

TRANSIENT DYNAMICS
IN AN EXCITONIC INSULATOR:
FAST COMPUTATION OF
NONEQUILIBRIUM GREEN'S FUNCTIONS

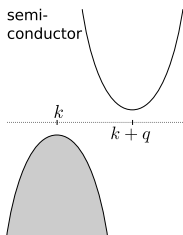
Riku Tuovinen, Denis Golež, Michael Schüler,
Martin Eckstein, and Michael Sentef



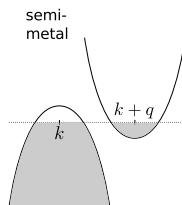
DPG Spring Meeting, Berlin
March 15th 2018

WHAT? EXCITONIC INSULATOR (EI) PHASE¹

Indirect semiconductor (small gap) or -metal (small overlap)



Reduce the gap below
exciton binding energy
 \Rightarrow EI phase



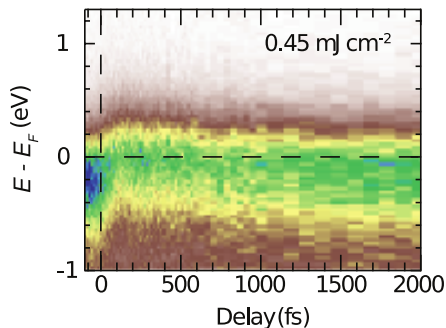
Reduce the overlap \Rightarrow
reduce the number of free
carriers \Rightarrow less screening
 \Rightarrow EI phase

\sim BCS superconductivity: electrons form Cooper pairs

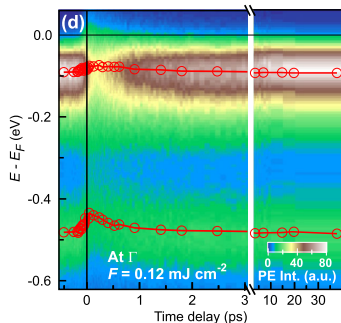
¹N. F. Mott, *Phil. Mag.* **6**, 287 (1961); L. V. Keldysh and Yu. V. Kopayev, *Sov. Phys. Solid State* **6**, 2219 (1965); D. Jérôme, T. M. Rice, and W. Kohn, *Phys. Rev.* **158**, 462 (1967)

WHY? RECENT TIME-DOMAIN EXPERIMENTS

Time-resolved ARPES measurements for materials exhibiting the EI phase [TiSe₂ and Ta₂NiSe₅]



S. Hellmann, *et al.*, EPJ Web of Conferences **41**, 03022 (2013)



S. Mor, *et al.*, Phys. Rev. Lett. **119**, 086401 (2017)

Critical photoexcitation observed: band gap can be either enhanced (\sim increased exciton condensation) or decreased

HOW? TIME-PROPAGATION OF GREEN FUNCTIONS^{2 3}

- ▶ Two-time Green's functions defined on the **Keldysh contour**

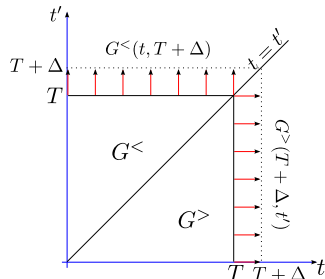
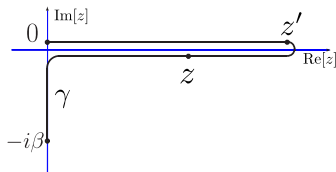
$$G(z, z') = -i \langle T_\gamma [\hat{\psi}(z) \hat{\psi}^\dagger(z')] \rangle$$

- ▶ Integro-differential equations

$$[\text{System}] [i\partial_z - h] G = \delta + \int_\gamma \Sigma G$$

System Many-body effects

- ▶ **Expensive for both CPU and RAM**



²A. Stan, N. E. Dahlen, and R. van Leeuwen, *J. Chem. Phys.* **130**, 224101 (2009)

³G. Stefanucci and R. van Leeuwen, *Nonequilibrium Many-Body Theory of Quantum Systems: A Modern Introduction*, (Cambridge University Press, Cambridge, 2013)

GENERALIZED KADANOFF–BAYM ANSATZ (GKBA)^{4 5}

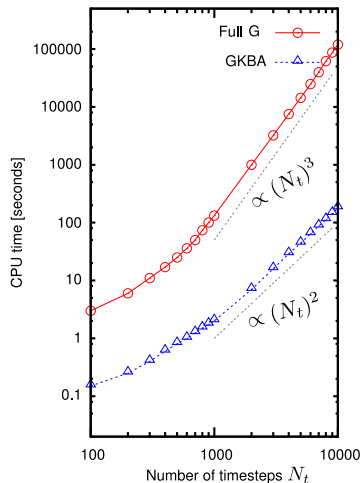
- ▶ Full Green's function reconstructed from **time-diagonal**

$$G^{\lessgtr}(t, t') \approx i \left[G^R(t, t') G^{\lessgtr}(t', t') - G^{\lessgtr}(t, t) G^A(t, t') \right]$$

- ▶ Approximate propagators

$$G^{R/A}(t, t') \approx \mp i \theta[\pm(t - t')] \exp[-ih(t - t')]$$

⇒ Evolution of a time-local density matrix $\rho(t) \equiv -iG^<(t, t)$

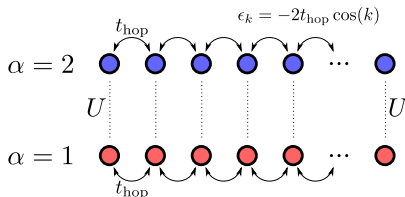


⁴P. Lipavský, V. Špička, and B. Velický, Phys. Rev. B **34**, 6933 (1986)

⁵S. Hermanns, K. Balzer, and M. Bonitz, Phys. Scr. **T151**, 014036 (2012)

MODEL FOR THE EXCITONIC INSULATOR⁶

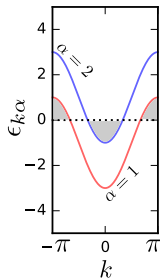
One-dimensional two-band system with interband Hubbard interaction



$$\hat{H}(t) = \hat{H}_{\text{eq}} + \hat{H}_{\text{ext}}(t),$$

$$\hat{H}_{\text{eq}} = \sum_{k\alpha} (\epsilon_{k\alpha} + \Delta_\alpha) \hat{c}_{k\alpha}^\dagger \hat{c}_{k\alpha} + \frac{1}{2} \sum_i U \hat{c}_{i,1}^\dagger \hat{c}_{i,1} \hat{c}_{i,2}^\dagger \hat{c}_{i,2},$$

$$\hat{H}_{\text{ext}}(t) = \sum_k (E(t) \hat{c}_{k,2}^\dagger \hat{c}_{k,1} + \text{h.c.})$$



Excitonic order parameter: $\langle \hat{c}_{(k+\pi)_1}^\dagger \hat{c}_{k_2} \rangle \neq 0$

⁶D. Golež, P. Werner, and M. Eckstein, Phys. Rev. B **94**, 035121 (2016)

EQUILIBRIUM BY MATSUBARA GREEN FUNCTION

$$k^M(\tau - \tau') \equiv -ik(-i\tau, -i\tau') \quad (k = G, \Sigma)$$

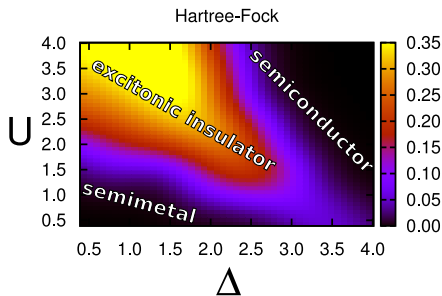
$$(-\partial_\tau - h_{\text{eq}})G^M(\tau - \tau') = \delta(\tau - \tau') + \int_0^\beta d\bar{\tau} \Sigma^M(\tau - \bar{\tau})G^M(\bar{\tau} - \tau')$$

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“Phase diagrams” using different self-energy approximations

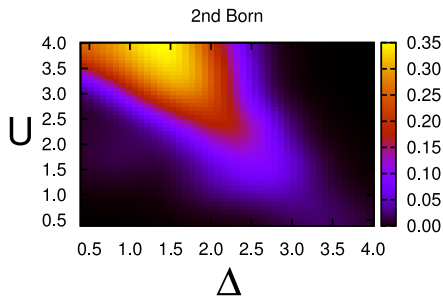
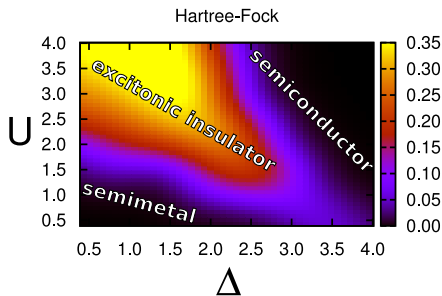


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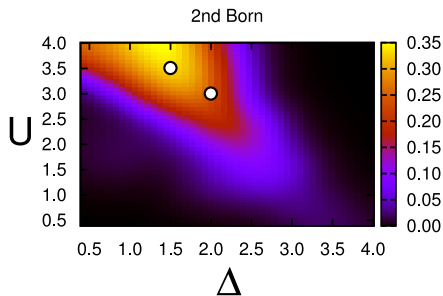
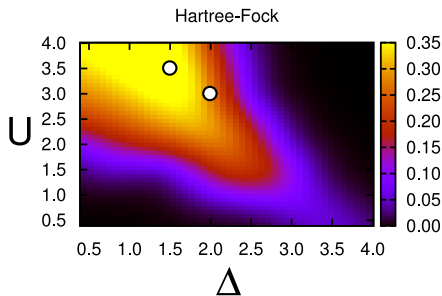


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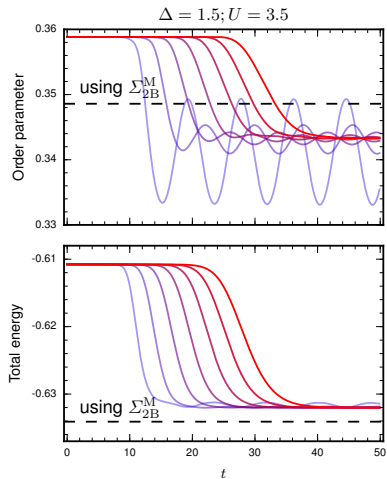
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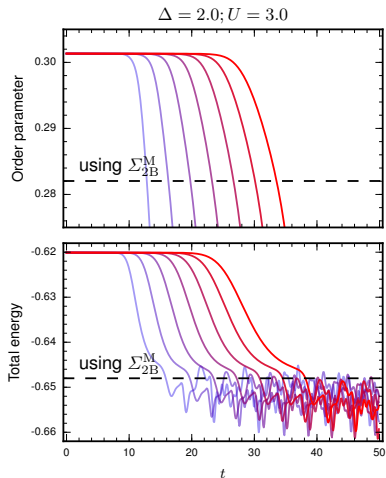
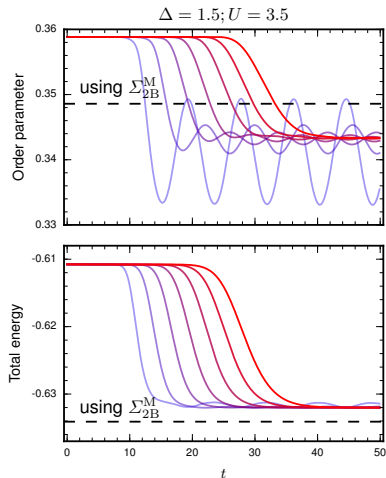
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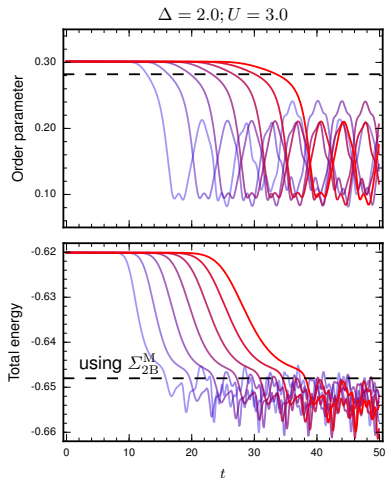
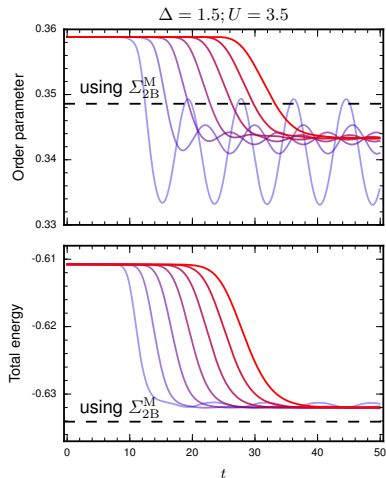
EQUILIBRIUM BY GKBA (ADIABATIC SWITCHING)



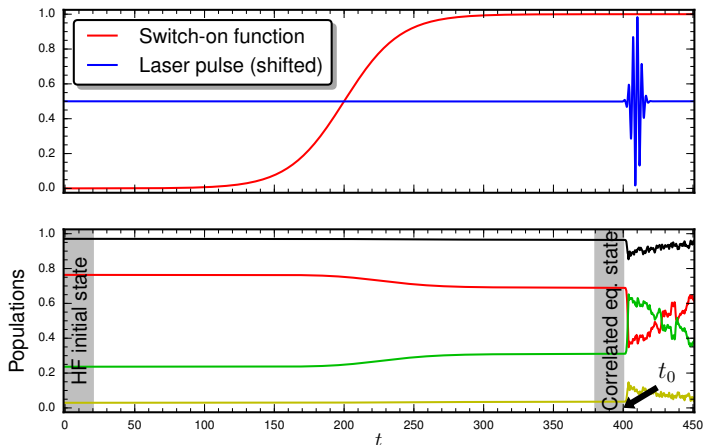
EQUILIBRIUM BY GKBA (ADIABATIC SWITCHING)



EQUILIBRIUM BY GKBA (ADIABATIC SWITCHING)



OUT-OF-EQUILIBRIUM: POPULATIONS AND ORDER



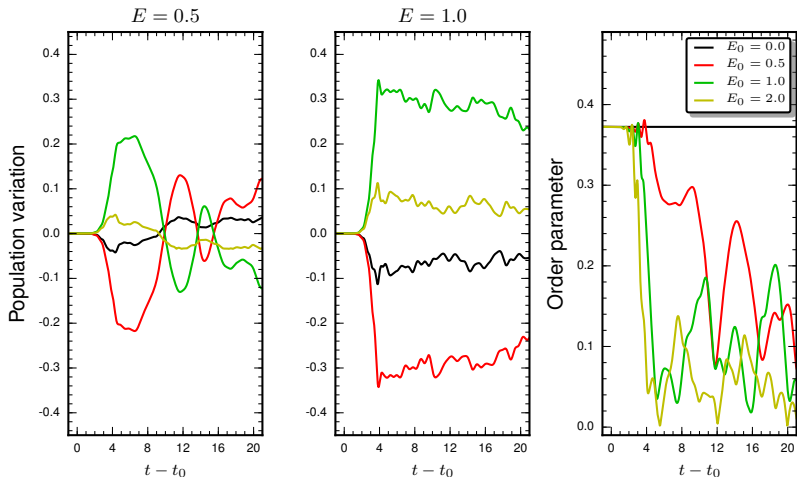
$\langle \hat{c}_{k1}^\dagger \hat{c}_{k1} \rangle$

 $\langle \hat{c}_{k2}^\dagger \hat{c}_{k2} \rangle$

 $\langle \hat{c}_{(k+\pi)1}^\dagger \hat{c}_{(k+\pi)1} \rangle$

 $\langle \hat{c}_{(k+\pi)2}^\dagger \hat{c}_{(k+\pi)2} \rangle$

OUT-OF-EQUILIBRIUM: POPULATIONS AND ORDER



SUMMARY

- ▶ Ultrafast experiments available in materials exhibiting the excitonic insulator phase
- ▶ Theoretical description is a challenge (electronic correlations, transient regime, ...)
- ▶ Generalized Kadanoff–Baym Ansatz computationally more applicable (must be careful though!)
- ▶ Preliminary results show light-induced population inversion and melting of the excitonic condensate

