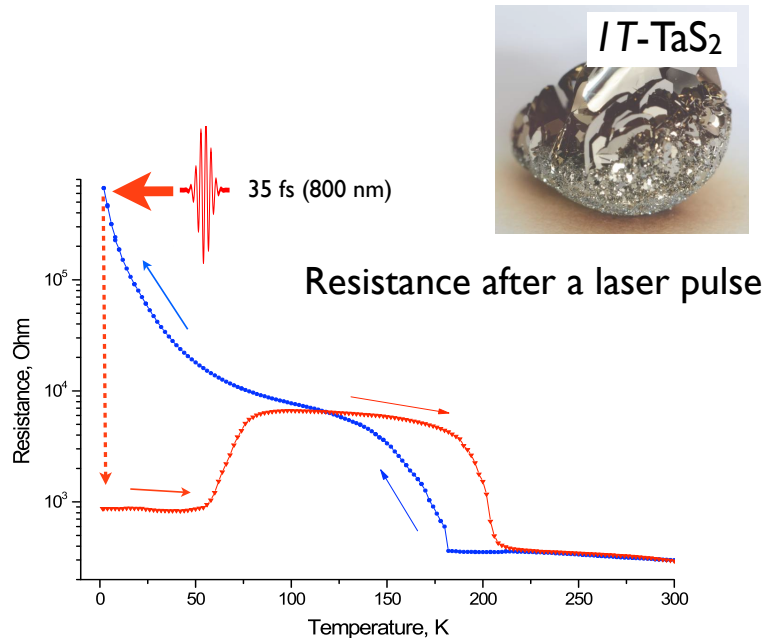


dynamical stabilization of a metastable state



# Is driven also useful?

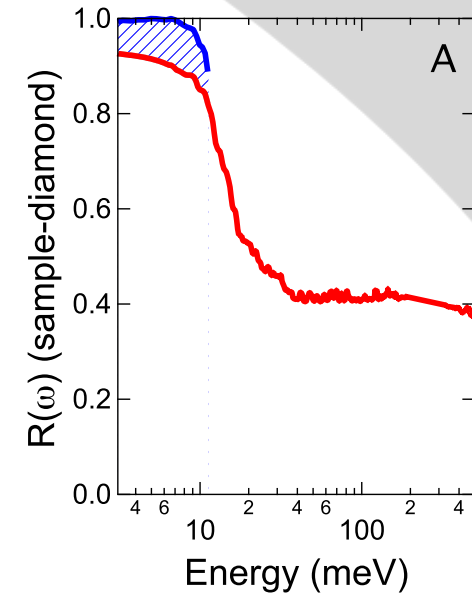
## Exposing hidden states



L Stojchevska et al. Science 2014;344:177-180

... and many more.

## Light-induced new states?



Possible light-induced superconductivity in  $K_3C_{60}$  at high temperature

M. Mitrano, A. Cantaluppi, D. Nicoletti, S. Kaiser, A. Perucchi, S. Lupi, P. Di Pietro, D. Pontiroli, M. Riccò, S. R. Clark, D. Jaksch & A. Cavalleri

Affiliations | Contributions | Corresponding author

Nature 530, 461–464 (25 February 2016) | doi:10.1038/nature16522



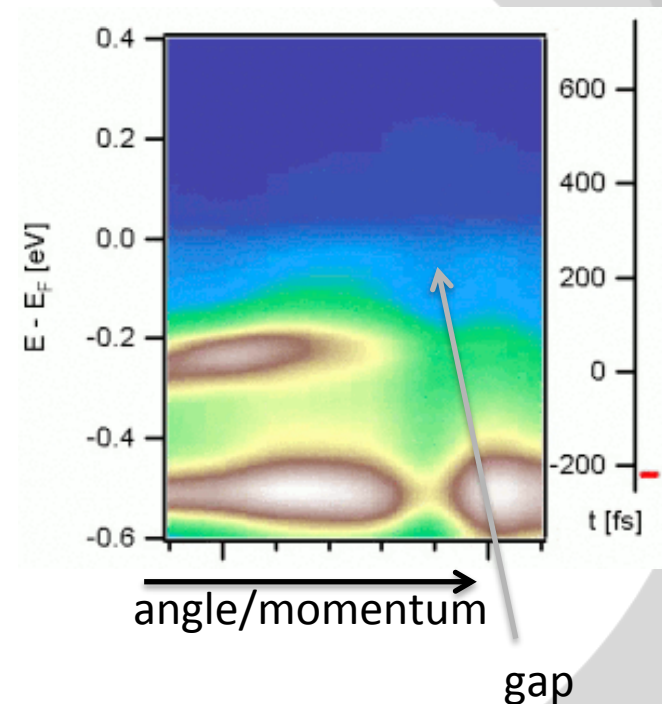
# Pump-probe spectroscopy

- stroboscopic investigations of dynamic phenomena



*Muybridge 1887*

## TbTe<sub>3</sub> CDW metal



*F. Schmitt et al., Science 321, 1649 (2008)  
Image courtesy: J. Sobota / F. Schmitt*

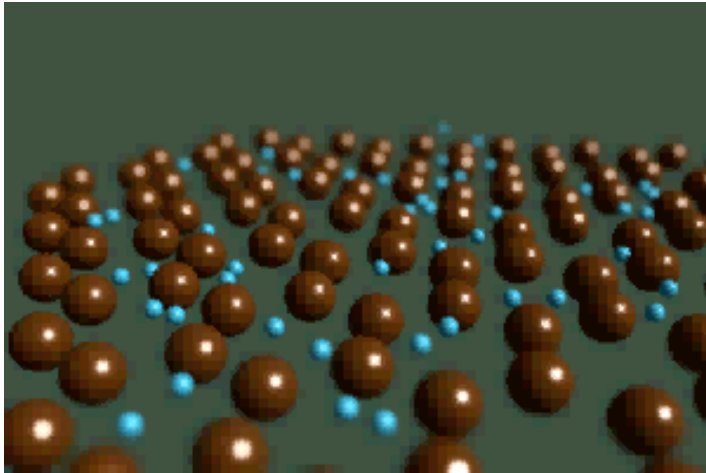
## U.S. Department of Energy “Five Grand Challenges to Science and the Imagination”

- *Grand Challenge #3: How do remarkable properties of matter **emerge** from complex correlations of the atomic or electronic constituents and how can we **control** these properties?*
- *Grand Challenge #5: How do we **characterize** and **control** matter **away** – especially very far away – from **equilibrium**?*

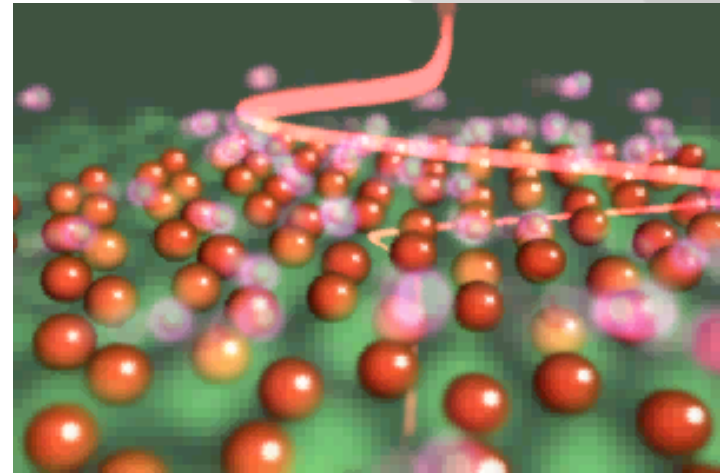
<http://science.energy.gov/bes/efrc/research/grand-challenges/>

# Challenge

movies by Koichiro Tanaka (Kyoto university)



many-body problem  
(electrons + ions)



nonequilibrium many-body problem  
(electrons + ions + photons)

Mission statement:

To **understand** and **predict** electron-ion dynamics and  
**control** of **emergent nonequilibrium** electronic structure

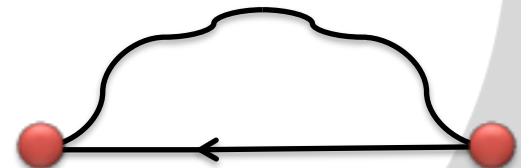


## Main challenges:

- hierarchy of energy and time scales
- high laser intensities: nonperturbative/nonlinear

## Possible approaches:

- first principles (time-dependent density functional theory (TDDFT))
- effective models:
  - Feynman diagrams: self-energy
  - Keldysh nonequilibrium Green's functions
  - connection with DFT: Sham-Schlüter integral equation

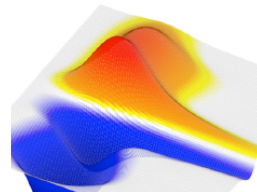


# Ultrafast Materials Science today

## Understanding the nature of quasiparticles

- Relaxation dynamics
- Control of couplings

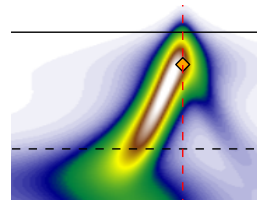
*PRL* 111, 077401 (2013)     *PRB* 95, 024304 (2017)  
*PRX* 3, 041033 (2013)     *PRB* 95, 205111 (2017)  
*PRB* 87, 235139 (2013)     *PRL* 121, 097402 (2018)  
*PRB* 90, 075126 (2014)     *arXiv:1802.09437, Sci. Adv.*  
*Nat. Comm.* 7, 13761 (2016) *arXiv:1808.02389*



## Understanding ordered phases

- Collective oscillations
- Competing orders

*PRB* 92, 224517 (2015)     *arXiv:1806.08187*  
*PRB* 93, 144506 (2016)     *arXiv:1808.00712*  
*PRL* 118, 087002 (2017)     *arXiv:1808.04655*  
   *arXiv:1810.06536*



## Creating new states of matter

- nonequilibrium topological states

*Nature Comm.* 6, 7047 (2015)  
*Nature Comm.* 8, 13940 (2017)  
*Nature Comm.* 9, 4452 (2018)

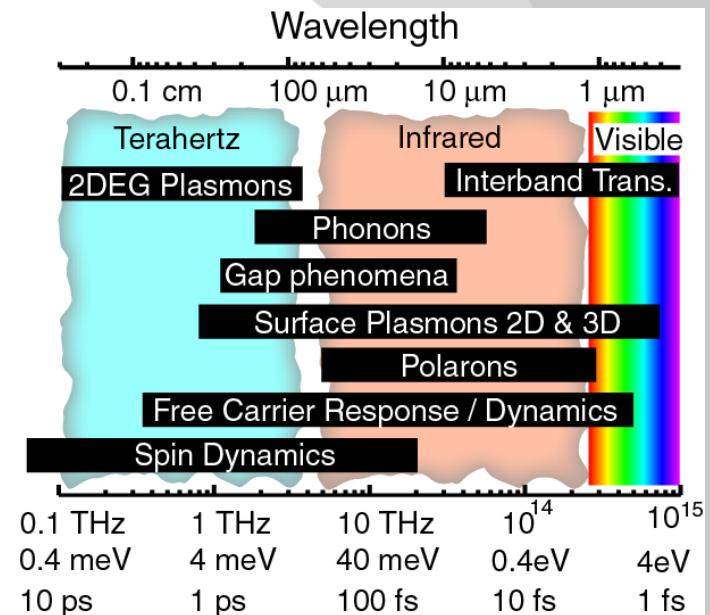
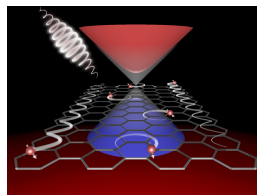
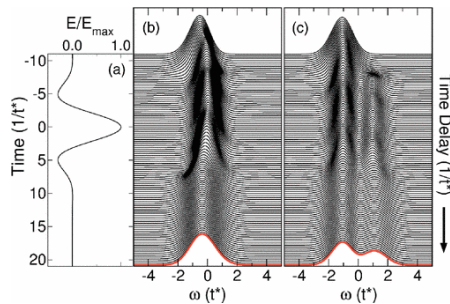
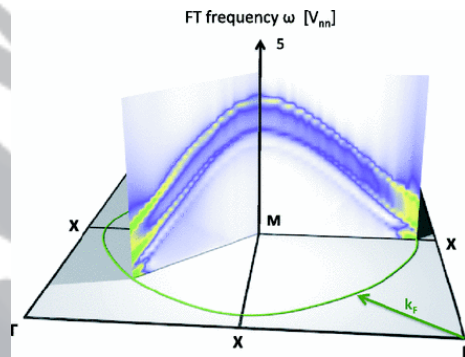


Image courtesy:  
D. Basov

# Relaxation dynamics

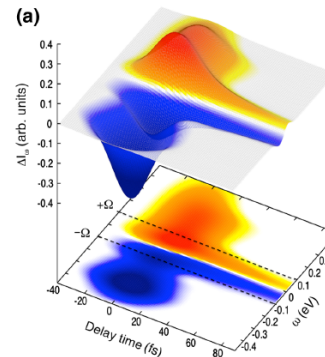


*PRL 111, 077401 (2013)*  
nonthermal  
pumped states

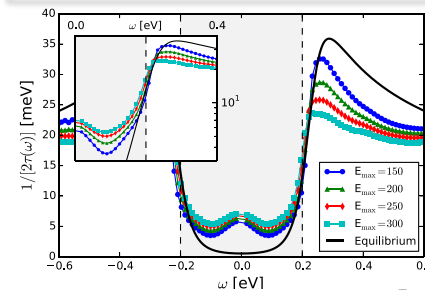


*PRB 87, 235139 (2013)*  
extracting  
unoccupied  
electronic  
structure

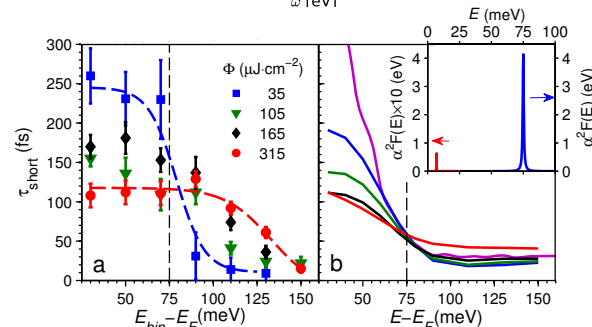
## examining electron-boson coupling



*PRX 3, 041033 (2013)*  
small fluences



*PRB 90, 075126 (2014)*  
fluence  
dependence



*Nat. Comm. 7, 13761 (2016)*  
comparison  
with  
experiment



# Electron-boson coupling

Holstein model (minimal version):

$$H = \sum_k \epsilon(k) c_k^\dagger c_k + \Omega \sum_i b_i^\dagger b_i - g \sum_i c_i^\dagger c_i (b_i + b_i^\dagger)$$

ElectronsBosonsElectron-boson  
(Fermi gas/liquid) (e.g., Einstein phonon) coupling

Pump laser:

$$\epsilon(k) \rightarrow \epsilon(k, t)$$

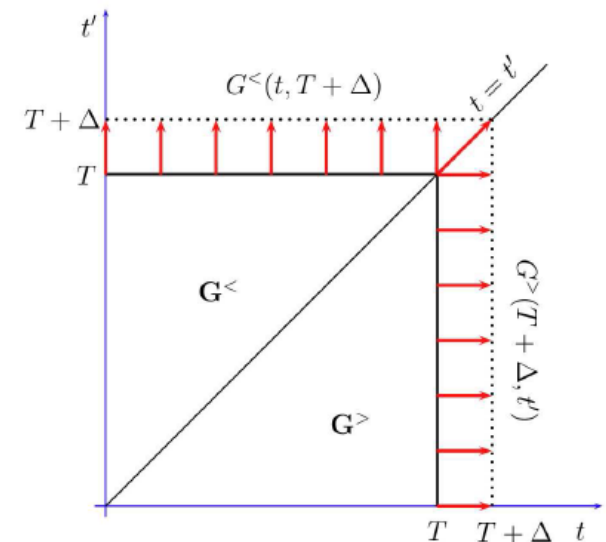
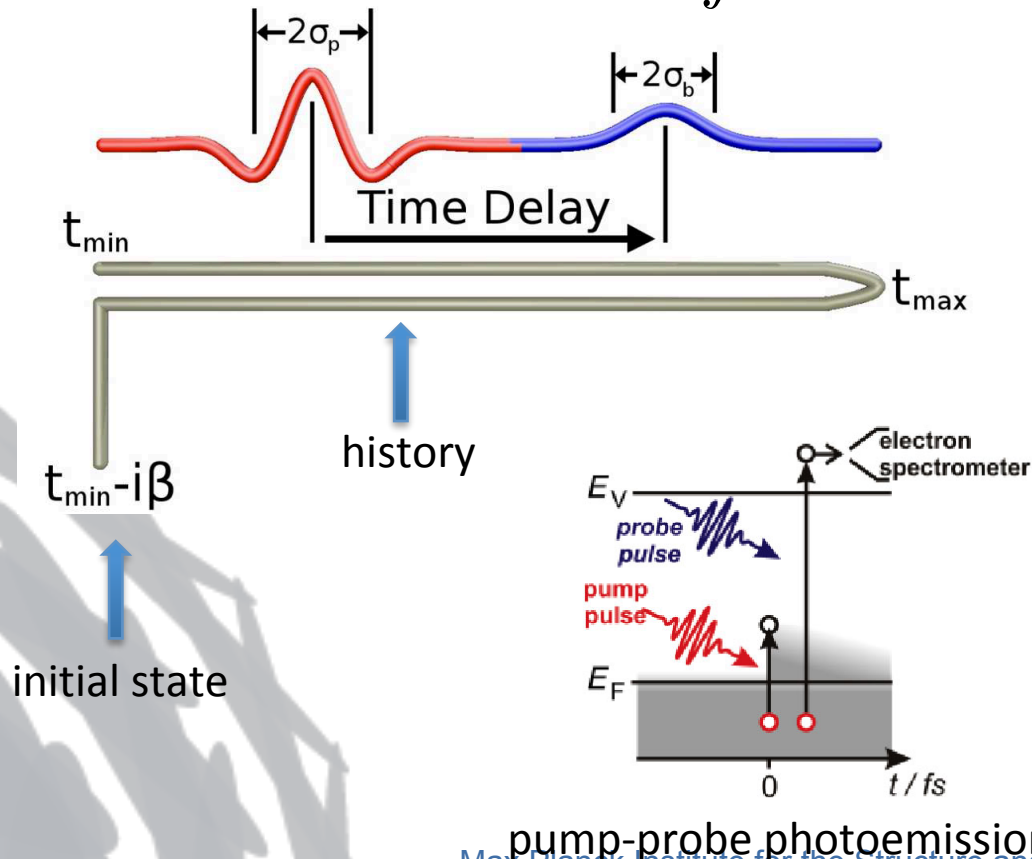
# Method: Keldysh Green functions

$$G_k(\omega) = G_k^0(\omega) + G_k^0(\omega)\Sigma(\omega)G_k(\omega)$$

$$G_{\mathbf{k}}(t, t') = G_{\mathbf{k}}^0(t, t') + \oint dt_1 dt_2 G_{\mathbf{k}}^0(t, t_1) \underline{\Sigma(t_1, t_2)} G_{\mathbf{k}}(t_2, t')$$



self-energy  $\Sigma$ :  
 electron-electron scattering  
 electron-phonon scattering  
 ...



# Electron-boson coupling

PRX 3, 041033 (2013)

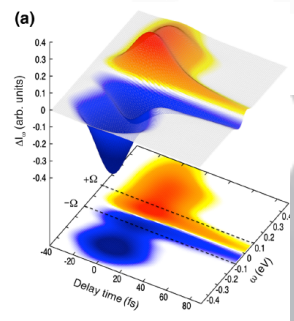
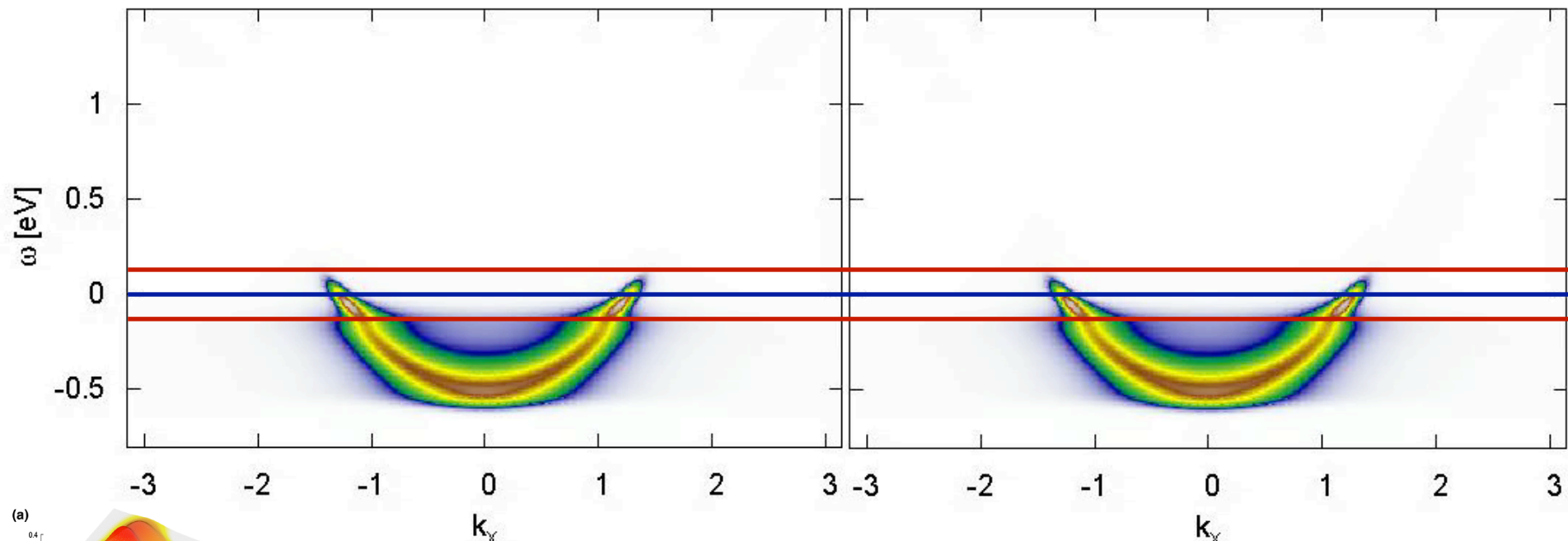
Weak pump

Strong pump

$t = -65.00$

time unit = 0.66 fs

$t = -65.00$

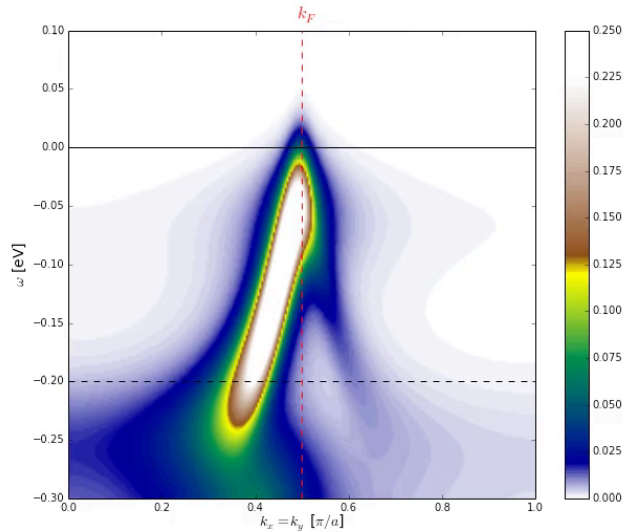


boson window effect for fast versus slow relaxation

nonlinear response for strong pump

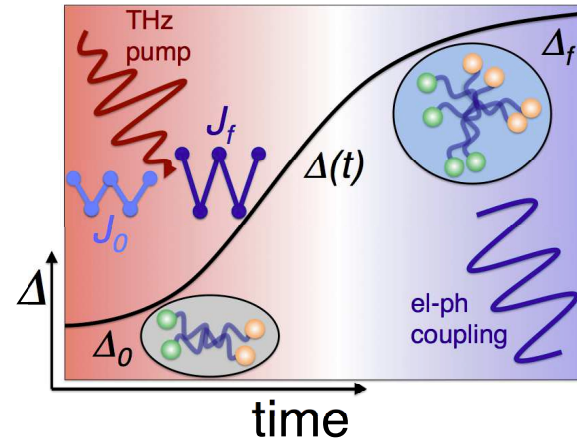


# Ordered phases



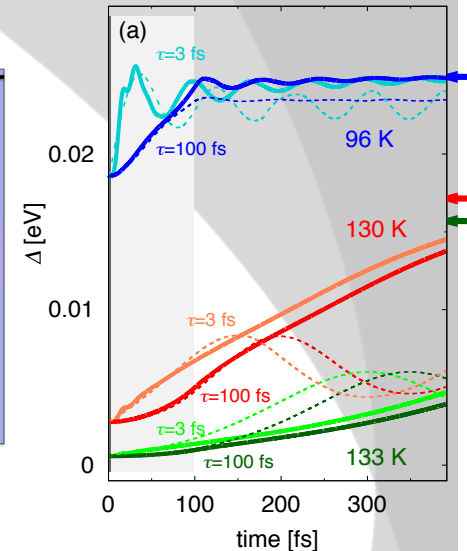
*PRB 92, 224517 (2015)*

**Higgs amplitude mode**  
oscillations in pump-  
probe photoemission  
spectroscopy



*PRB 93, 144506 (2016)*

**Light-enhanced superconductivity:**  
electron-phonon scattering versus  
collective order parameter dynamics



# Some recent key results

## How to engineer materials away from equilibrium?

### Part I: Light-enhanced electron-phonon coupling

Resonant excitation of IR phonon enhances electron-phonon coupling

*E. Pomarico et al., PRB 95, 024304 (2017) – experiment (bilayer graphene)*

*M. A. Sentef, PRB 95, 205111 (2017) – theory*

### Part II: Optical control of chiral superconductors

Short laser pulses allow for switching of Majorana modes

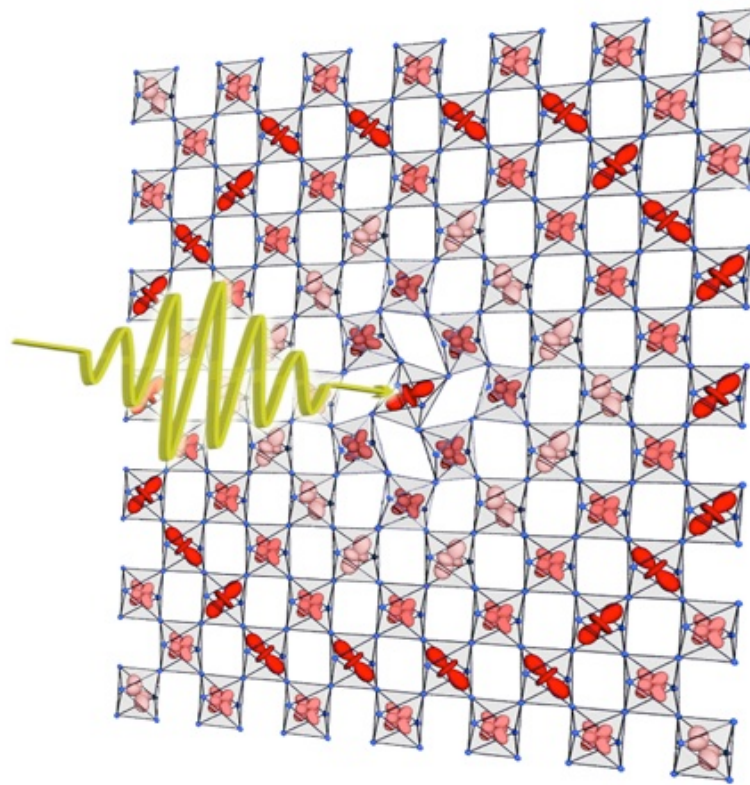
*M. Claassen et al., arXiv:1810.06536*

### Part III: From classical to quantized photon fields

Materials engineering in an optical cavity using vacuum fluctuations

*M. A. Sentef et al., arXiv:1802.09437*

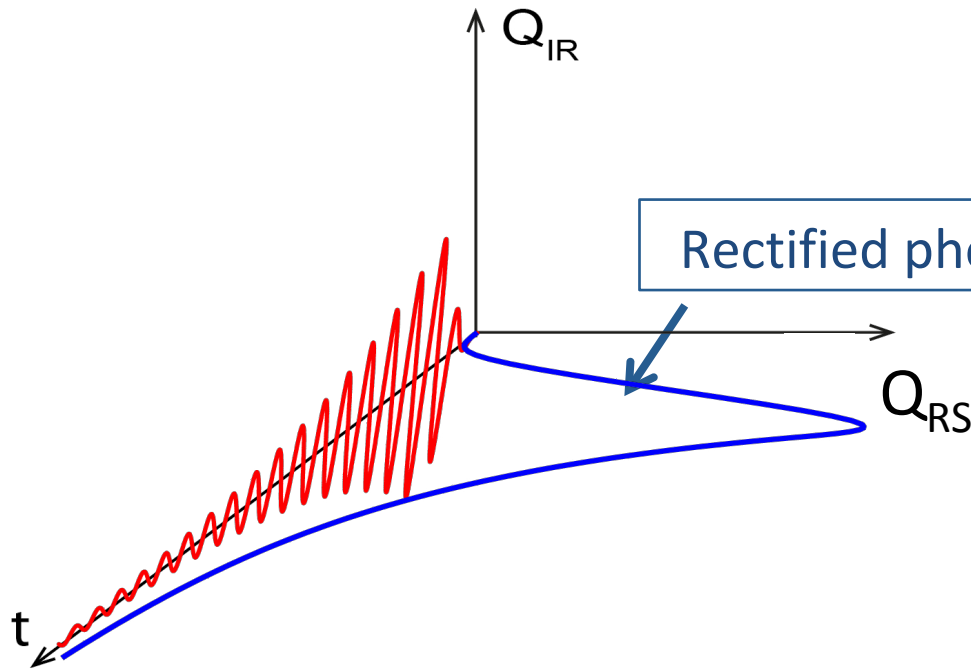
# I Resonant excitation of crystal lattice



*M. Först et al., Nature Physics 7, 854 (2011)*



# Classical nonlinear phononics



Rectified phonon field → directional force

Simplest model: classical dynamics

$$\ddot{Q}_{RS} + \Omega_{RS}^2 Q_{RS} = A Q_{IR}^2$$

$$\ddot{Q}_{IR} + \Omega_{IR}^2 Q_{IR} = \frac{e^* E_0}{\sqrt{M_{IR}}} \sin(\Omega_{IR} t) F(t)$$

„nonlinear phononics“

$$H = A Q_{IR}^2 Q_{RS}$$

*M. Först et al., Nature Physics 7, 854 (2011)*

Explains a number of observed effects, e.g.,

- structurally induced metal-insulator transitions

Rini et al., *Nature* 449, 72 (2007)

- phononic rectification in YBCO

Mankowsky et al., *Nature* 516, 71 (2014)

- ferroelectric switching in  $\text{LiNbO}_3$

Subedi et al., *Phys. Rev. B* 89, 220301 (2014)

Mankowsky et al., *Phys. Rev. Lett.* 118, 197601 (2017)

Classical phonon dynamics **does not** explain all effects in IR-driven materials.

examples: - light-induced superconductivity  
- light-enhanced el-ph coupling

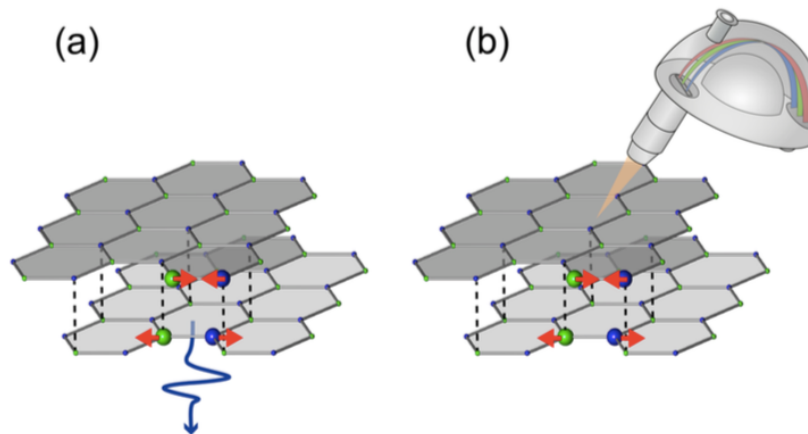
... quantum nature of phonons important?

## Enhanced electron-phonon coupling in graphene with periodically distorted lattice

E. Pomarico, M. Mitrano, H. Bromberger, M. A. Sentef, A. Al-Temimy, C. Coletti, A. Stöhr, S. Link, U. Starke, C. Cacho, R. Chapman, E. Springate, A. Cavalleri, and I. Gierz  
Phys. Rev. B **95**, 024304 – Published 13 January 2017

*PRB 95, 024304 (2017)*

enhanced electron-phonon coupling for pump on resonance  
with IR phonon

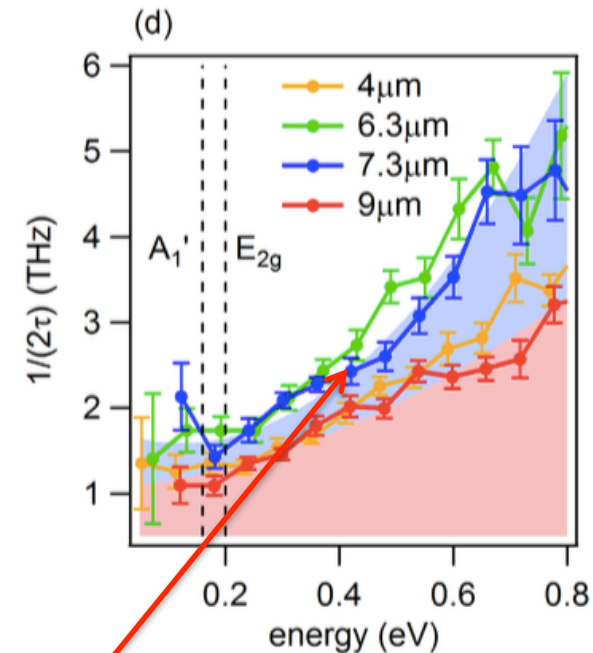
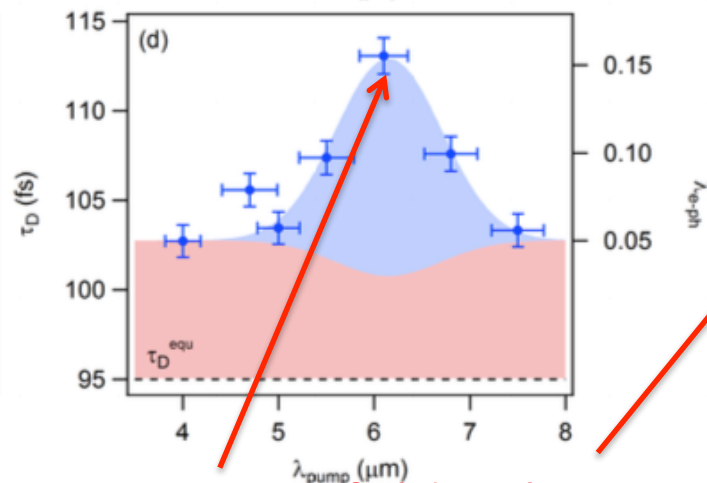
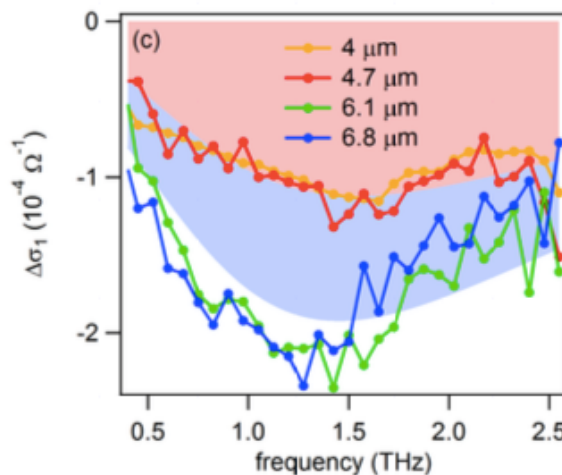
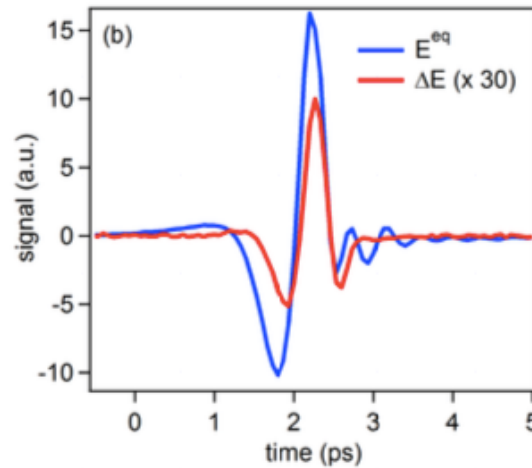
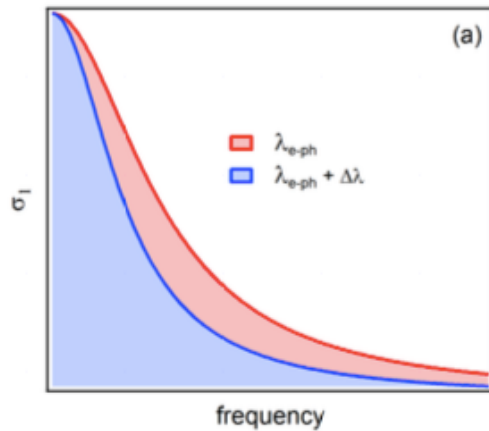


# Dynamically enhanced coupling

PRB 95, 024304 (2017)

transient reduction of THz Drude weight

accelerated tr-ARPES relaxation



driving on phonon resonance: 3-fold enhancement of effective  $\lambda_{e-ph}$

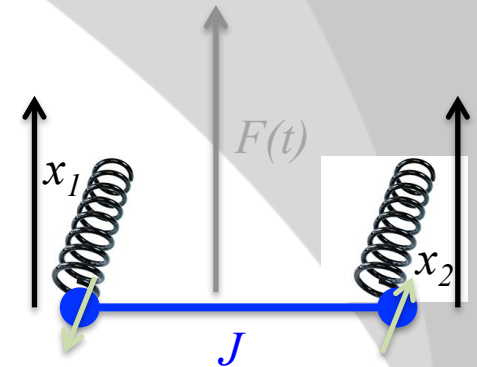
# Quantum nonlinear phononics

PRB 95, 205111 (2017)

also cf. Kennes et al., Nat. Physics 13, 479 (2017)

2-site toy model, solve dynamics exactly

$$\begin{aligned}\hat{H}(t) = & -J \sum_{\sigma} (c_{1,\sigma}^{\dagger} c_{2,\sigma} + c_{2,\sigma}^{\dagger} c_{1,\sigma}) \\ & + g_2 \sum_{\sigma, l=1,2} \hat{n}_{l,\sigma} \underbrace{(b_l + b_l^{\dagger})}_{x_l} \quad \text{density-dependent squeezing of phonon} \\ & + \Omega \sum_{l=1,2} b_l^{\dagger} b_l + F(t) \sum_{l=1,2} (b_l + b_l^{\dagger}),\end{aligned}$$



Idea: Drive **nonlinearly coupled IR-phonon**, analyze electronic response

Drive:  $F(t) = F \sin(\omega t),$

Response:  $I(\omega, t_0) = \text{Re} \int dt_1 dt_2 e^{i\omega(t_1 - t_2)} s_{t_1, t_2, \tau}(t_0)$

time-resolved spectral function  $\times \left[ \langle \psi(t_2) | c_{1,\uparrow}^{\dagger} \mathcal{T} e^{-i \int_{t_1}^{t_2} H(t) dt} c_{1,\uparrow} | \psi(t_1) \rangle + \right.$   
 $\left. + \langle \psi(t_1) | c_{1,\uparrow} \mathcal{T} e^{-i \int_{t_2}^{t_1} H(t) dt} c_{1,\uparrow}^{\dagger} | \psi(t_2) \rangle \right],$

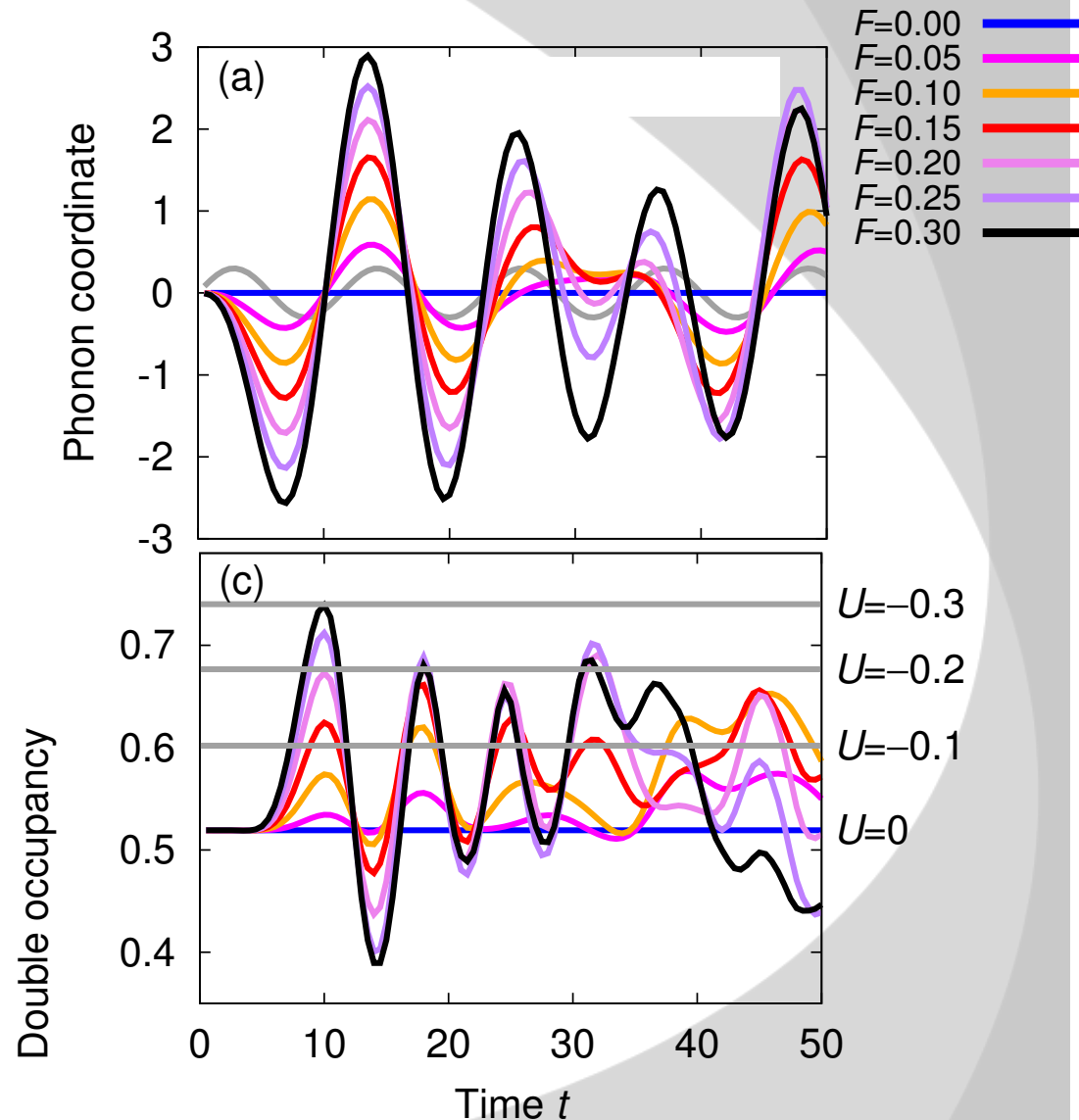


# IR-driven nonlinear el-ph system

Driving IR phonon with  
sinusoidal  $F(t)$ :  
coherent phonon oscillation

enhancement of local  
electronic double  
occupancy

-> induced el-el attraction

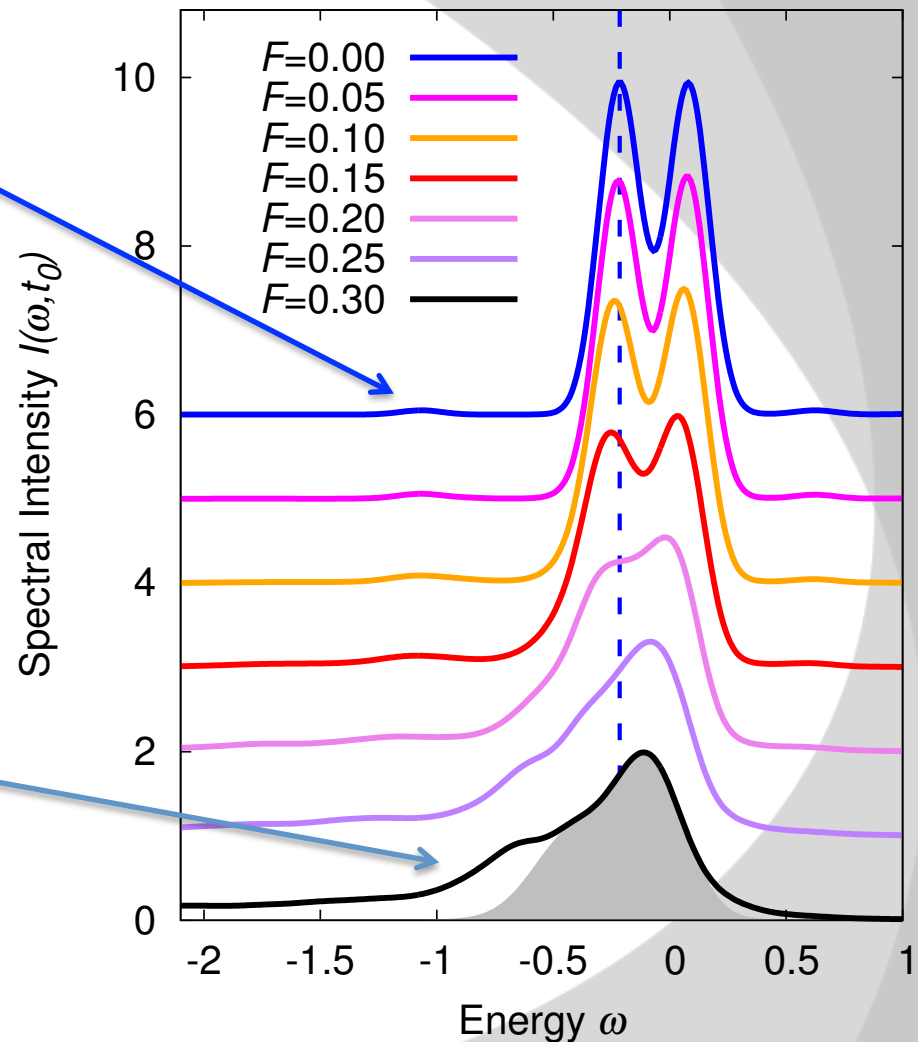


2-phonon shakeoff

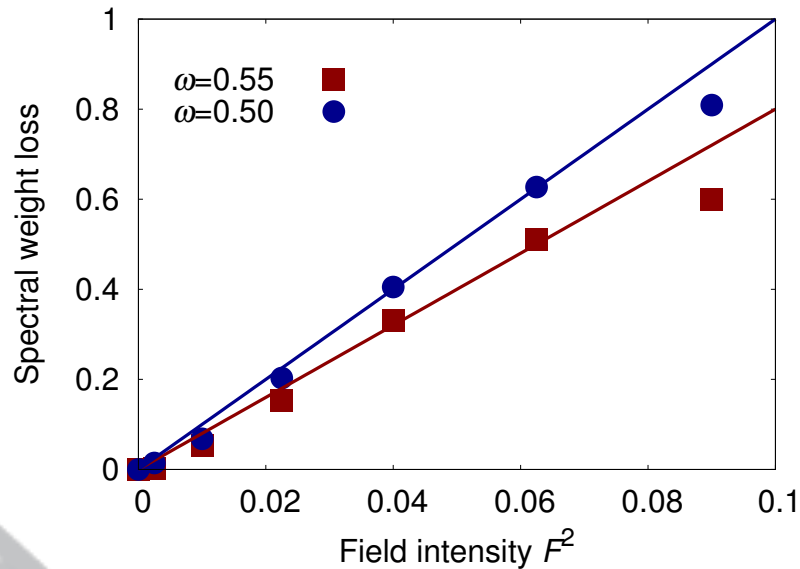
Reduced coherence peaks  
with stronger driving

light-enhanced el-ph  
coupling

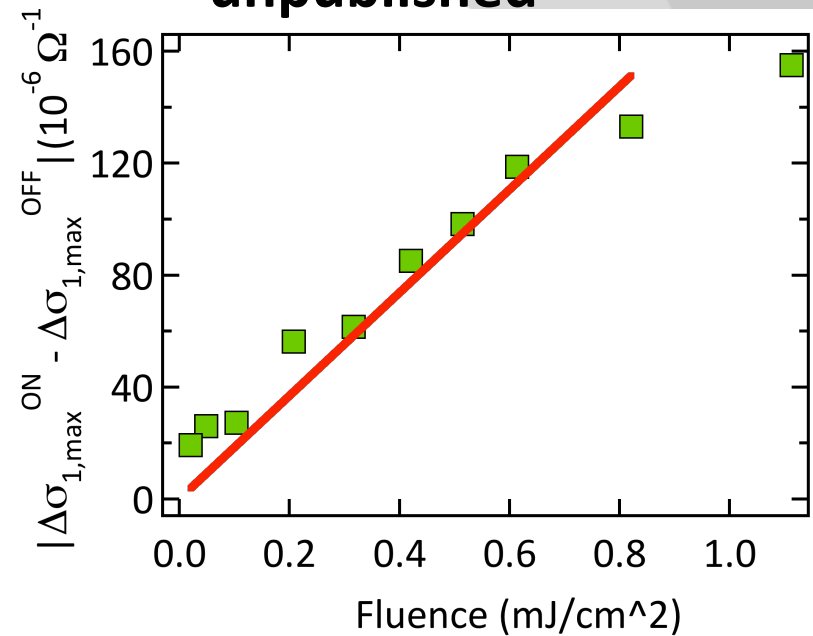
light-induced polaron formation



## Theory



## Data by E. Pomarico, unpublished



Coherence peak weight loss: proportional to field intensity  $F^2$  **consistent with experiments**

# Summary I

- enhanced electron-phonon coupling in phononically driven bilayer graphene

*PRB 95, 024304 (2017)*



E. Pomarico



I. Gierz



A. Cavalleri

Exact solution of electron-phonon model system:

- theoretical proposal: nonlinear el-ph coupling as mechanism behind this enhancement

*PRB 95, 205111 (2017)*

# II Optical control of Majoranas

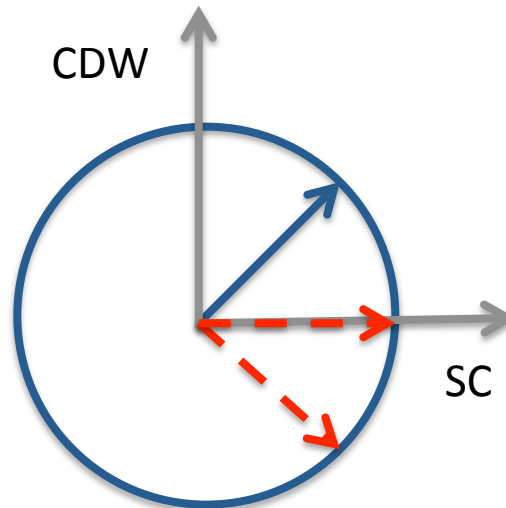
- prior work: optical control of competing orders

Theory of Laser-Controlled Competing Superconducting and Charge Orders

M. A. Sentef, A. Tokuno, A. Georges, and C. Kollath

Phys. Rev. Lett. **118**, 087002 – Published 21 February 2017

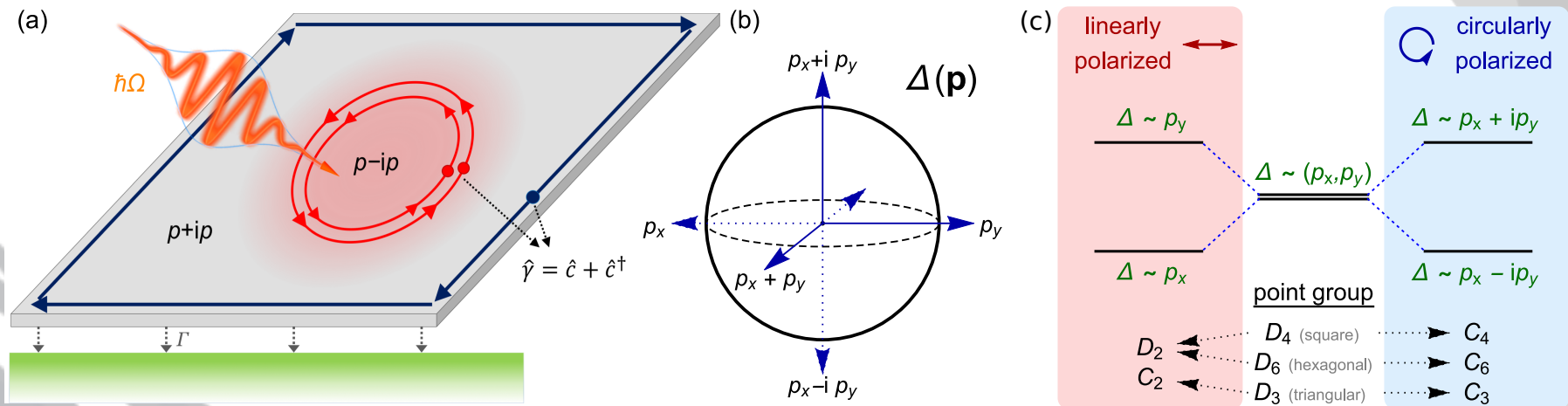
- selective laser driving **switches** between phases





# II Optical control of Majoranas

- can one switch the chirality of a 2D topological superconductor?



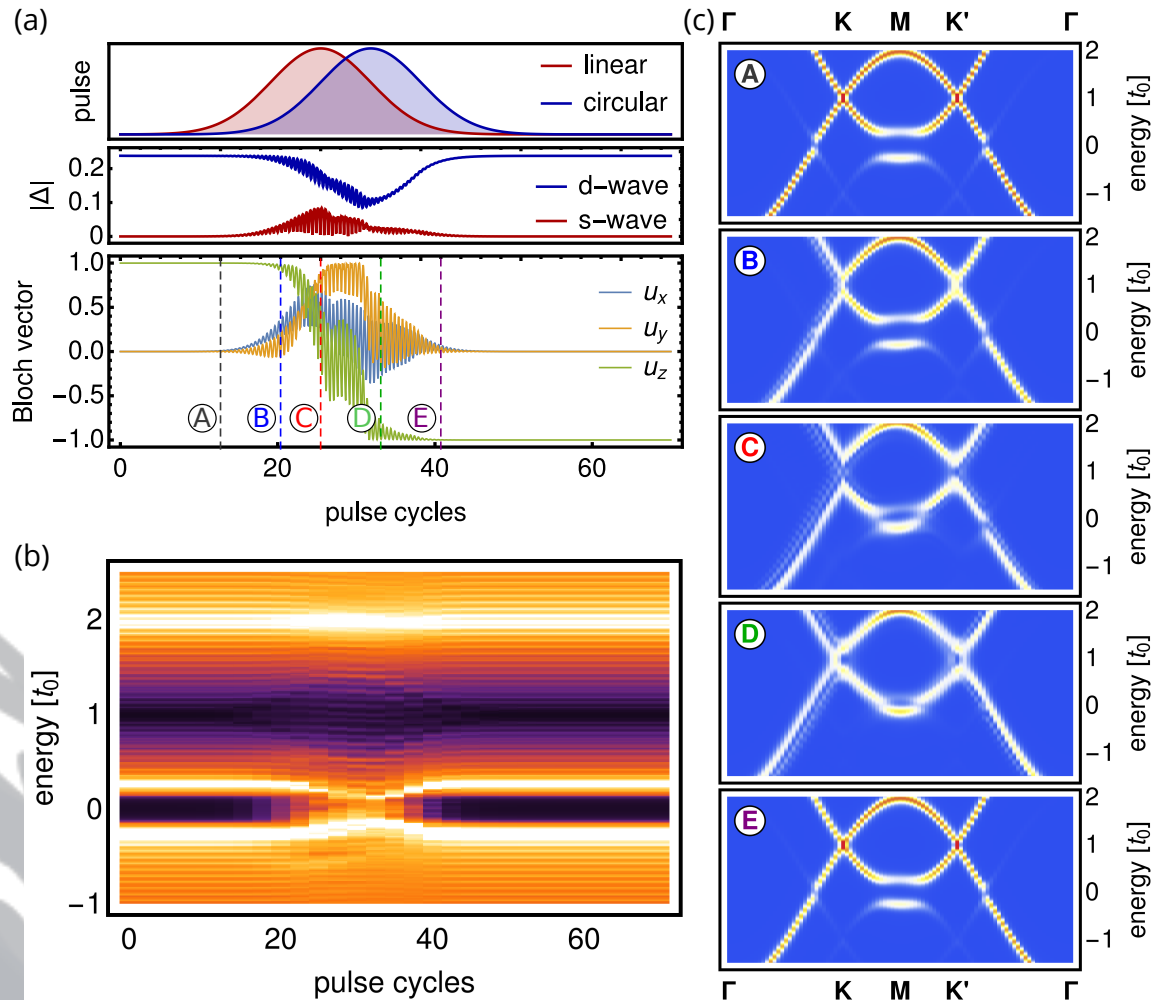
key idea: use two-pulse sequence with linearly and circularly polarized light

multiband Bogoliubov-de-Gennes Hamiltonians for **doped graphene** (d+id) and **Sr2RuO4** (p+ip)  
coupling to fermionic reservoir to dissipate energy  
laser driving via Peierls substitution

Keldysh equations of motion for Nambu Green's functions:

$$i\partial_t \mathcal{G}_{\mathbf{k}}(t, t') = \mathcal{H}_{\mathbf{k}}(t, \Delta_{\mathbf{k}}(t)) \mathcal{G}_{\mathbf{k}}(t, t') + \int d\tau \hat{\Sigma}_{\mathbf{k}}(t, \tau) \mathcal{G}_{\mathbf{k}}(\tau, t')$$
$$\Delta_{\mathbf{k}}(t) = \frac{1}{L} \sum_j v^{(j)} \hat{\eta}_{\mathbf{k}}^{(j)} \sum_{\substack{\mathbf{k}' \\ \alpha\beta}} \hat{\eta}_{\mathbf{k}'\alpha\beta}^{(j)} \left\langle \hat{c}_{-\mathbf{k}',\beta\downarrow} \hat{c}_{\mathbf{k}',\alpha\uparrow} \right\rangle$$

# Optical control of Majoranas



two-pulse sequence  
reverses d+id state  
in graphene

time-resolved  
spectroscopy tracks  
chirality reversal

# Summary II

- All-optical **control of chiral Majorana modes**
- towards arbitrarily programmable quantum computer?

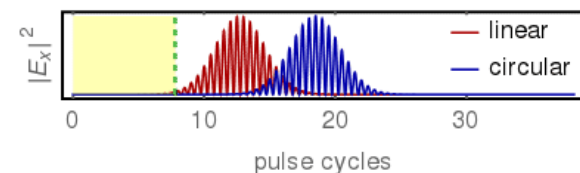
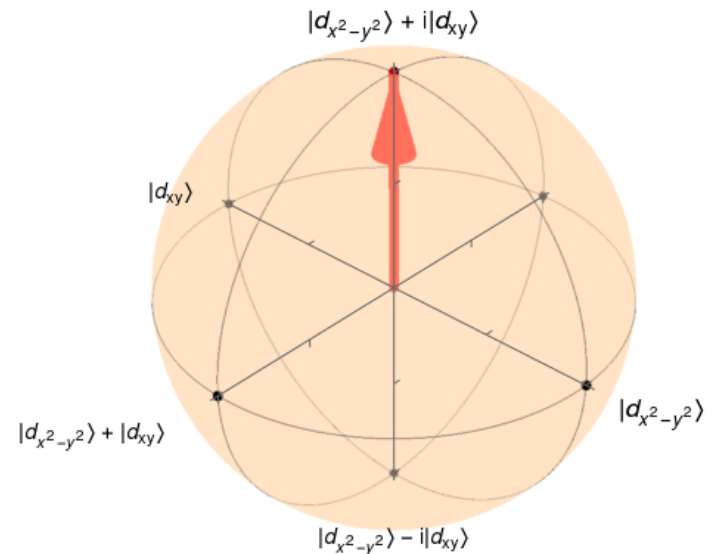
*M. Claassen et al., arXiv:1810.06536,  
submitted to Nat. Phys.*



M. Claassen

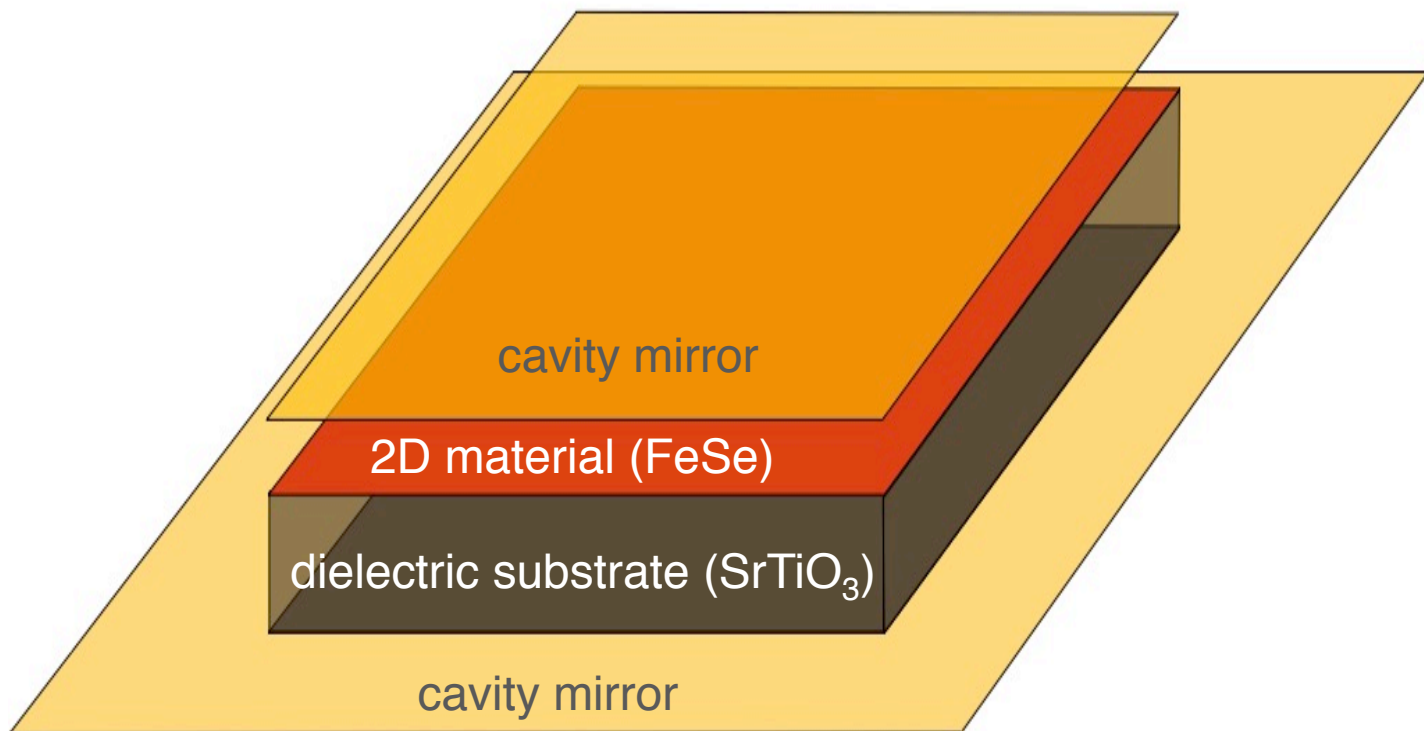


D. Kennes



# III Cavity materials

- can one use enhanced vacuum fluctuations to change materials properties?





*BCS superconductors: **phonon**-mediated superconductivity*

*Ginzburg, Phys. Lett. 13, 101 (1964): **exciton**-mediated superconductivity?*

*Ruvalds, Phys. Rev. B 35, 8869(R) (1987): **plasmon**-mediated superconductivity?*

PRL **104**, 106402 (2010) PHYSICAL REVIEW LETTERS week ending 12 MARCH 2010

## Exciton-Polariton Mediated Superconductivity

Fabrice P. Laussy,<sup>1</sup> Alexey V. Kavokin,<sup>1,2</sup> and Ivan A. Shelykh<sup>3,4</sup>

**Cavity-assisted mesoscopic transport of fermions:  
Coherent and dissipative dynamics.**

*Hagenmüller et al., 1801.09876*

## Cavity-mediated electron-photon superconductivity

Frank Schlawin<sup>1</sup>, Andrea Cavalleri<sup>1,2</sup> and Dieter Jaksch<sup>1</sup>

**1804.07142**

## Cavity Quantum Eliashberg Enhancement of Superconductivity

Jonathan B. Curtis,<sup>1,2,\*</sup> Zachary M. Raines,<sup>1,2</sup> Andrew A. Allocca,<sup>1,2</sup> Mohammad Hafezi,<sup>1</sup> and Victor M. Galitski<sup>1,2</sup>

**1805.01482**

## Manipulating quantum materials with quantum light

Martin Kiffner<sup>1,2</sup>, Jonathan Coulthard<sup>2</sup>, Frank Schlawin<sup>2</sup>, Arzhang Ardavan<sup>2</sup>, and Dieter Jaksch<sup>2,1</sup>

**1806.06752**

## Cavity superconductor-polaritons **1807.06601**

Andrew A. Allocca,<sup>\*</sup> Zachary M. Raines, Jonathan B. Curtis, and Victor M. Galitski

PHYSICAL REVIEW B **93**, 054510 (2016)

## Superconductivity and other collective phenomena in a hybrid Bose-Fermi mixture formed by a polariton condensate and an electron system in two dimensions

Ovidiu Cotel, <sup>1,\*</sup> Sina Zeytinoglu, <sup>1,2</sup> Manfred Sigrist, <sup>2</sup> Eugene Demler, <sup>3</sup> and Ata Imamoglu <sup>1</sup>

Cavity quantum-electrodynamical polaritonically enhanced  
electron-phonon coupling and its influence on superconductivity

M. A. Sentef,<sup>1,\*</sup> M. Ruggenthaler,<sup>1</sup> and A. Rubio<sup>1,2,3</sup>

**1802.09437**

## Superradiant Quantum Materials

Giacomo Mazza<sup>1,2,\*</sup> and Antoine Georges<sup>2,3,1,4</sup>

**1804.08534**

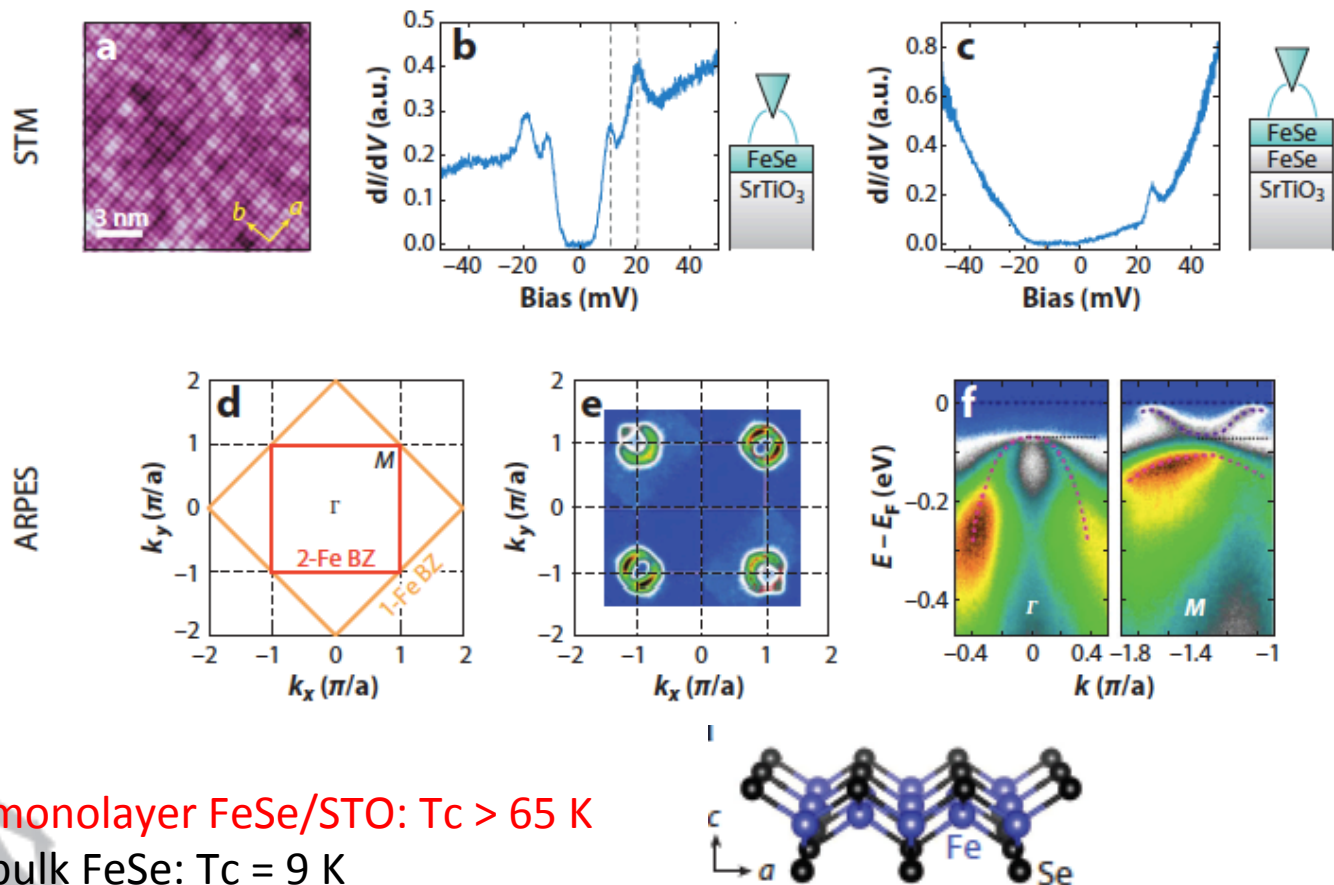
## Ab-initio Exciton-polaritons:

Cavity control of Dark Excitons in two dimensional Materials

Simone Latini,<sup>1,\*</sup> Enrico Ronca,<sup>1,†</sup> Umberto De Giovannini,<sup>1,2,‡</sup> Hannes Hübener,<sup>1,§</sup> and Angel Rubio<sup>1,3,¶</sup>

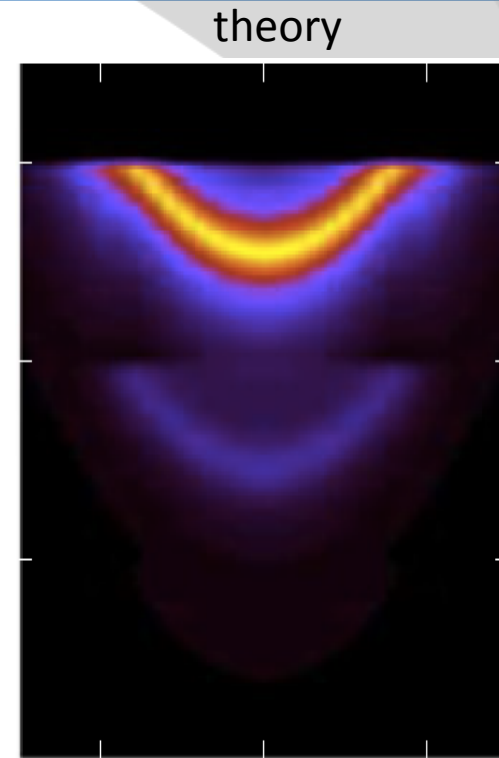
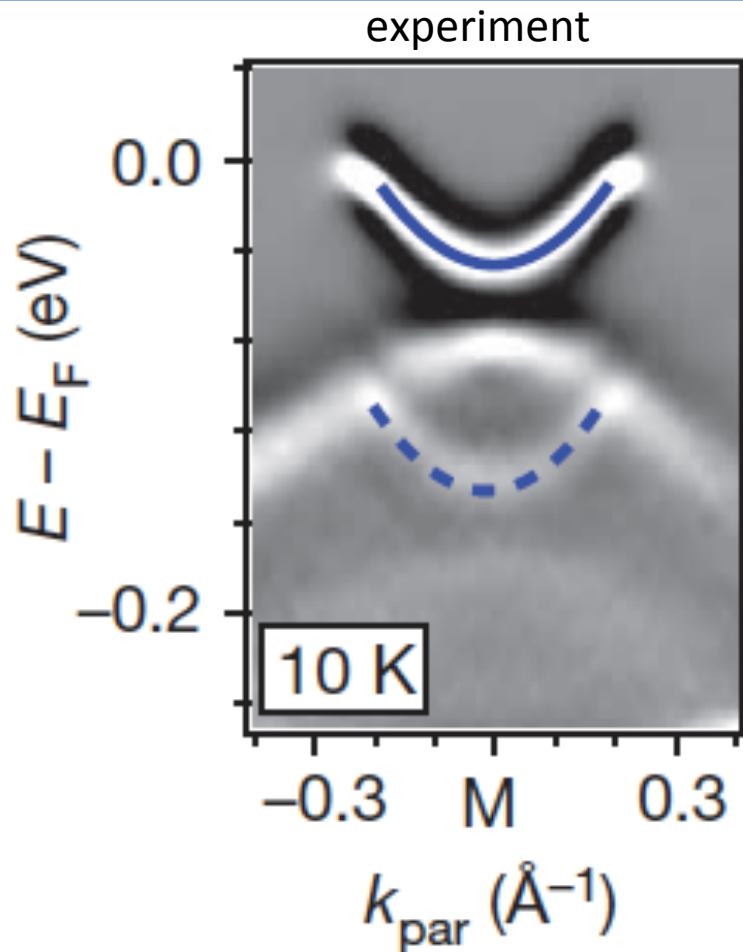
**1810.02672**

# monolayer FeSe/STO



Wang QY, Li Z, Zhang WH, Zhang ZC, Zhang JS, et al. 2012. *Chin. Phys. Lett.* 29:037402  
 Liu D, Zhang W, Mou D, He J, Ou YB, et al. 2012. *Nat. Commun.* 3:931  
 Huang and Hoffman, *Annu. Rev. CMP* 8, 311 (2017)

# monolayer FeSe/STO: ARPES



replica bands: forward (small- $q$ )  
electron-phonon scattering

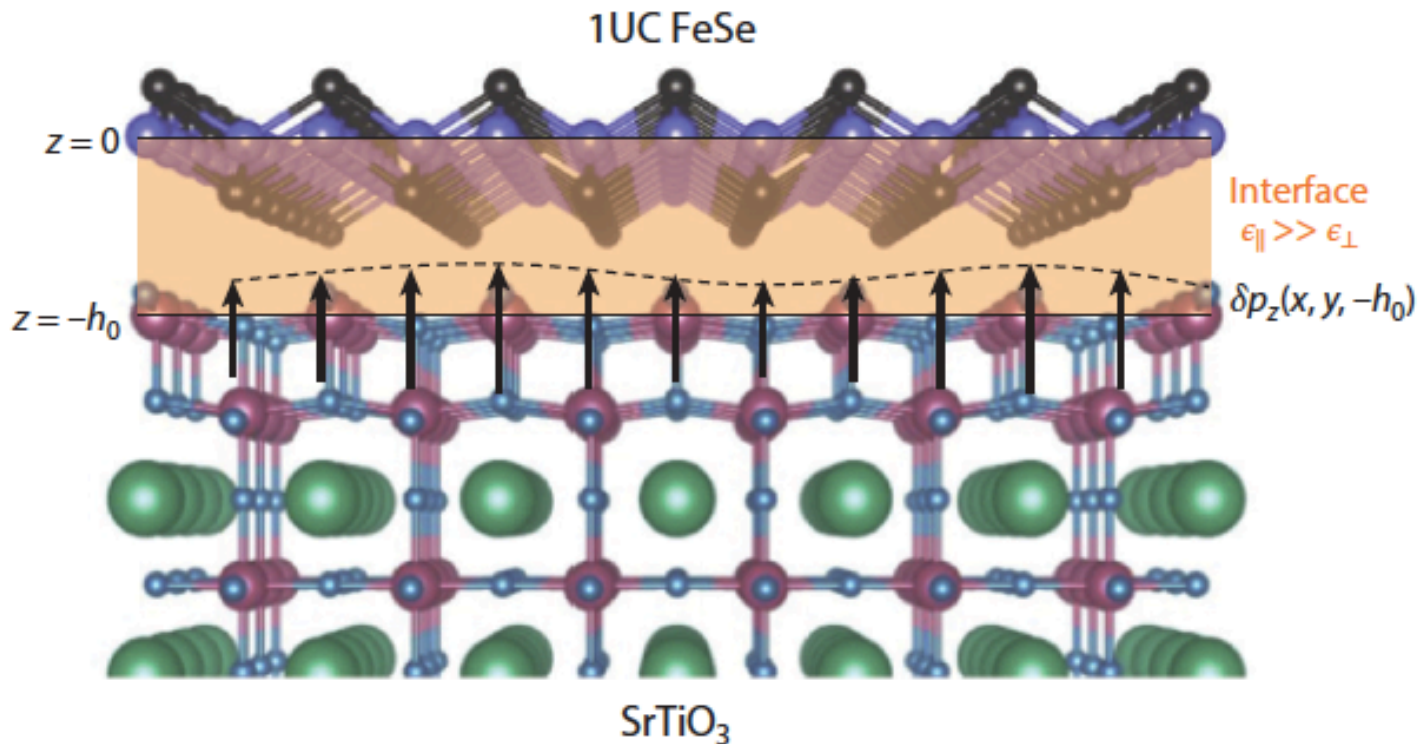
*Lee et al., Nature 515, 245 (2014)*

*Rademaker et al., New J. Phys. 18, 022001 (2016)*

# monolayer FeSe/STO: interfacial phonon

bare el-phonon vertex  $g(\vec{q}) = g_0 \exp(-|\vec{q}|/q_0)$  *Lee et al., Nature 515, 245 (2014)*

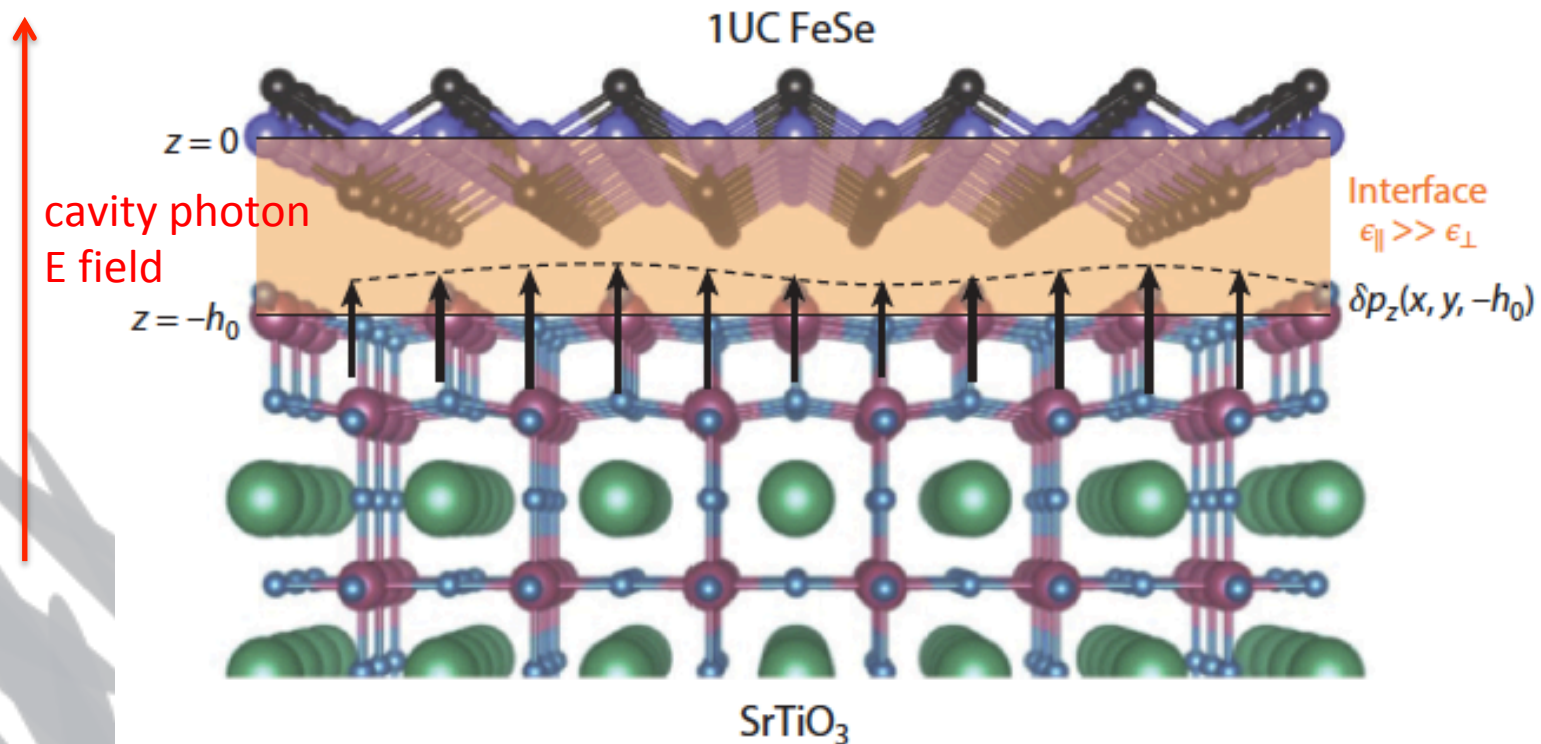
$$q_0^{-1} = h_0 \sqrt{\epsilon_{\parallel}/\epsilon_{\perp}} \quad \epsilon_{\parallel}/\epsilon_{\perp} \approx 100$$



*Huang and Hoffman, Annu. Rev. CMP 8, 311 (2017)*

# Cavity engineering

- idea: use **phonon polaritons** to enhance electron-phonon coupling



*Huang and Hoffman, Annu. Rev. CMP 8, 311 (2017)*



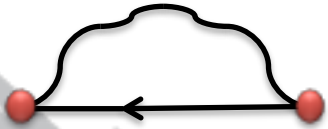
$$H = \sum_{\vec{k}, \sigma} \epsilon_{\vec{k}} c_{\vec{k}, \sigma}^{\dagger} c_{\vec{k}, \sigma} + \frac{1}{\sqrt{N}} \sum_{\vec{k}, \vec{q}, \sigma, \lambda = \pm} c_{\vec{k} + \vec{q}, \sigma}^{\dagger} c_{\vec{k}, \sigma} (g_{\lambda}^{*}(\vec{q}) \alpha_{-\vec{q}, \lambda}^{\dagger} + g_{\lambda}(\vec{q}) \alpha_{\vec{q}, \lambda}) + \sum_{\vec{q}, \lambda = \pm} \omega_{\lambda}(\vec{q}) \alpha_{\vec{q}, \lambda}^{\dagger} \alpha_{\vec{q}, \lambda}$$

electrons
el-polariton coupling
polaritons

bare el-phonon vertex  $g(\vec{q}) = g_0 \exp(-|\vec{q}|/q_0) \quad q_0^{-1} = h_0 \sqrt{\epsilon_{\parallel}/\epsilon_{\perp}}$

G-self-consistent Migdal-Eliashberg diagram

$$\hat{\Sigma}(\vec{k}, i\omega_n) = \frac{-1}{N\beta} \sum_{\vec{q}, m, \lambda = \pm} |g_{\lambda}(\vec{q})|^2 D_{\lambda}^{(0)}(\vec{q}, i\omega_n - i\omega_m) \hat{\tau}_3 \hat{G}(\vec{k} + \vec{q}, i\omega_m) \hat{\tau}_3$$

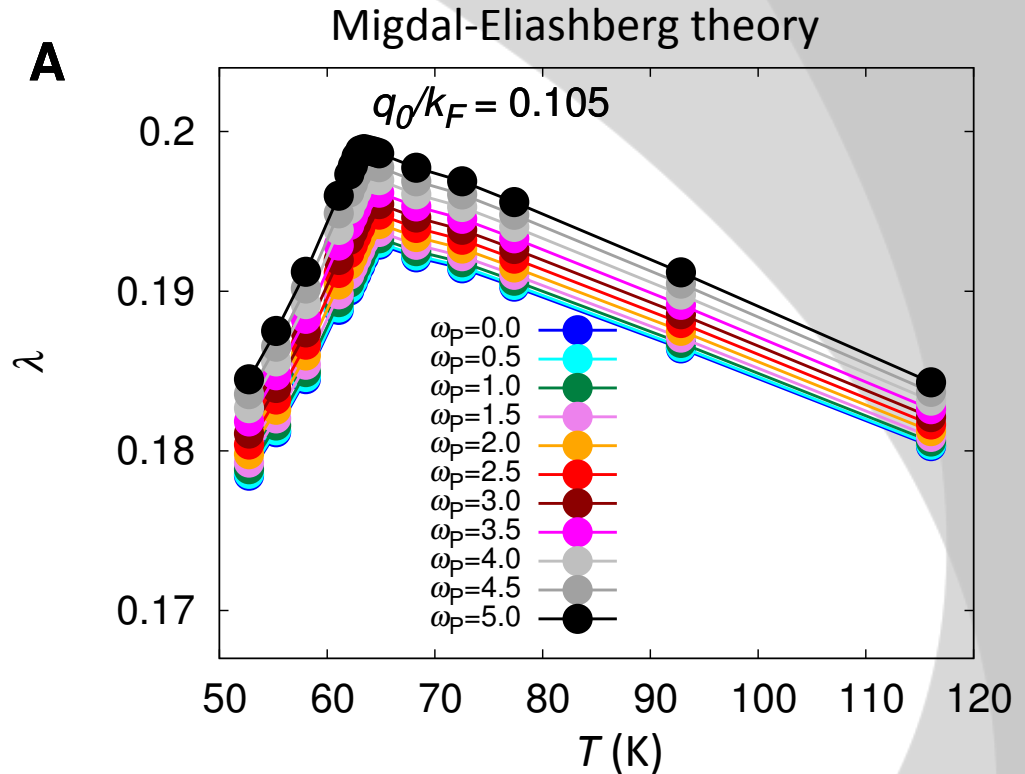
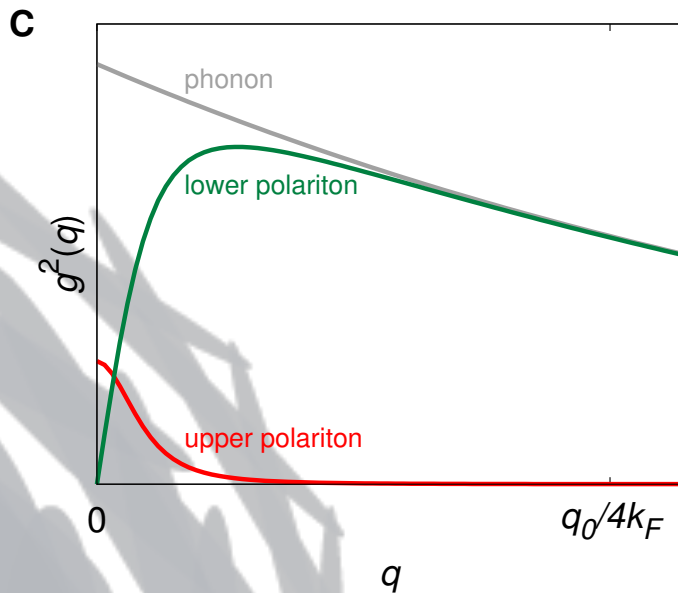
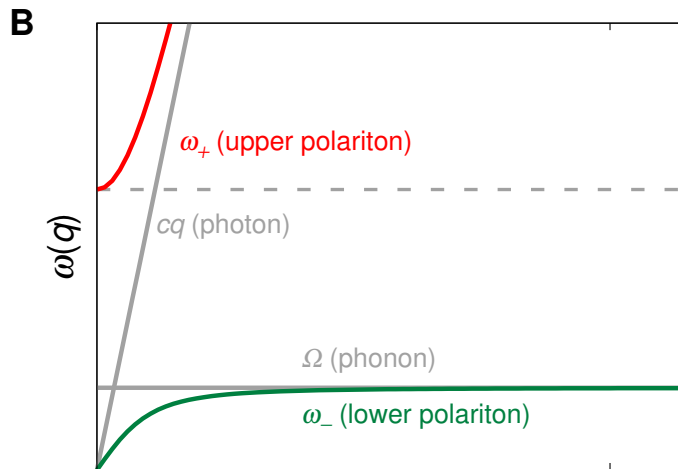


$$\hat{\Sigma}(\vec{k}, i\omega_n) = i\omega_n [1 - Z(\vec{k}, i\omega_n)] \hat{\tau}_0 + \chi(\vec{k}, i\omega_n) \hat{\tau}_3 + \phi(\vec{k}, i\omega_n) \hat{\tau}_1$$

$$\lambda \equiv Z(\vec{k}_F, i\pi/\beta) - 1$$

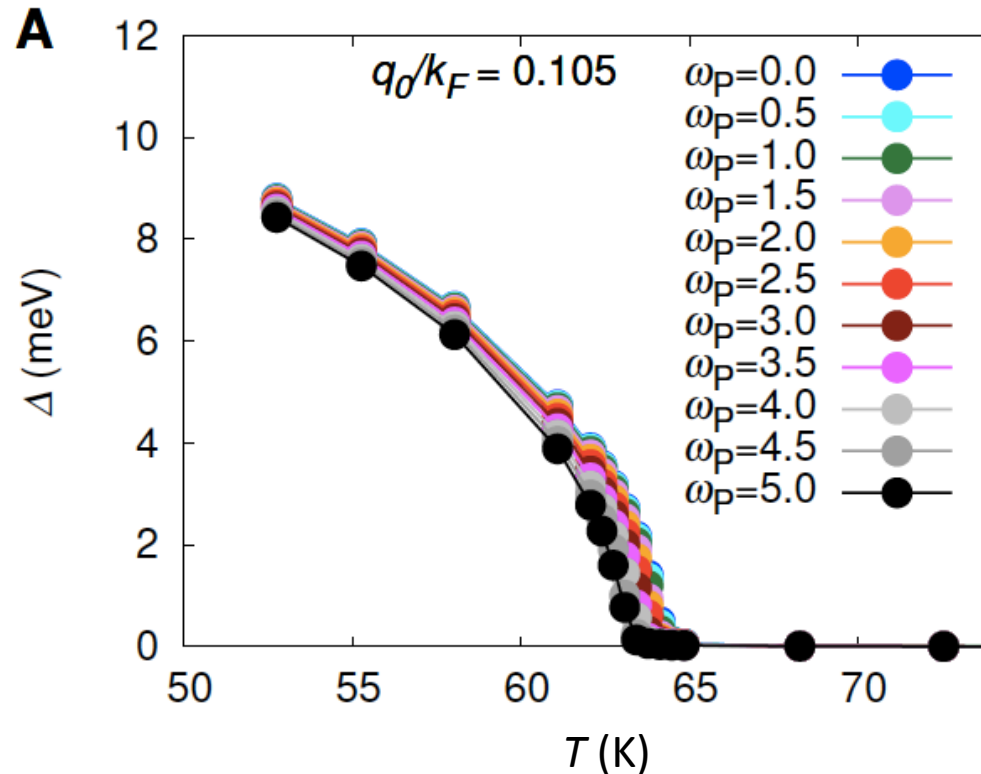
Mass enhancement:  $m^*/m = 1 + \lambda$

# Cavity materials: Phonon polaritons



enhanced electron-phonon coupling,  
controlled by cavity volume

# Superconductivity



suppressed superconductivity despite enhanced el-ph coupling

forward scattering

$$T_C \approx \frac{\lambda\Omega}{2 + 3\lambda}$$

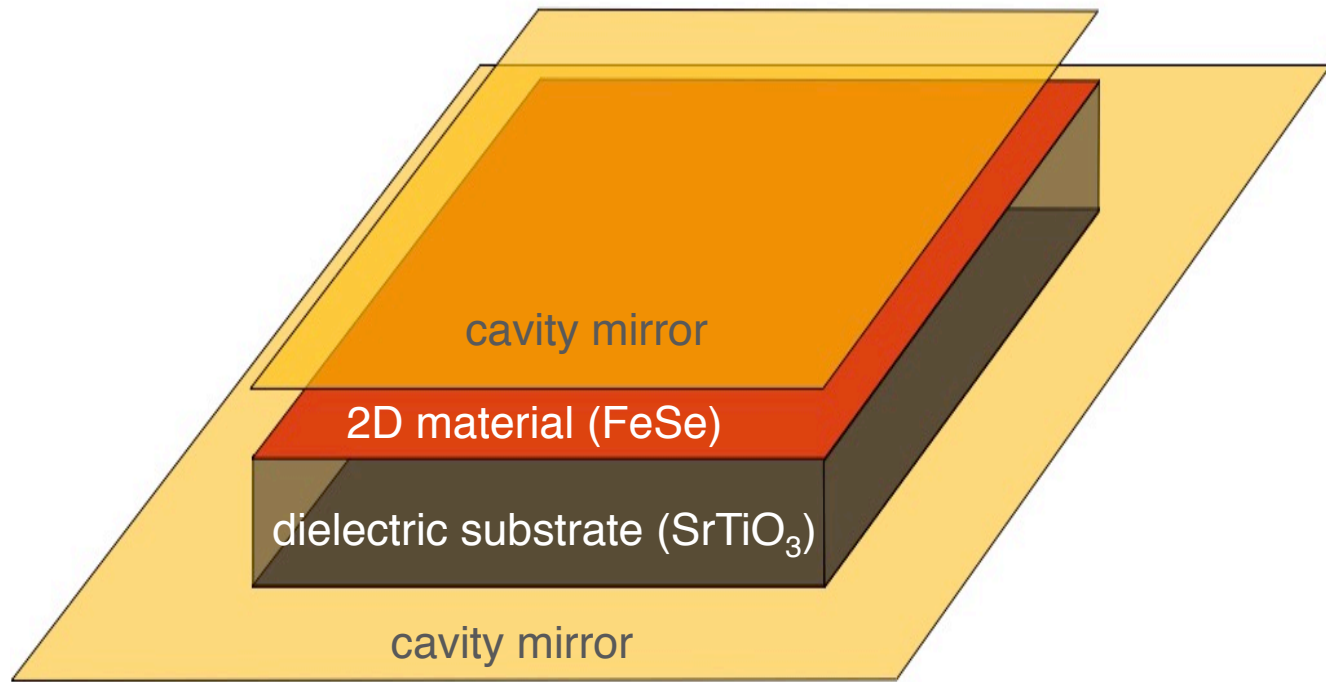
vs.  $T_{C,BCS} \approx 1.13\Omega \exp(-\frac{1}{\lambda})$

q-independent scattering

# Summary III

- cavity leads to **enhanced electron-phonon coupling**
- can one also enhance superconductivity?

*M. A. Sentef, M. Ruggenthaler, A. Rubio, arXiv:1802.09437  
(to appear in Science Adv.)*



## Ultrafast laser engineering of

- band structure, topology (Floquet)

*Nature Commun. 6, 7047 (2015)*

*Nature Commun. 8, 13940 (2017)*

*arXiv:1803.07447*

- electron-phonon coupling

*PRB 95, 024304 (2017)*

*PRB 95, 205111 (2017)*

*arXiv:1802.09437*

- Hofstadter's butterfly (subresonant  
excitations in correlated insulators)

*PRL 121, 097402 (2018)*

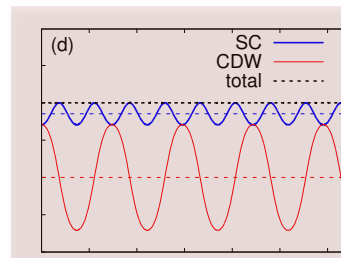
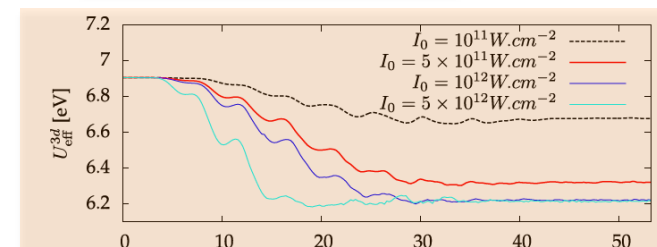
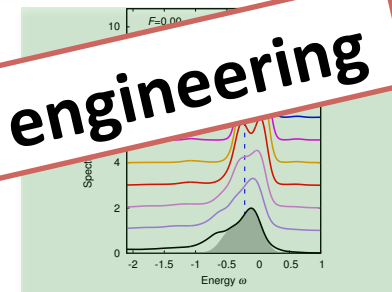
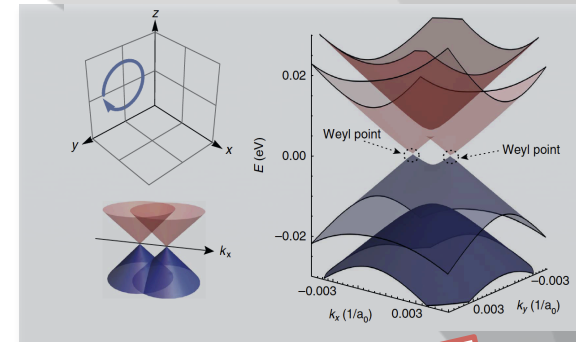
- ordered phases

*PRB 92, 224517 (2015) arXiv:1806.08187*

*PRB 93, 144506 (2016) arXiv:1808.00712*

*PRL 118, 087002 (2017) arXiv:1808.04655*

*arXiv:1810.06536*



**Towards nonequilibrium materials engineering**

# Outlook: Group projects

- R. Tuovinen (postdoc): nonequilibrium Green's functions (GKBA) for **time-resolved transport** and **excitonic condensates** (*JCTC 14, 2495 (2018)*; *arXiv:1808.00712*)
- G. Topp (PhD student): modeling **time-resolved spectroscopy**, **electron-lattice dynamics** (*arXiv:1803.07447, Nature Comm.*)
- S. Ramirez (PhD student) **light-induced Majoranas**
- M. Kalthoff (PhD student) time-dependent matrix product states (t-DMRG) for **Floquet engineering of correlated systems** (w/ D. Kennes, FU Berlin)
- D. Hofmann (master student) topological **exciton polaritons** (master), **machine learning** for time-dependent variational wave functions (w/ G. Carleo, CCQ NYC)
- X. Wang (student, Tsinghua) Green's functions for **cavity 2D materials** with focus on topology
- M. Puviani (PhD st., Modena) **quantum nonlinear phononics**, ultrafast melting of ferrielectric charge-density wave (*arXiv:1806.08187, PRB*)

