

# High $T_c$ superconductors

IMPRS Focus Course „Superconductivity“

Friday lecture

Michael A. Sentef

with material from Mike Norman's 2011 talk  
„High-Temperature Superconductivity – After 25 years, where are we at?“

It All Started Back in 1986

Z. Phys. B – Condensed Matter 64, 189–193 (1986)



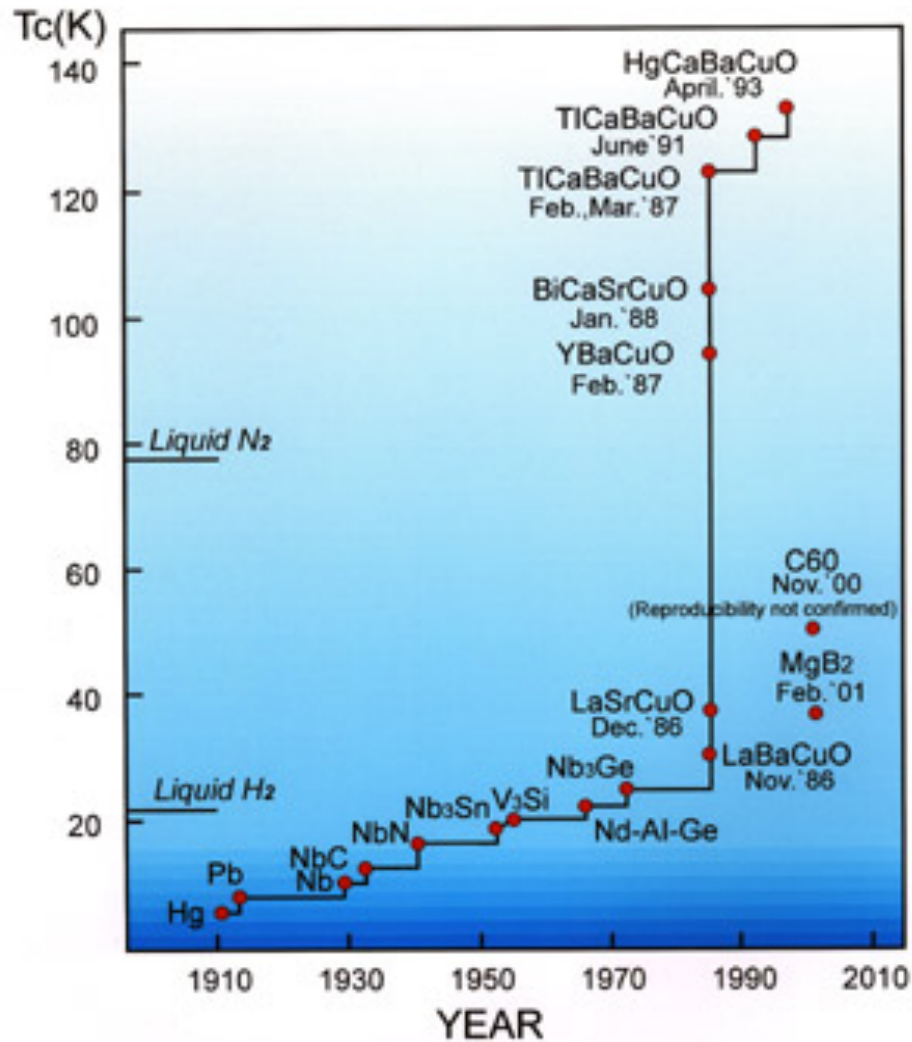
## Possible High $T_c$ Superconductivity in the Ba – La – Cu – O System

J.G. Bednorz and K.A. Müller

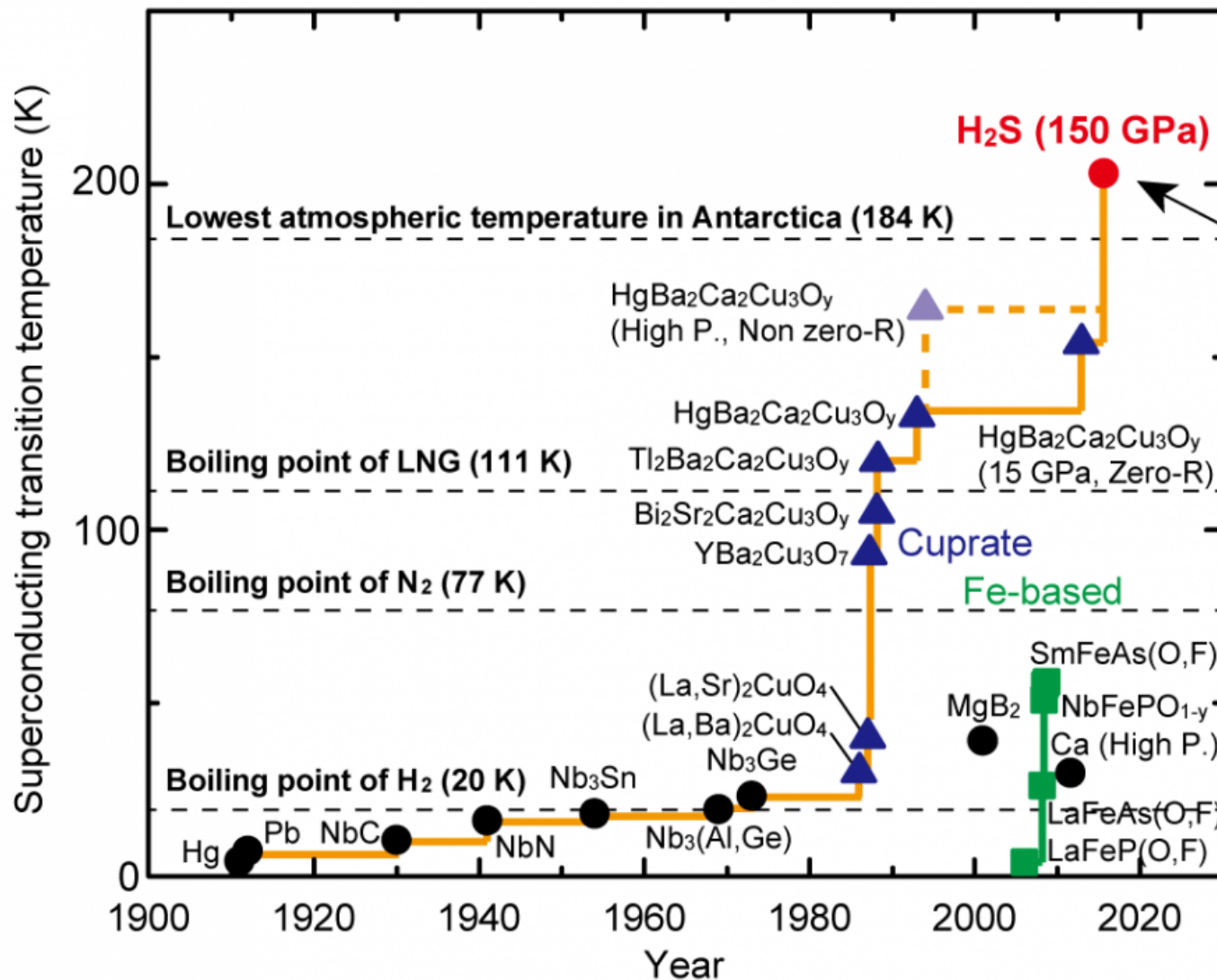
IBM Zürich Research Laboratory, Rüschlikon, Switzerland

Received April 17, 1986

$T_c$  Shot Up Like a Rock  
(many cuprates superconduct above 77K)

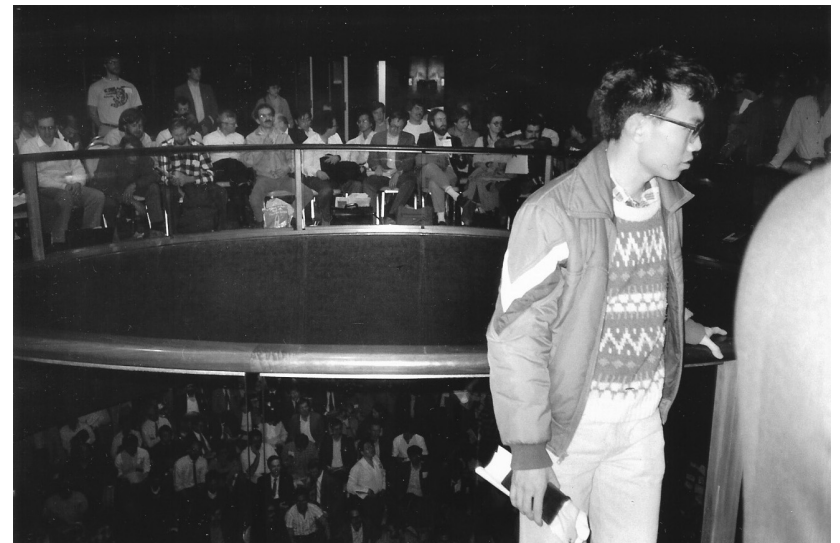


$T_c$  Shot Up Like a Rock  
(many cuprates superconduct above 77K)



credit: Osaka University

## Woodstock of Physics - March 1987





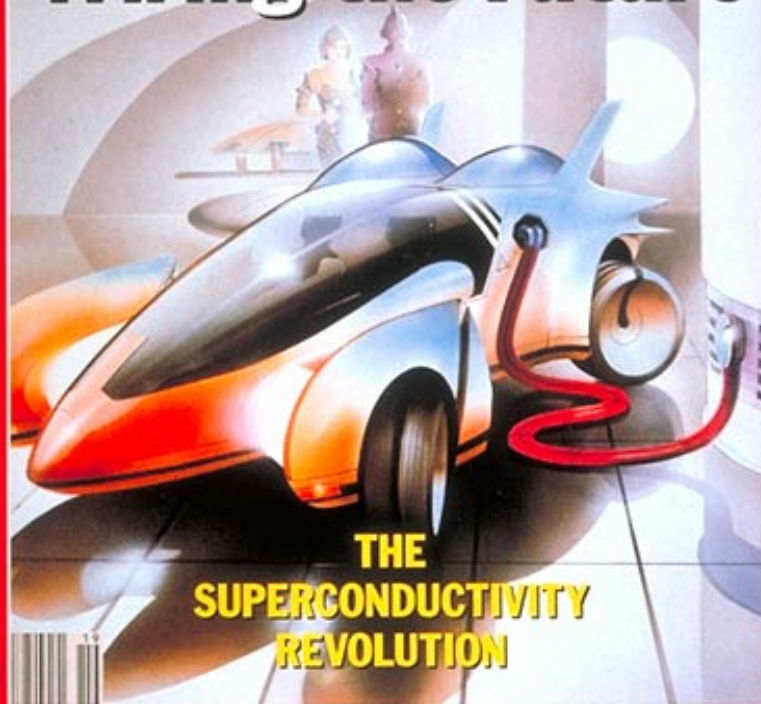
MAY 11, 1987

\$1.95

# TIME

## Wiring the Future

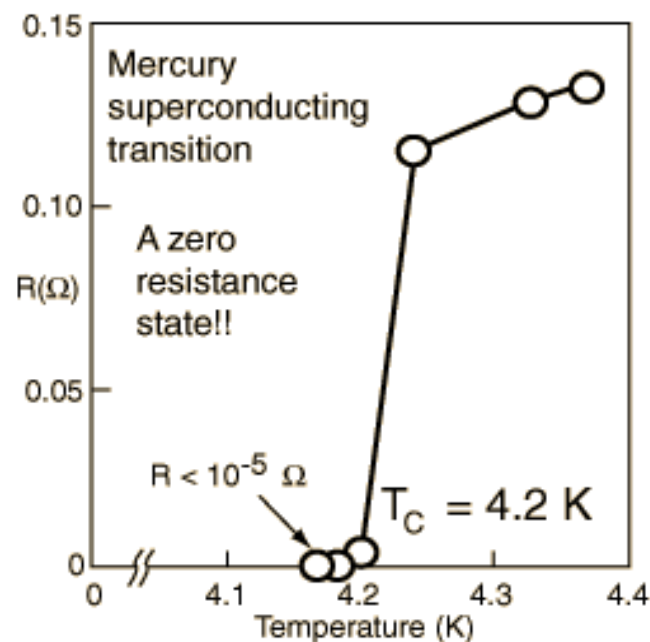
CONTRA ARMS  
The Widening  
Web



**THE  
SUPERCONDUCTIVITY  
REVOLUTION**



## Zero resistance

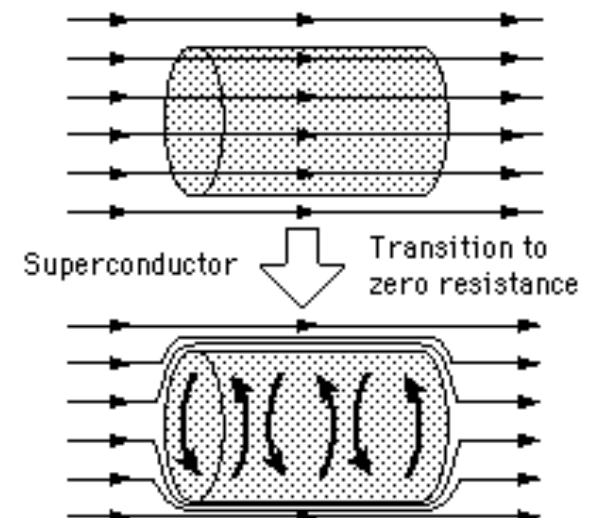
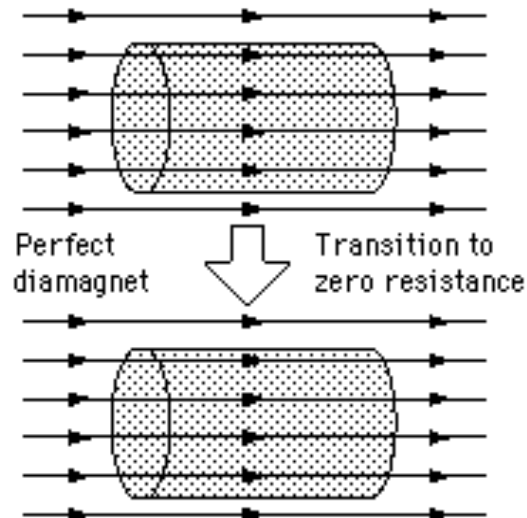


H. K. Onnes (1911)

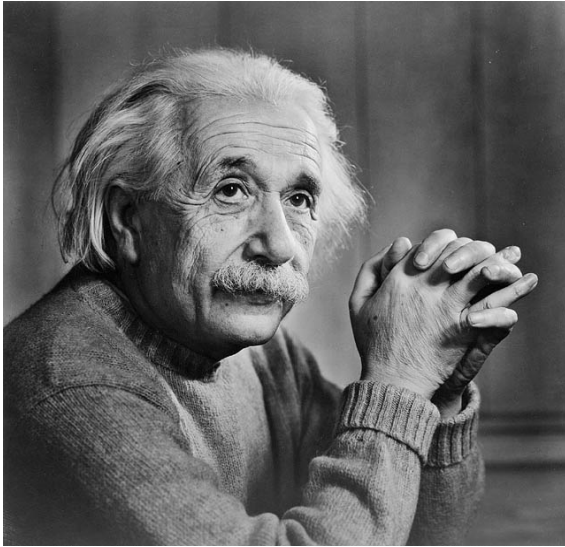
## Superconductors:

- (1) They are perfect conductors
- (2) They expel magnetic flux

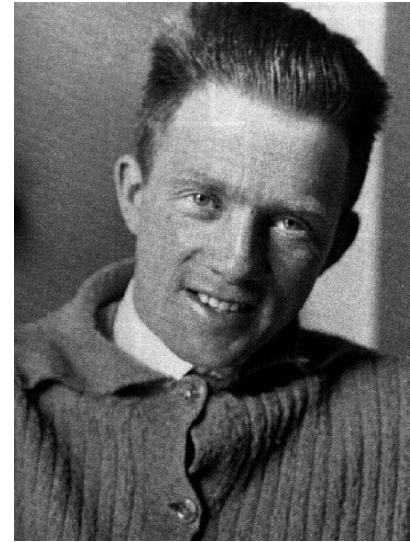
## Meissner effect (1933)



## The Path to a Microscopic Theory was Littered with Many Famous Physicists



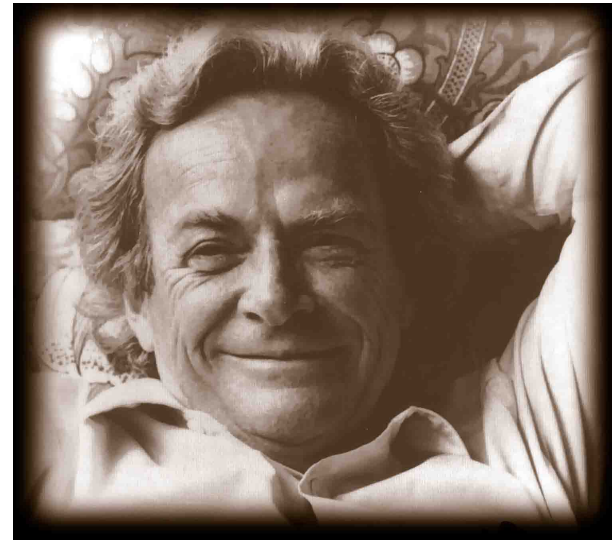
Einstein



Heisenberg



Landau



Feynman



Eventually, Three Guys in Illinois Got It Right  
(Bardeen, Cooper, Schrieffer - 1956,1957)



## A (Very) Short History of Superconductivity

1. London theory - rigidity to macroscopic perturbations implies a “condensate” (1935,1950)
2. Ginzburg-Landau ( $\Psi$ ) theory - order parameter for condensate (1950)
3. Isotope effect (Maxwell, Serin & Reynolds, Frohlich, 1950)
4. Cooper pairs (1956)
5. Bardeen-Cooper-Schrieffer (BCS) microscopic theory (1957)
6. Type-II superconductors (Abrikosov vortices, 1957)
7. Connection of BCS to Ginzburg-Landau (Gorkov, 1958)
8. Strong coupling superconductivity (Eliashberg, Nambu, Anderson, Schrieffer, Wilkins, Scalapino ..., 1960-1963)
9. p-wave superfluidity in  $^3\text{He}$  (Osheroff, Richardson, Lee, 1972; Leggett, 1972)
10. Heavy Fermion Superconductivity (Steglich, 1979)
11. High Temperature Superconductivity (Bednorz & Muller, 1986)
12. Iron Arsenides (Hosono, 2008)

## Rules of B. Matthias for discovering new superconductors

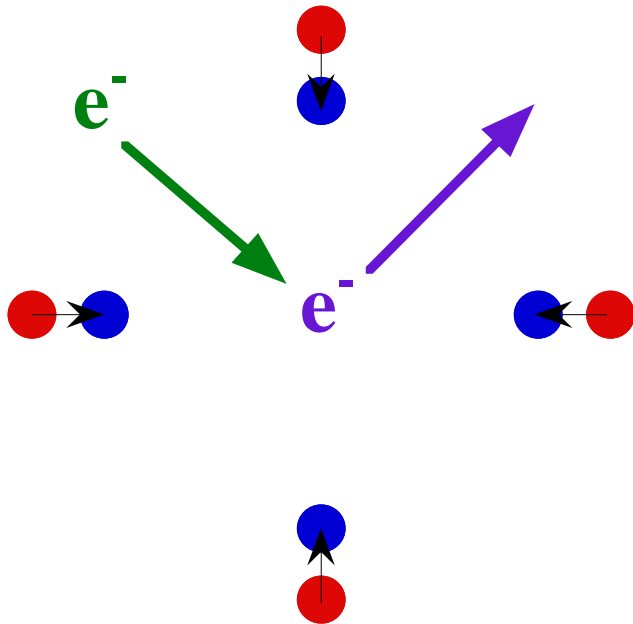
1. high symmetry is best
2. peaks in density of states are good
3. stay away from oxygen
4. stay away from magnetism
5. stay away from insulators
6. stay away from theorists



Scanned at the American Institute of Physics

# Everything You Wanted to Know About Pair Formation (But Were Afraid to Ask)

(the electron-phonon case)



1. 1st  $e^-$  attracts + ions
2. Ions shift position from red to blue
3. 1st  $e^-$  moves away
4. 2nd  $e^-$  sees + ion hole and moves to former position of 1st  $e^-$

Interaction is local in space  
(s-wave pairs,  $L=0$ ,  $S=0$ )  
but retarded in time  
( $T_c \ll$  Debye frequency)





But cuprates have  
d-wave pairs!  
( $L=2$ ,  $S=0$ )

van Harlingen;  
Tsuei & Kirtley -  
Buckley Prize -1998

Artwork by  
Gerald Zeldin (2000)

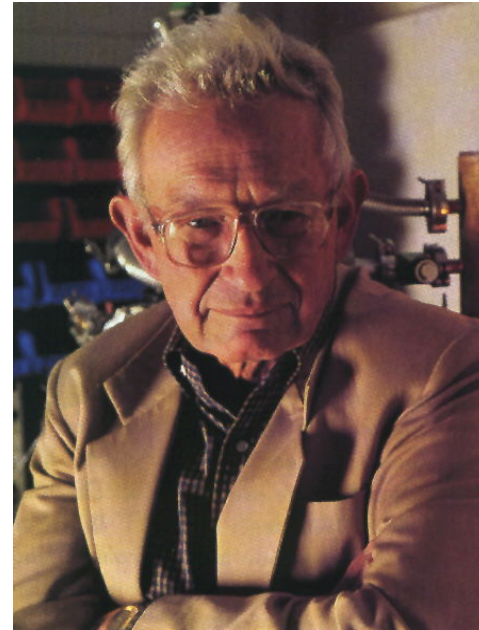




Alex Abrikosov  
(small  $q$  phonons)



Bob Laughlin  
(competing phases)



Phil Anderson  
(RVB; interlayer tunneling; RVB)



Karl Mueller  
(bipolarons)

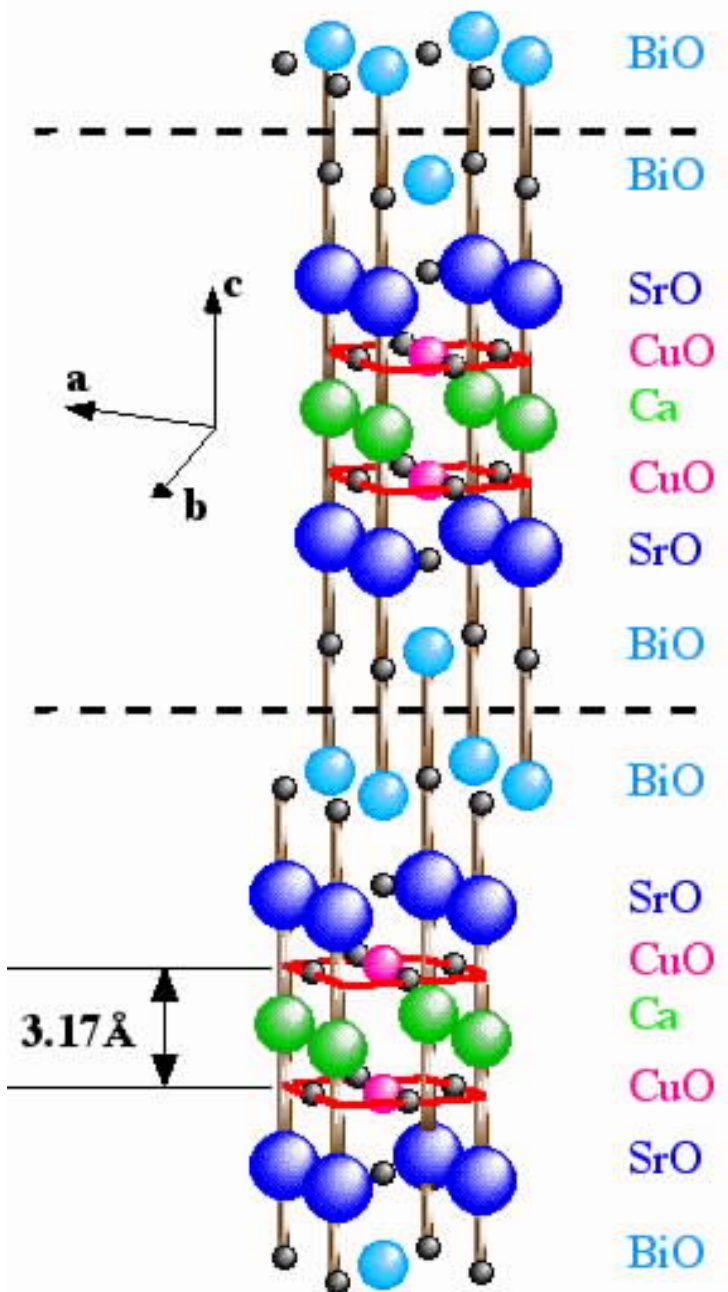


Bob Schrieffer  
(spin bags)

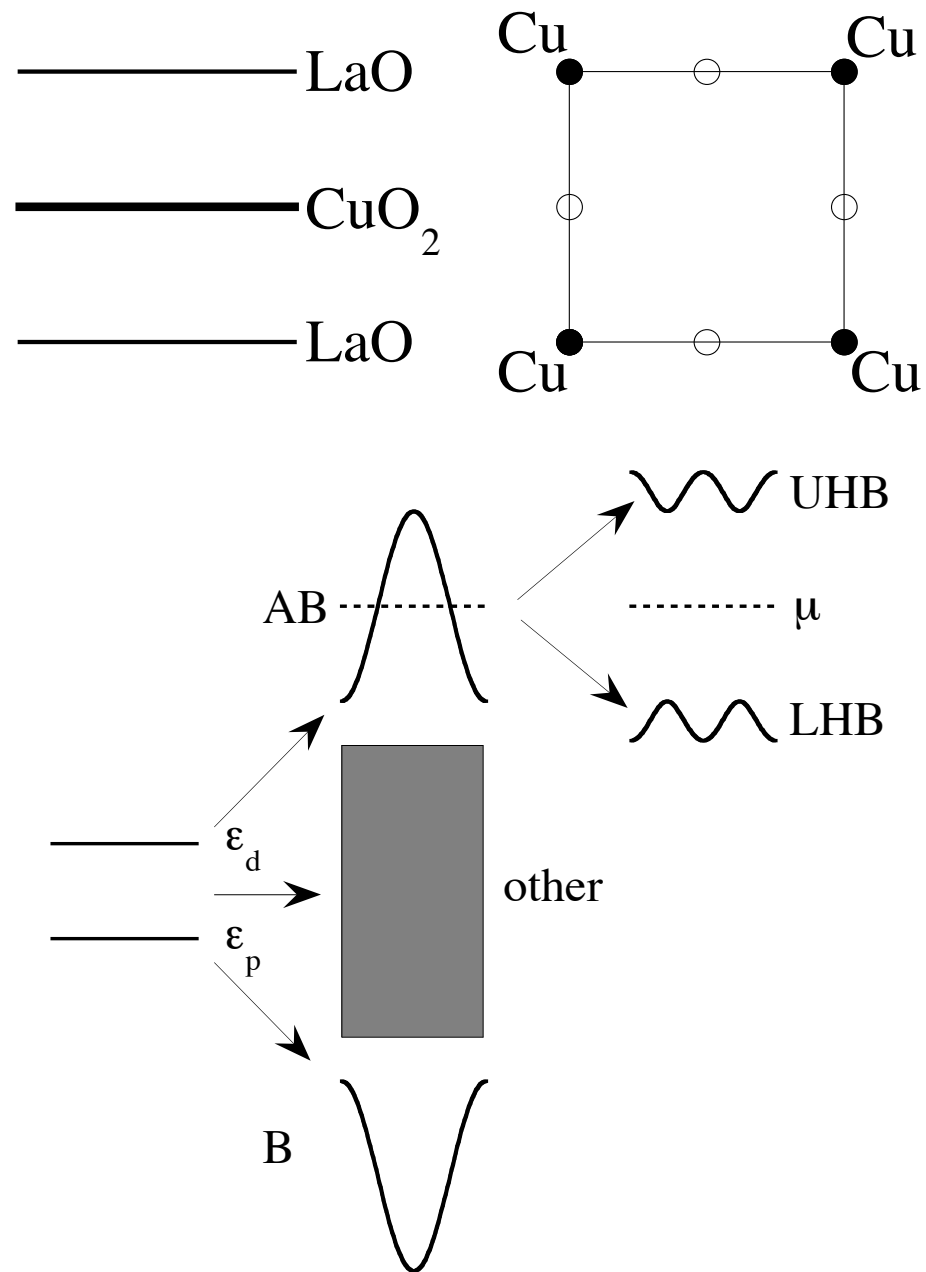


Tony Leggett  
(interlayer Coulomb)

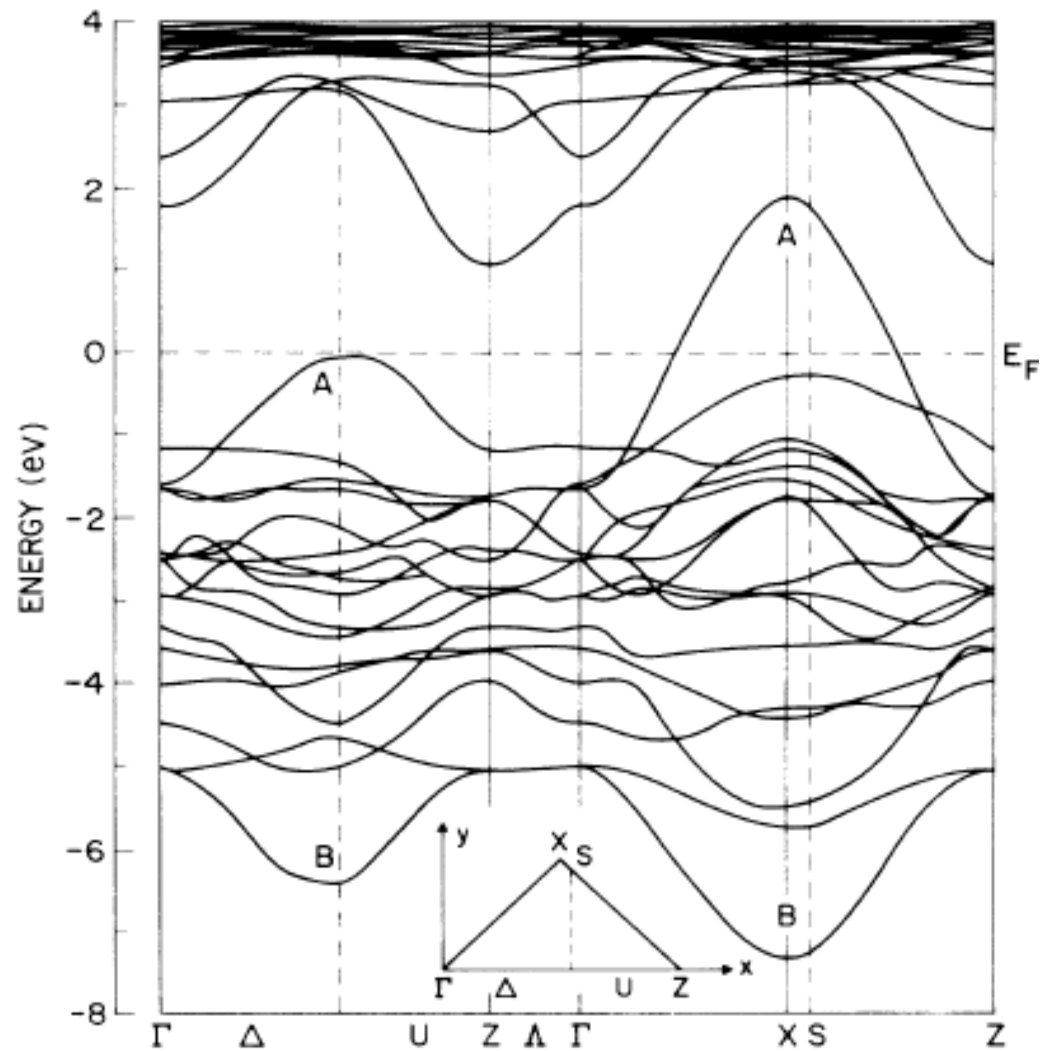
# Bi2212



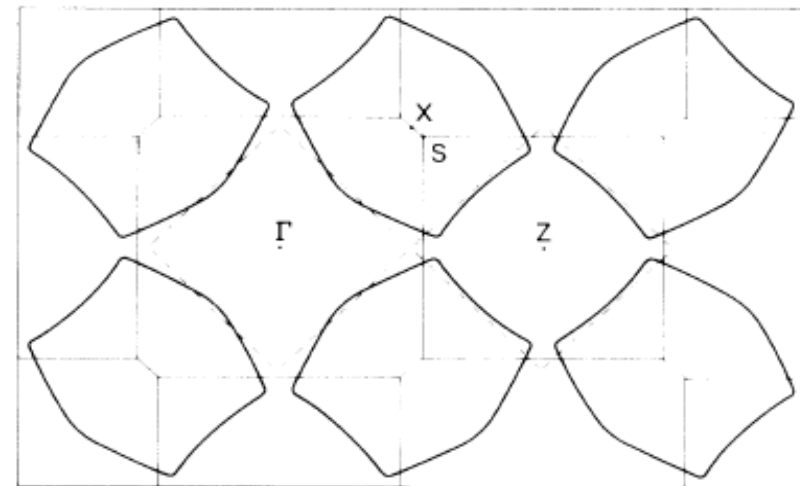
## Electronic Structure of Cuprates



## Electronic structure from density functional theory



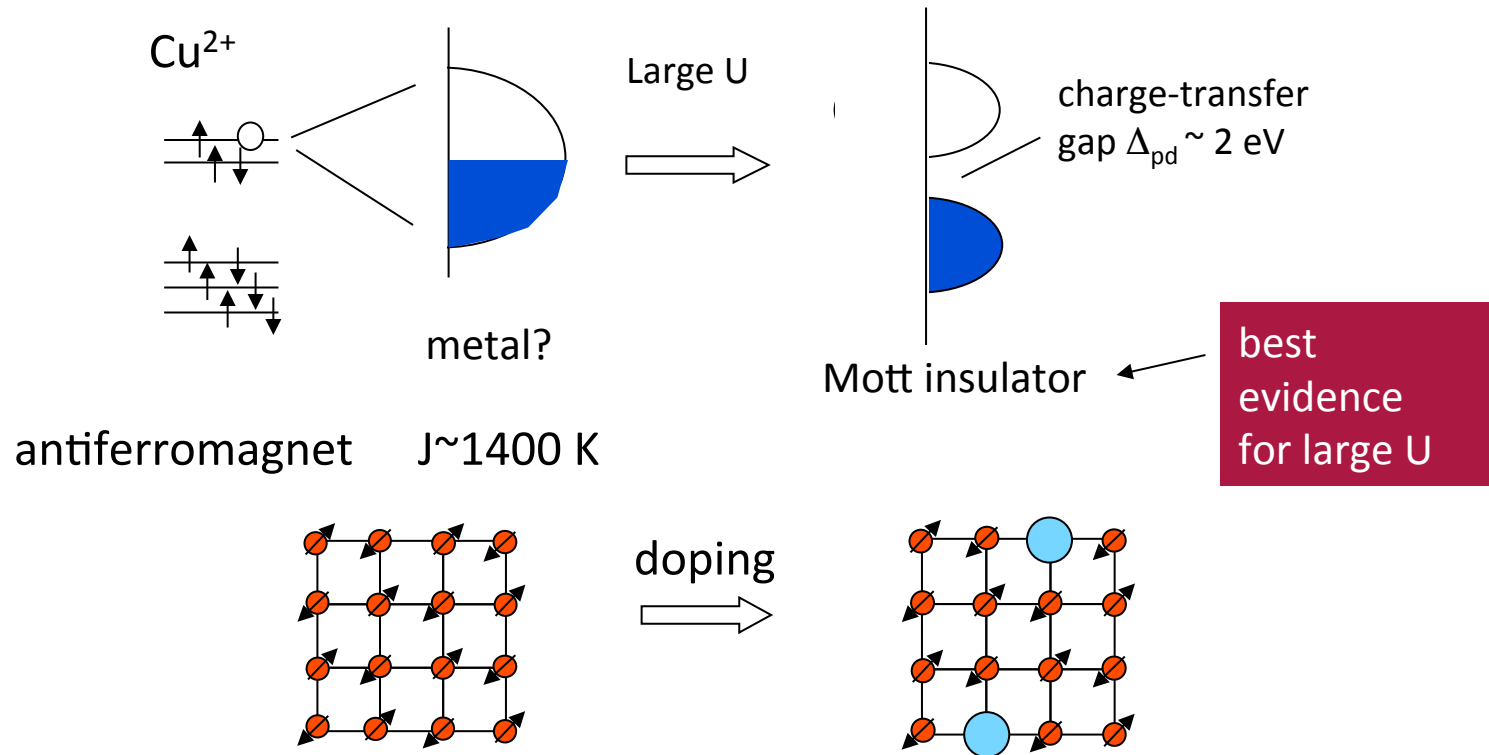
Energy vs Momentum



Fermi surface

Len Mattheiss  
PRL (1987)

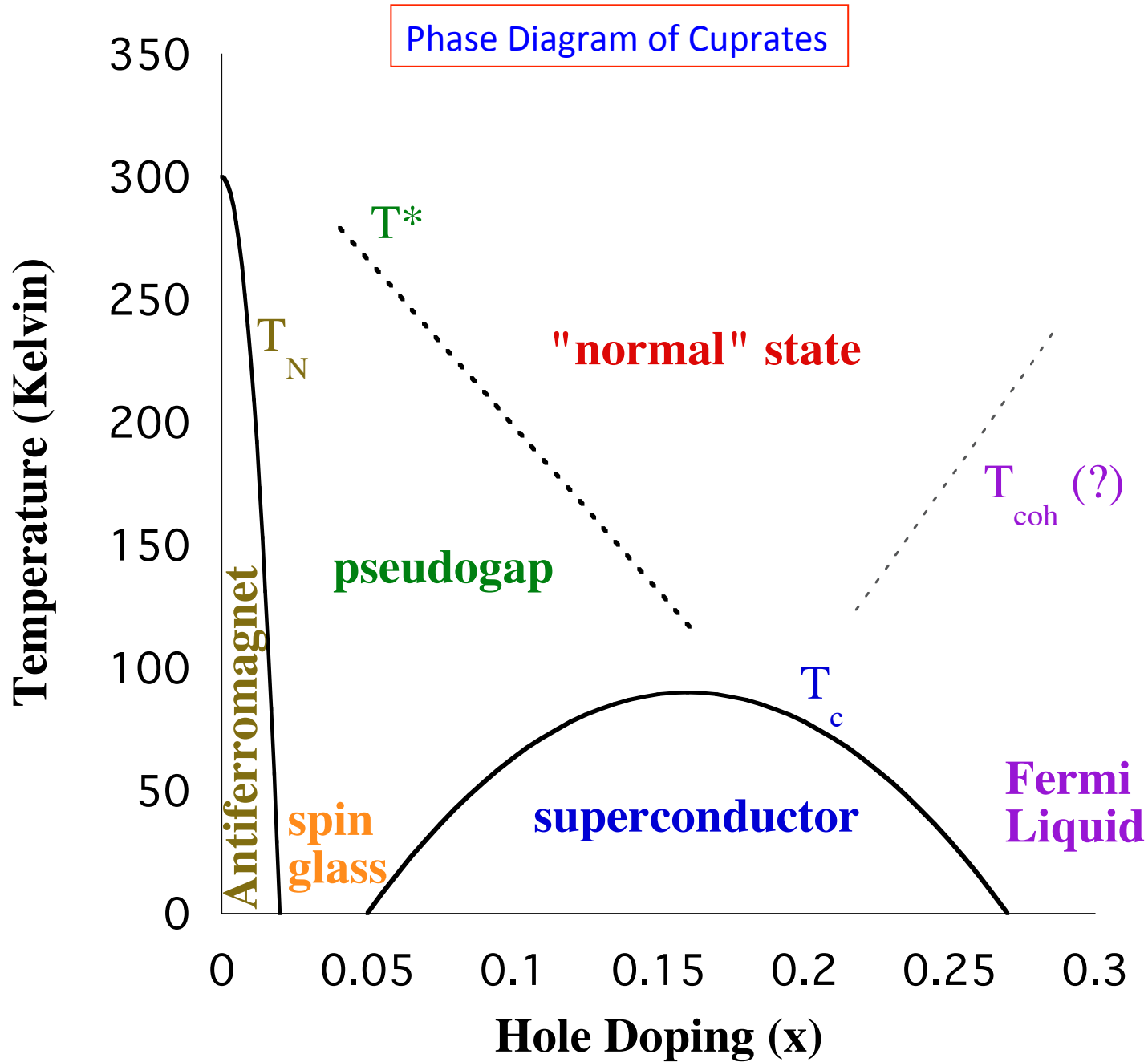
# Short (and biased!) tutorial on cuprates



$$H = -t \sum_{i,j,\sigma} c_{i\sigma}^{\dagger} c_{j\sigma} + U \sum_i n_{i\uparrow} n_{i\downarrow} \quad \text{Hubbard}$$

$$t = 0.3 \text{ eV}, \quad U = 2 \text{ eV}, \quad J = 4t^2/U = 0.12 \text{ eV}$$

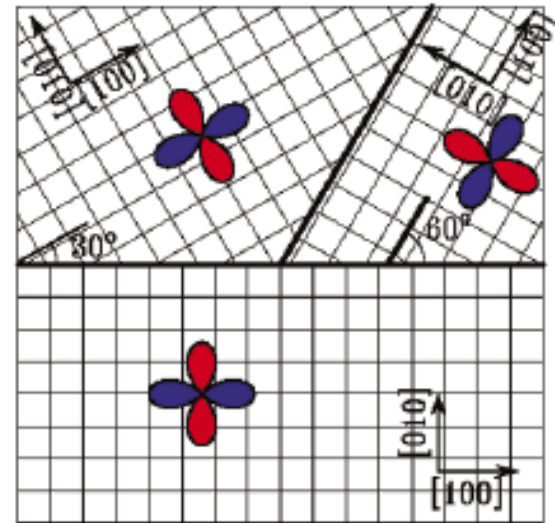
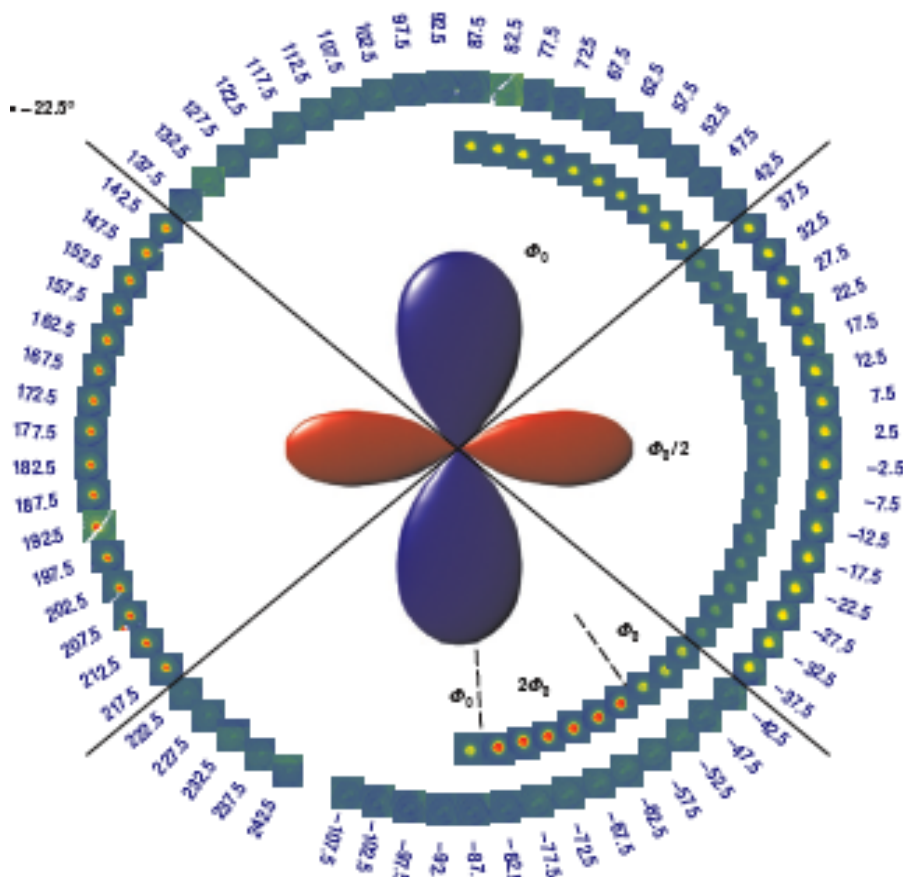
(slide from Phil Anderson)





## What We DO Know

1. There are  $2e^-$  pairs
2. The pairs are d-wave ( $L=2, S=0$ )
3. There are “normal” (i.e.,  $2e^-$ ) vortices
4. Quasiparticles exist (but only below  $T_c$ )



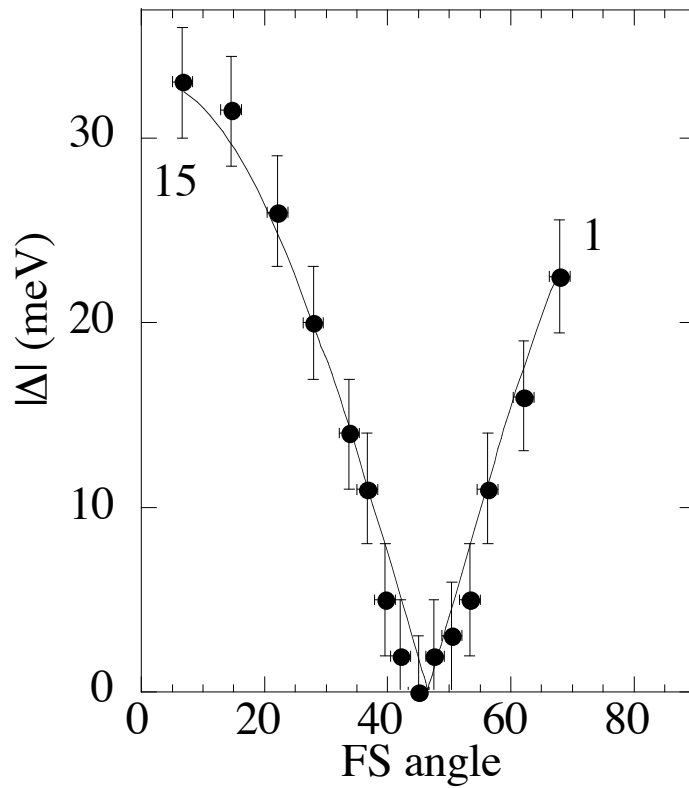
d-wave pairing observed by phase sensitive tunneling -

van Harlingen, Kirtley & Tsuei  
Kirtley *et al*, Nat. Phys. (2006)

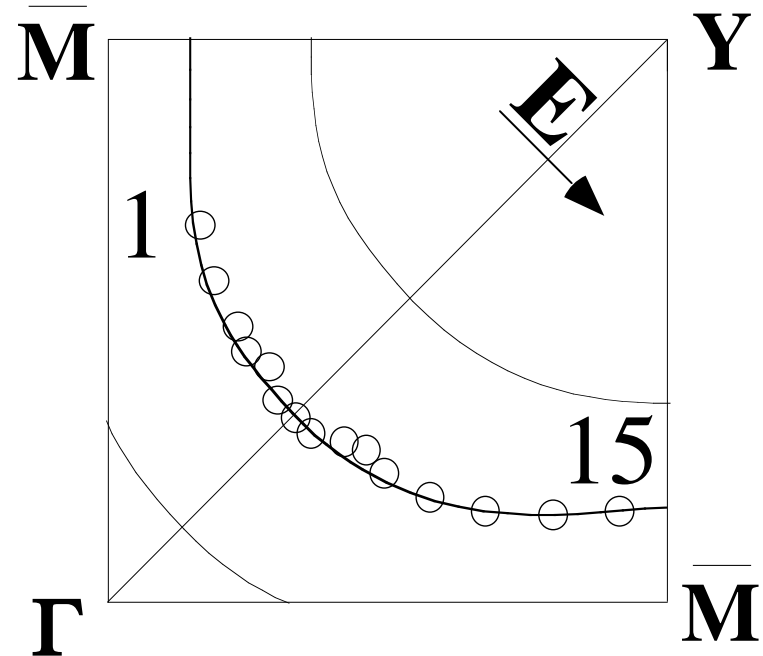
# Extraction of the Superconducting Energy Gap from Photoemission

Campuzano, Shen, Johnson – Buckley Prize (2011)

$\Delta_k \rightarrow \cos(k_x a) - \cos(k_y a) \rightarrow$  Implies near-neighbor pairs



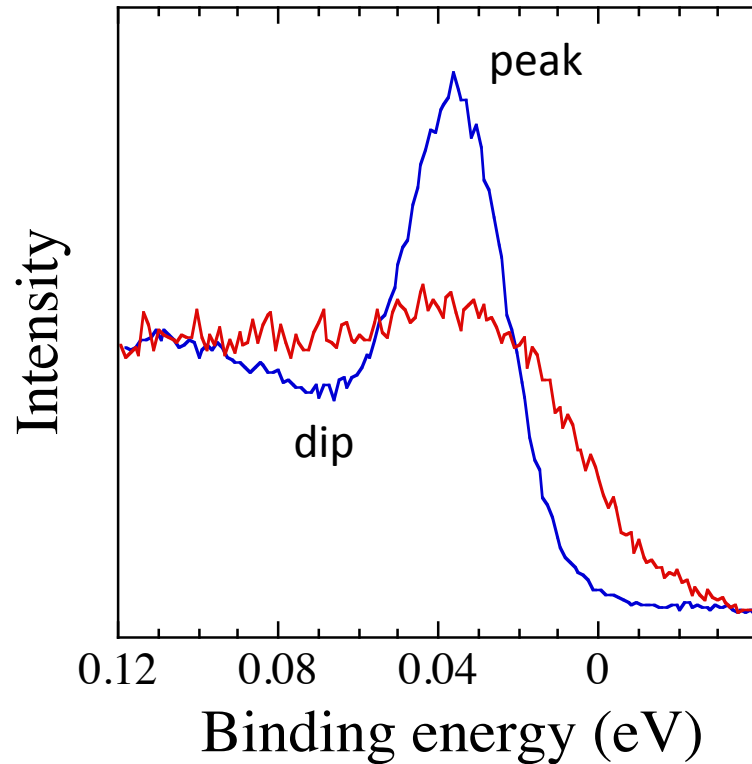
Dirac cone



Bi2212,  $T_c = 87\text{K}$

Ding *et al.*, PRB (1996)

Photoemission spectrum **above** and **below**  $T_c$   
at momentum  $k=(\pi,0)$  for Bi2212

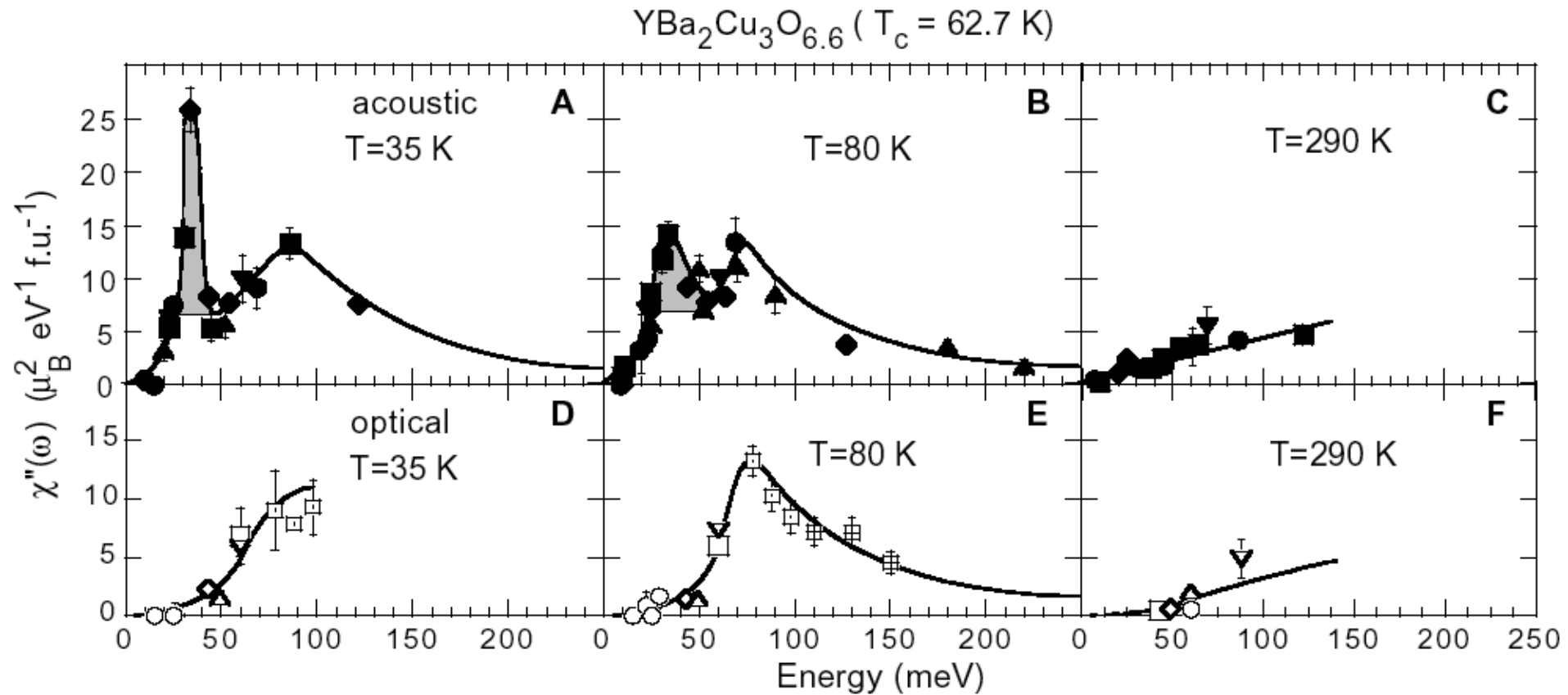


Incoherent normal state

Coherent superconductor

Norman *et al*, PRL (1997)

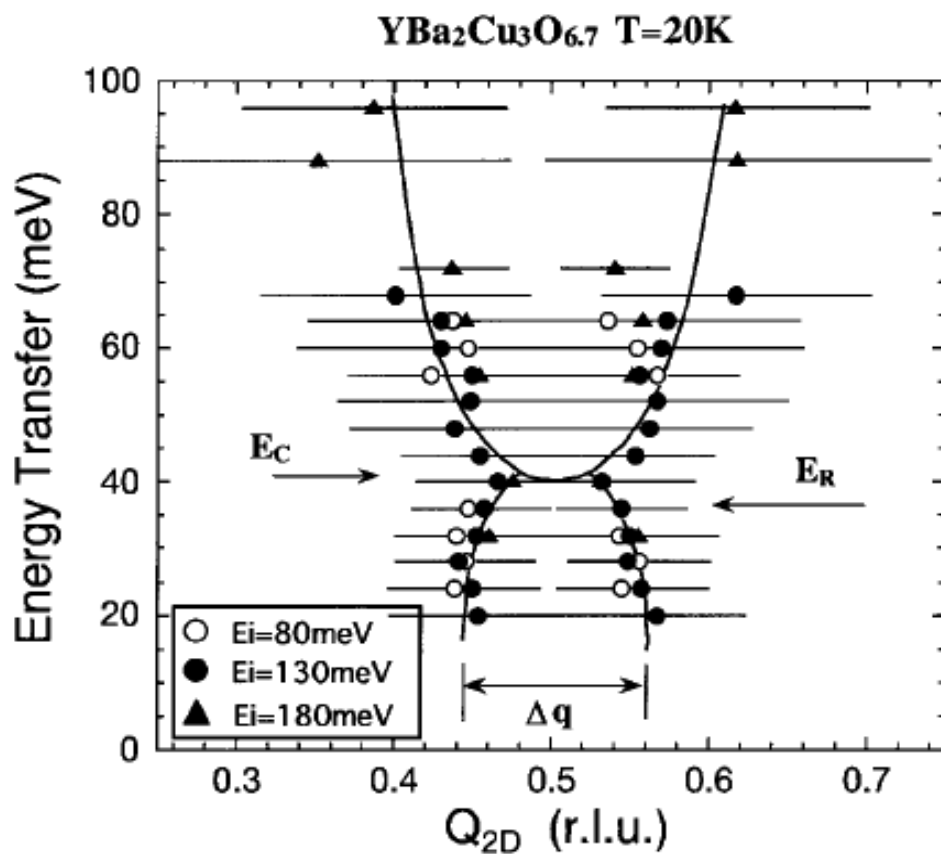
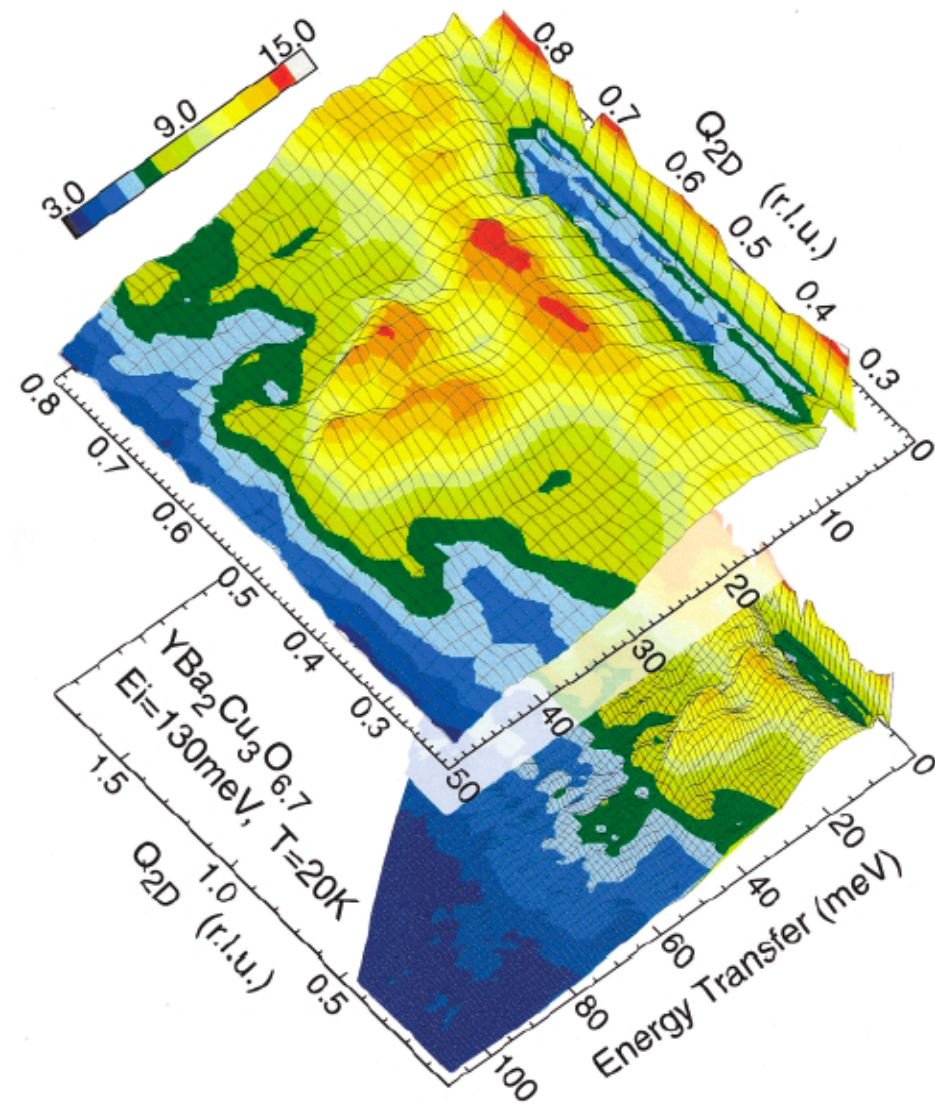
Neutron Spin Resonance ( $S=1$  excitation)  
Rossat-Mignod/Bourges, Mook/Dai, Keimer/Fong



Dai *et al*, Nature (1999)

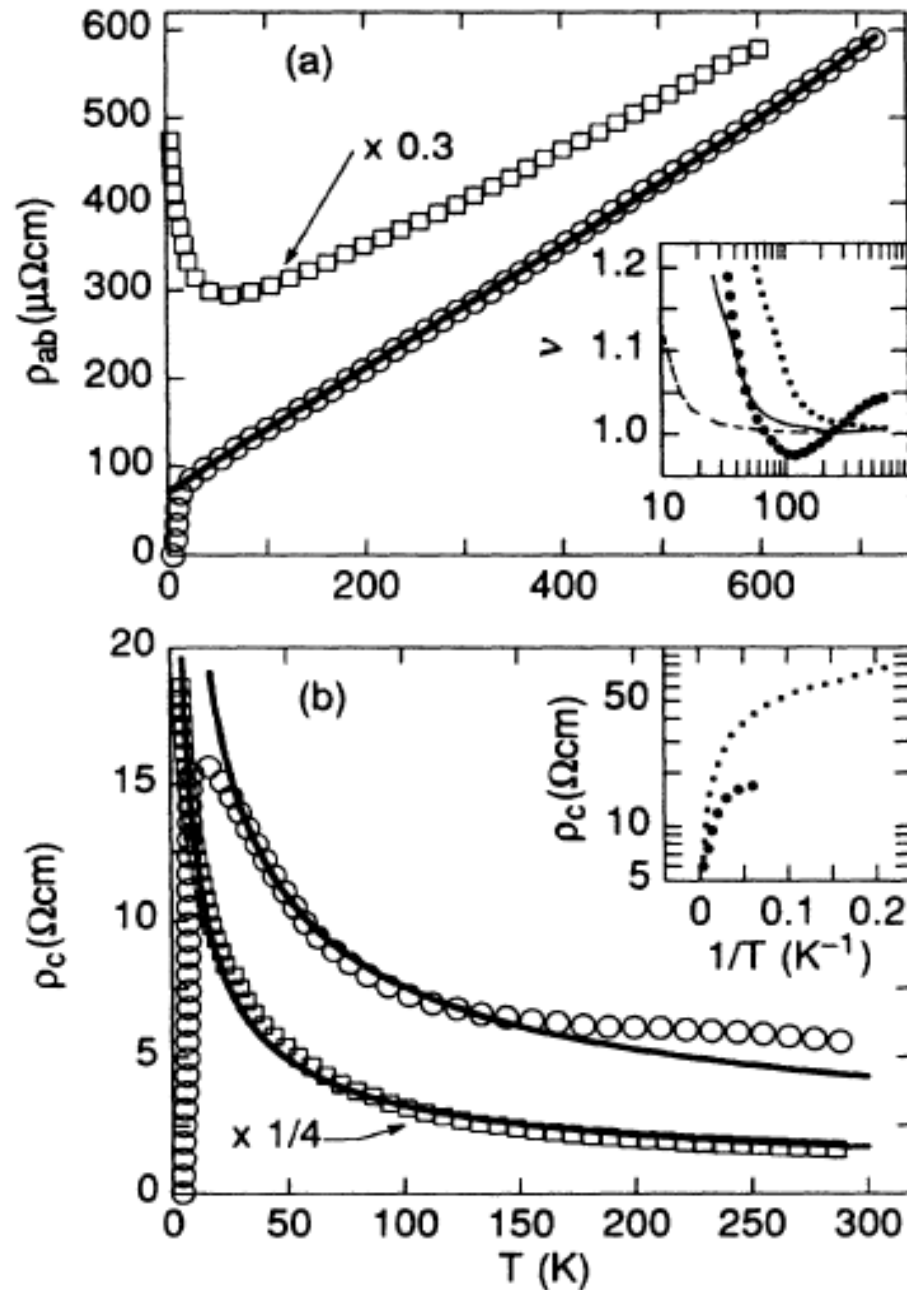
Dispersion of magnetic excitations has the form of an hourglass

Arai *et al*, PRL (1999)





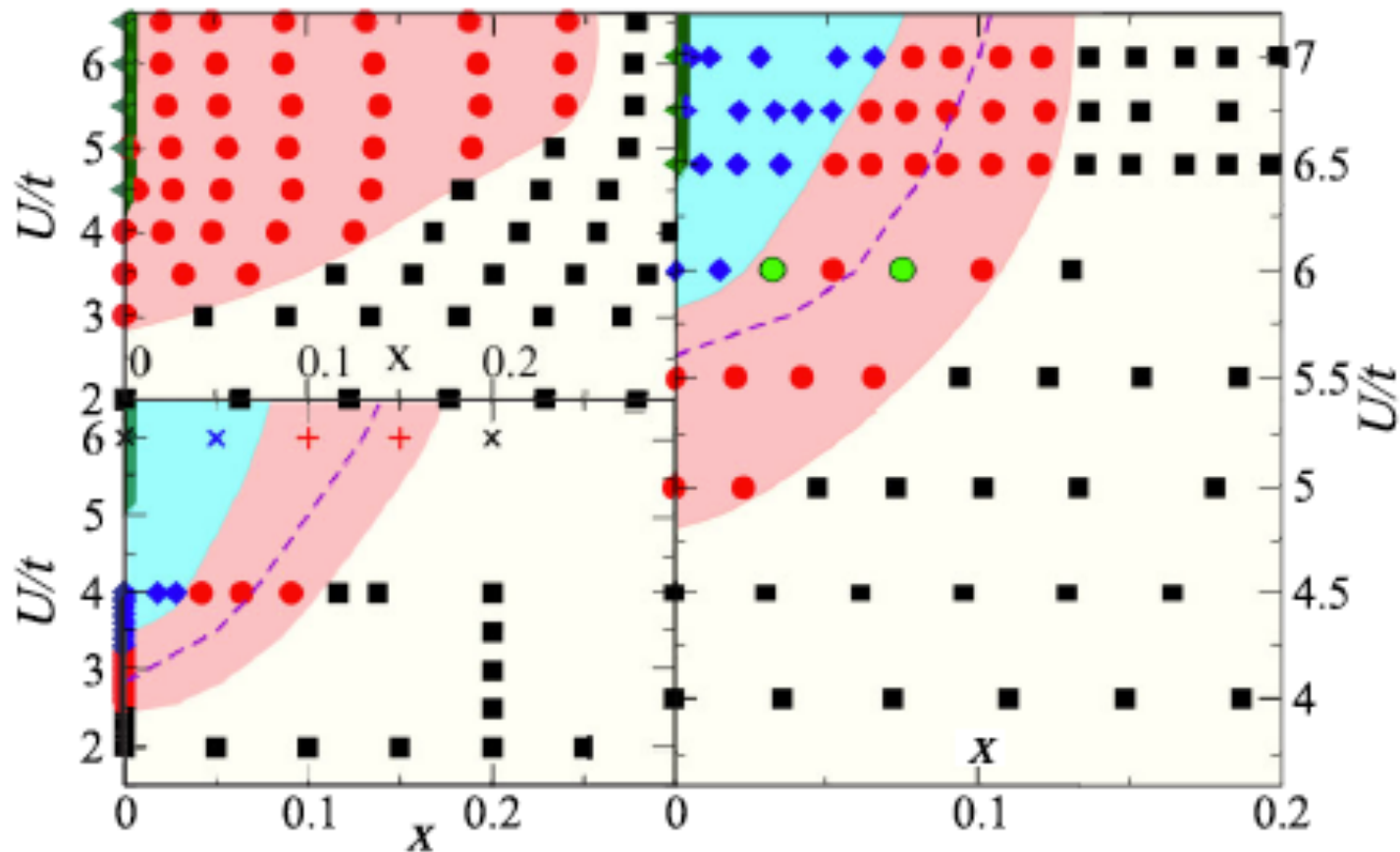
The “strange metal” phase exhibits linear  $T$  resistivity



Martin *et al*  
PRB (1990)

# Superconductivity and the Pseudogap in the Two-Dimensional Hubbard Model

Emanuel Gull,<sup>1,2</sup> Olivier Parcollet,<sup>3</sup> and Andrew J. Millis<sup>4</sup>





evidence for **d-wave superconductivity** in the  
Hubbard model (no phonons, just onsite repulsion  $U$ )


# Rules of B. Matthias for discovering new superconductors

1. high symmetry is best

2. peaks in density of states are good

 stay away from oxygen

 stay away from magnetism

 stay away from insulators

 stay away from theorists



## Paradigm shift!

high  $T_c$  materials are/have many things that conventional superconductors are/have **not**:

- terrible metals
- strong magnetic correlations
- lots of oxygen
- two-dimensional / anisotropic
- role of phonons still unclear but they are likely not the sole cause of high  $T_c$
- possibly no pairing glue needed (but this is under debate)