

# Bands with plane waves

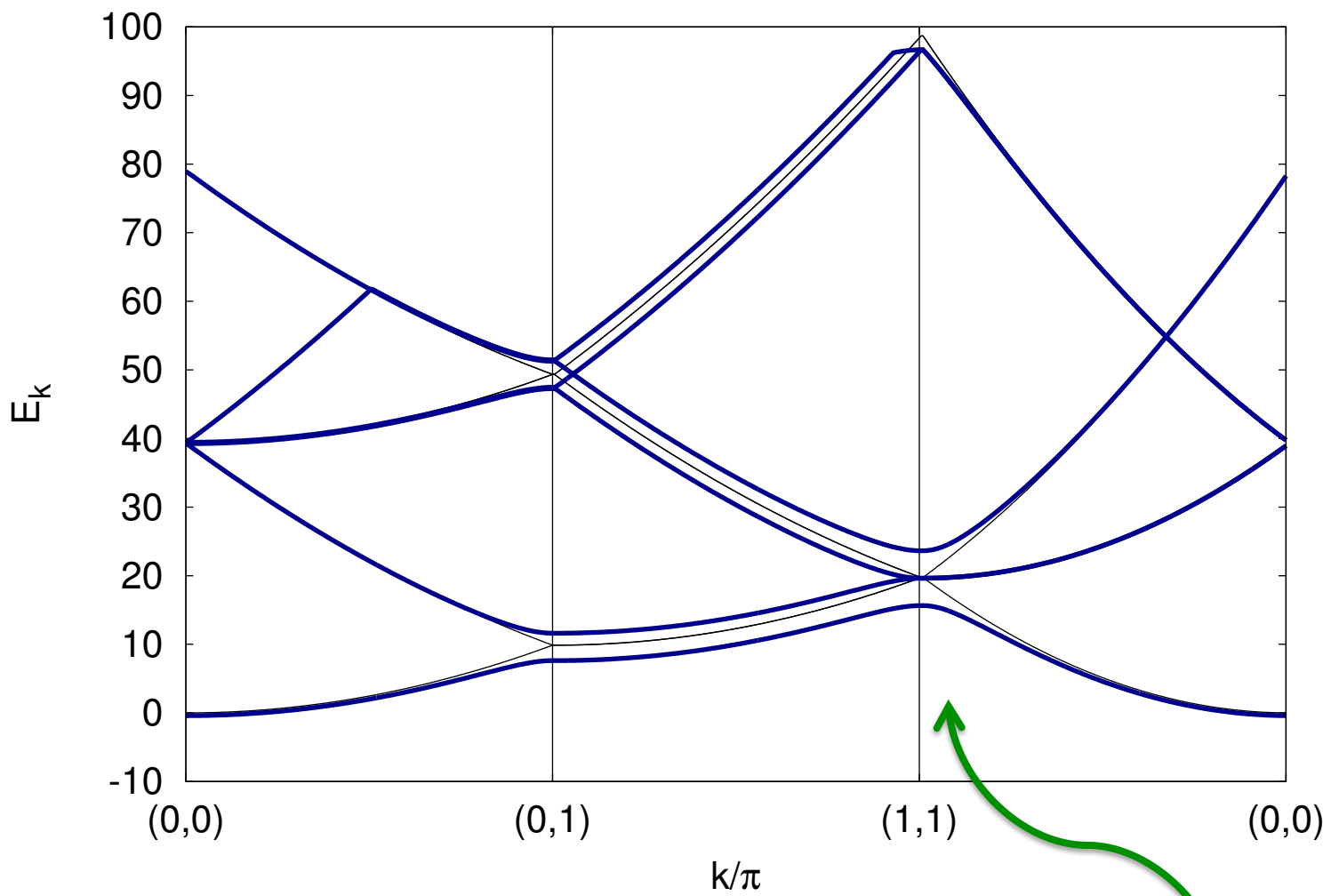
IMPRS Solid State Physics

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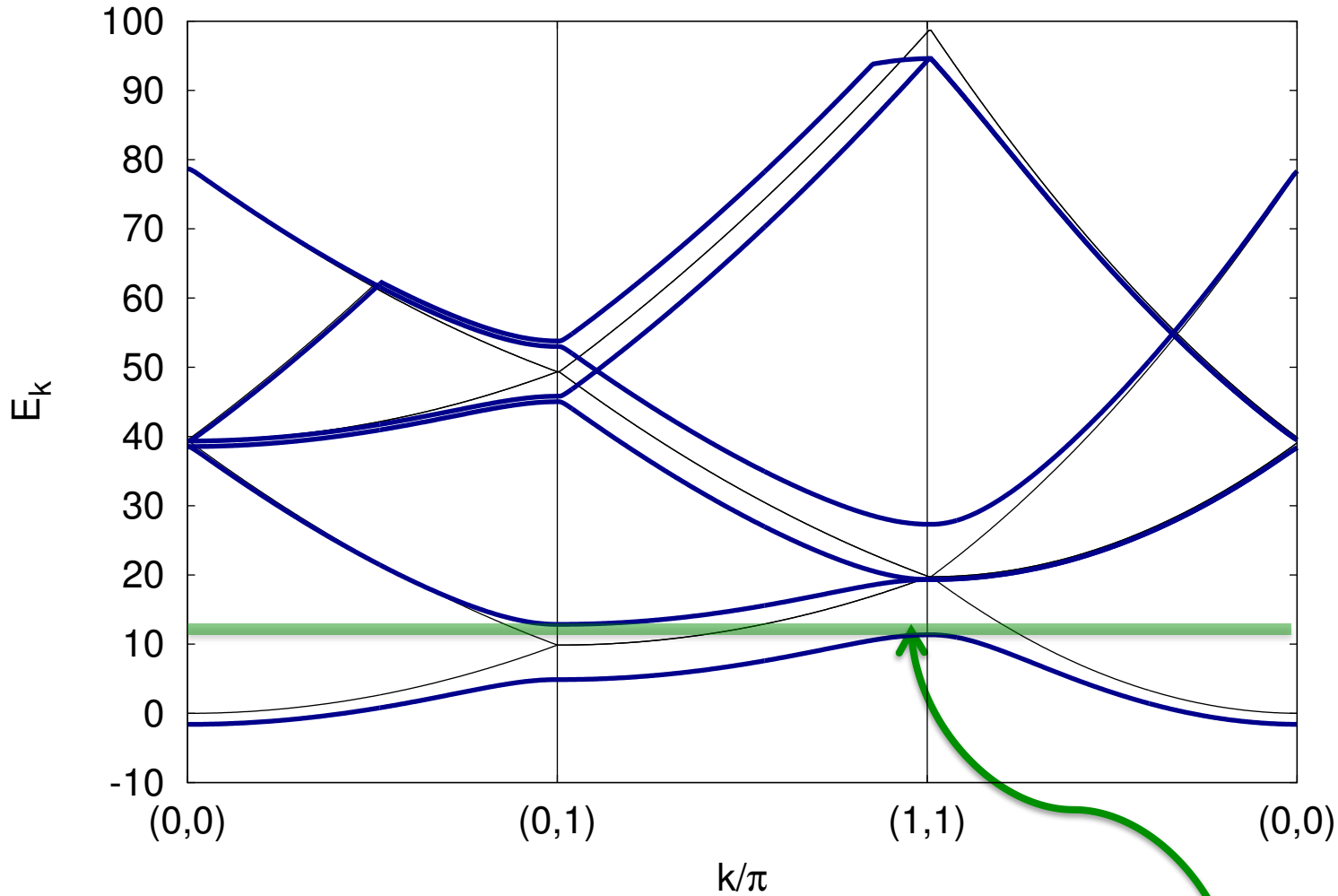
MPSD Hamburg

$V_0 = 4, V_1 = 0$ ; Black: free, Blue:  $N=3$



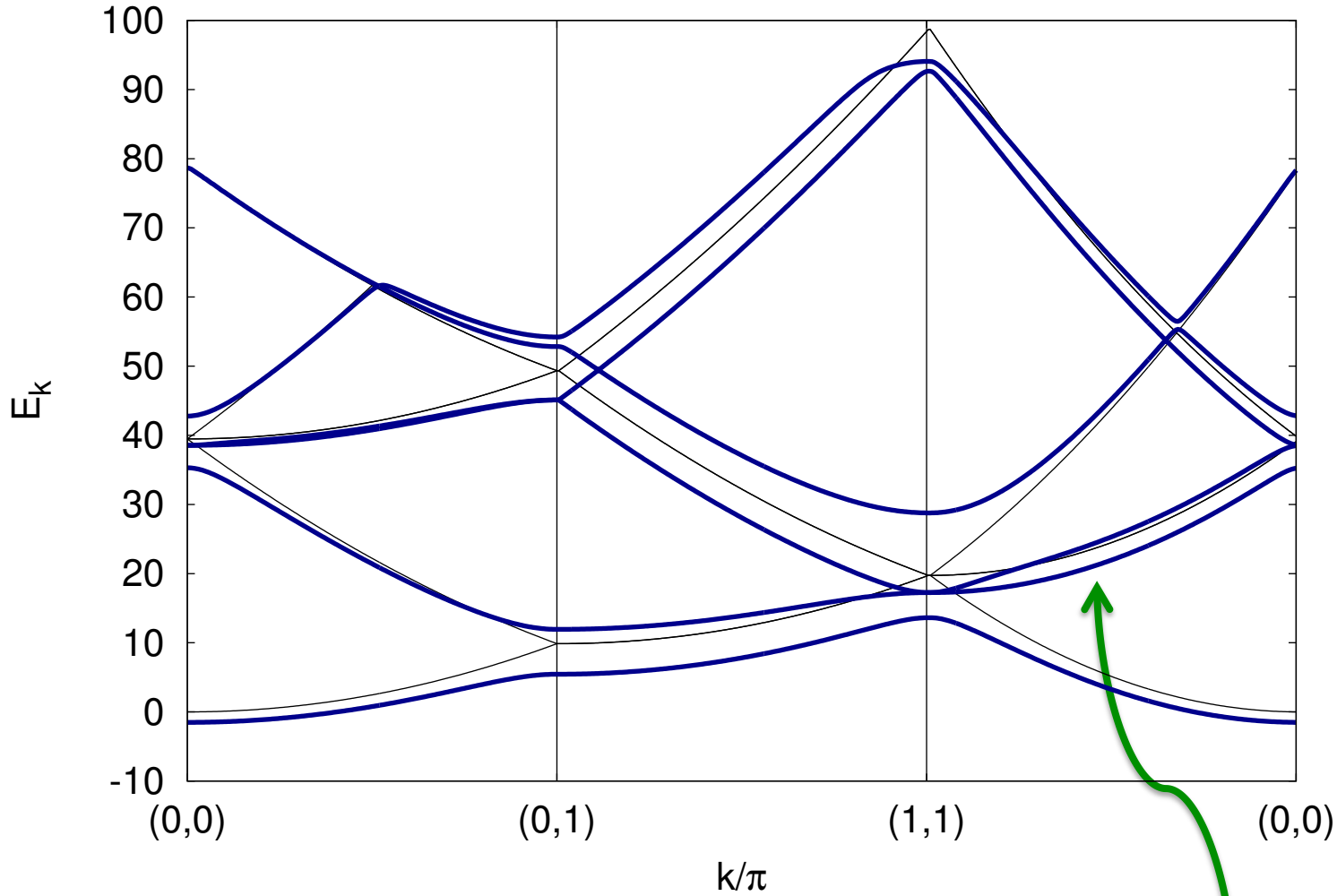
Degeneracies lifted but still metallic  
Fermi surface: Hole and electron pockets  
for 2 electrons per unit cell

$V_0 = 8, V_1 = 0$ ; Black: free, Blue:  $N=3$



Insulator: Indirect band gap  
for 2 electrons per unit cell

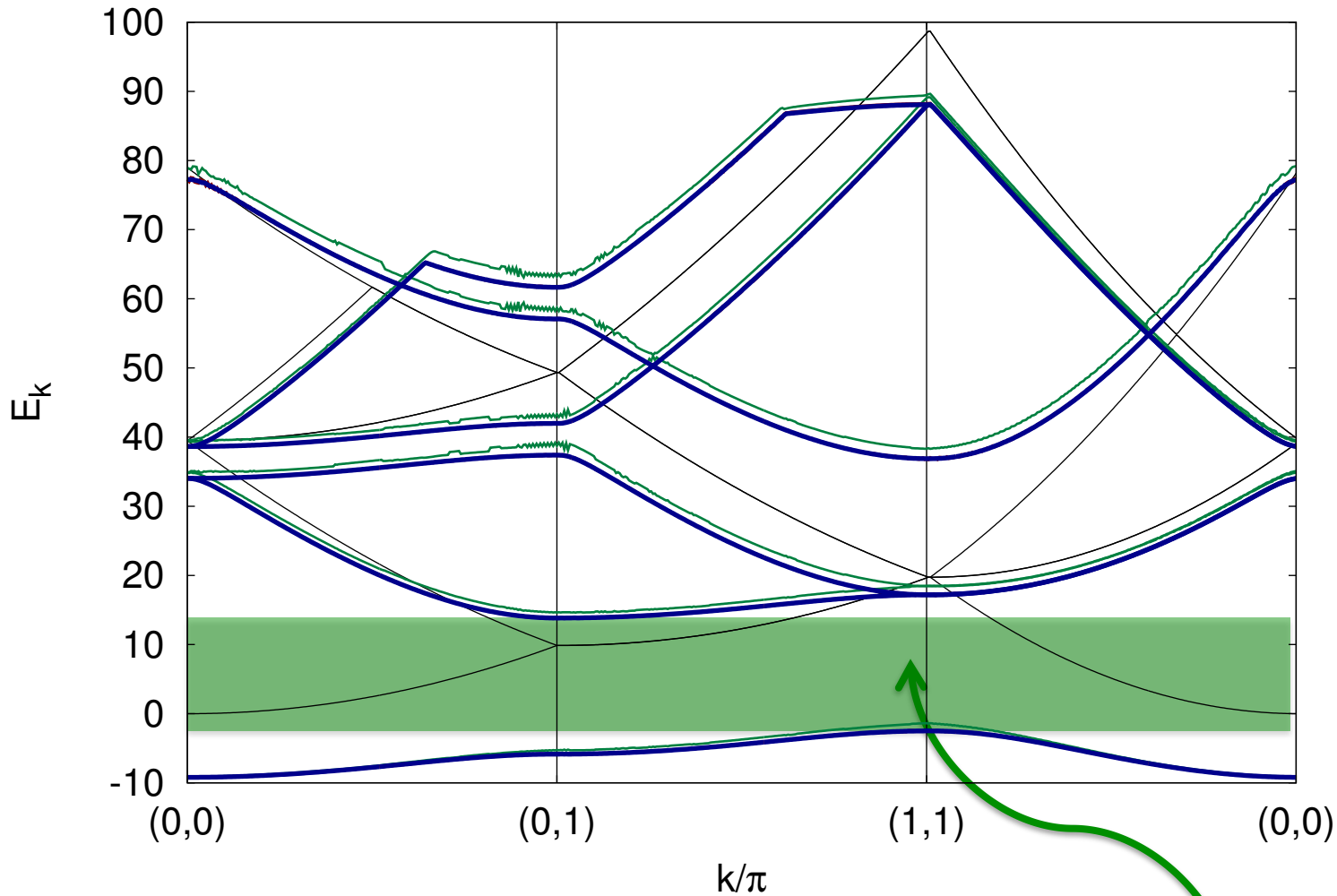
$V_0 = 8, V_1 = 4$ ; Black: free, Blue:  $N=3$



Lifting of degeneracies in 1st order perturbation theory due to  $V_1 > 0$

$V_0 = 20, V_1 = 0$ ; Black: free, Green:  $N=1$ , Red:  $N=2$ , Blue:  $N=3$

Check convergence with  $N = \#$ plane waves



Strong potential: Lowest band becomes flat  
tight-binding limit, see below

Insulator: Indirect band gap  
for 2 electrons per unit cell